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PERCENTILE POINTS OF ORDER STATISTICS IN  
SAMPLES FROM BETA, NORMAL, CHI (1 D.F.) POPULATIONS

by

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SAMPLES FROM BETA, NORMAL, CHI (1 D.F.) POPULATIONS

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0. ABSTRACT

If  $p(\alpha, i, N)$  denotes the  $\alpha^{\text{th}}$  probability point of  $i^{\text{th}}$  smallest order statistic in random samples of size  $N$  drawn from the Beta distribution,  $p(\alpha, i, N)$  is computed accurate to eight decimal places for  $N = 1(1)30(5)60$ ,  $i = 1(1) 1+[N/2]$  and  $\alpha = 0.01, 0.025, 0.10, 0.25, 0.50, 0.75, 0.90, 0.95, 0.99$ . Also, the 25th, 50th and 75th percentile points of the Beta distribution for  $N = 65(5)100$ ,  $i = 1(1) 1+[N/2]$  are computed with the same accuracy. Using the above values the percentile points of the normal, chi (1 d.f.) and Weibull order statistics in samples of sizes up to and including 30 are computed accurate to 4 or 5 decimal places. Applications of these tables are indicated.

1. INTRODUCTION

Pearson [9] has provided extensive tables of the incomplete Beta distribution. It was realized that certain percentage points of the incomplete

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Beta distribution were more useful than the complete distribution of the incomplete Beta. Thompson [10] tabulated the percentage points of the incomplete Beta distribution accurate to five significant figures for  $v_1 = 1(1)10, 12, 15, 20, 24, 30, 40, 60, 120; v_2 = 1(1)30, 40, 60, 120, \infty; \alpha = 0.005, 0.01, 0.025, 0.05, 0.10, 0.25, 0.50$  where  $v_1$  and  $v_2$  denote the parameters of the Beta distribution and  $\alpha$  denotes the percentage. Comrie and Hartley [2] gave methods of interpolation in the tables of Thompson [10]. Cochran [1] gave an approximate formula for the percentage points of the incomplete Beta distribution, for large values of its parameters. Eisenhart et al [3] tabulated accurate to five significant figures, the percentile points of the median in samples from the uniform distribution of sizes  $N = 3(2)15(10)95$  and for  $\alpha = 0.001, 0.005, 0.01, 0.025, 0.05, 0.10, 0.20, 0.25$ . Applying inverse interpolation in Pearson's [9] tables, Gupta [5] tabulated the percentile points of the order statistics in samples drawn from the gamma population with even degrees of freedom. Leone et al [8] tabulated the percentile points of the binomial distribution for sample sizes  $N = 10(5)100$  and  $\alpha = 0.0025, 0.005, 0.01, 0.025, 0.05, 0.1, 0.9, 0.95, 0.975, 0.99, 0.995, 0.9975$ . Using Thompson's [10] and other values, Eisenhart [4] tabulated accurate to five significant figures the probability points of order statistics in random samples of size  $N$  from a uniform distribution, for  $N = 1(1)10$  and for  $\alpha = 0.001, 0.005, 0.01, 0.025, 0.05, 0.10, 0.20, 0.25, 0.50$ .

Some rank order test statistics for instance, Terry's  $c_1$ -test statistic and Fraser's [5] test for symmetry, are linear sums of expected values of order statistics in samples from standard normal and standard positive normal populations respectively. In the place of the expected values of order statistics, one could use the percentile points of the order statistics. Hence, it is of interest to prepare tables of the percentage points of order statistics in samples from a uniform distribution. The percentage points of order statistics

in samples drawn from any continuous population can be obtained by taking the inverse of the percentage points of the uniform order statistics, with respect to the cumulative distribution function of the underlying continuous population.

## 2. NOTATION

Let  $X_{1,N} \leq X_{2,N} \leq \dots \leq X_{N,N}$  be the order statistics in random samples of size  $N$  drawn from a continuous population having  $F(x)$  for its cumulative distribution function (c.d.f.). Let  $p(\alpha, i, N)$  denote the  $\alpha$ th percentage point of  $X_{i,N}$ . Then  $p(\alpha, i, N)$  is given by the relation

$$F(p(i, \alpha, N)) = \sum_{j=1}^{i-1} \binom{i-1}{j} F^j p(\alpha, i, N) [1 - F(p(i, \alpha, N))]^{i-j-1} = \alpha. \quad (2.1)$$

That is

$$\sum_{j=1}^{i-1} \binom{i-1}{j} F^j p(\alpha, i, N) [1 - F(p(i, \alpha, N))]^{i-j-1} = \alpha. \quad (2.2)$$

Thus, one can find  $p(\alpha, i, N)$  by solving Equation (2.2) for  $F(p(\alpha, i, N))$  and then taking its inverse with respect to  $F$ . A similar approach was made by Leone et al [8] for computing the percentiles of the binomial distribution. Unless otherwise stated,  $p$  denotes  $p(\alpha, i, N)$ . Throughout  $\Phi$  denotes the standard normal c.d.f. given by

$$\Phi(x) = (2\pi)^{-\frac{1}{2}} \int_{-\infty}^x e^{-t^2/2} dt. \quad (2.3)$$

## 3. METHODS OF COMPUTATION

The percentage points of the uniform order statistics were computed by Newton-Raphson iteration using the following polynomial representation for the relation when  $N$  and  $i$  are integral:

$$\sum_{j=i}^N \binom{N}{j} \cdot p(\alpha, i, N) [1-p(\alpha, i, N)]^{N-j} = \alpha.$$

The derivative of the left hand side expression of the above equation is evaluated from its integral representation given in (2.1). Double precision arithmetic was used when necessary to obtain eight decimal accuracy, that is, iteration was continued until the absolute difference between two iterations was less than  $10^{-9}$ . Since the percentage points of the uniform order statistics are roots of certain polynomials which constitute upper tails of the binomial distribution, our values given in Table 1 are related to the percentile points of the binomial distribution given by Leone et al [8]. The values of Leone et al [8] agree with our value to at least seven decimal places. In Table 1, the percentage points of the uniform order statistics are presented for  $N = 1(1)30(5)60$ ,  $i = 1(1) 1+[N/2]$  and  $\alpha = 0.01, 0.025, 0.10, 0.25, 0.50, 0.75, 0.90, 0.975, 0.99$ . The values for  $i > 1+[N/2]$  are obtained by using the relation

$$B_{1-p}(N+1-i, i) = 1 - B_p(i, N-i+1). \quad (3.1)$$

The percentage points of order statistics in random samples from any continuous population can be obtained by taking the inverse of the percentage points of the uniform order statistics with respect to the c.d.f. of the population. Thus, the percentage points of the normal order statistics are given by

$$x(p, i, N) = \Phi^{-1}(p(\alpha, i, N)) \quad (3.2)$$

Also, the c.d.f. of the positive normal (chi 1 d.f.) distribution is related to the normal c.d.f. by

$$\begin{aligned} x(x) &= 2\Phi(x) - 1, & x > 0, \\ &= c & \text{otherwise.} \end{aligned} \quad (3.3)$$

The percentage points of the chi-order statistics are given by

$$x(p,i,N) = \Phi^{-1} ((1+p)/2). \quad (3.4)$$

Hastings [7] approximation to  $\Phi$  was used. This approximation is given by

$$\Phi(x) = 1 - e^{-x^2/2} \sum_{k=1}^5 a_k \eta^k, \quad x \geq 0$$

where  $\eta = (1 + 2^{-1} xb)^{-1}$   
 $b = 0.32759110$   
 $a_1 = 0.12741479$   
 $a_2 = -0.14224838$   
 $a_3 = 0.71070690$   
 $a_4 = -0.72657604$   
 $a_5 = 0.53070273,$

when  $x < 0$ , the approximation is obtained by considering  $1 - \Phi(-x)$ . After using this approximation for  $\Phi$ , Newton-Raphson iteration was used to solve for  $x(p,i,N)$ . The percentage points of normal order statistics accurate to four decimal places are given in Table 2 for  $N = 1(1)30$ ,  $i = 1(1) 1+[N/2]$ . The other values can be obtained by symmetry. The percentage points of the chi-order statistics accurate to four decimal places are presented in Table 3 for  $N = 1(1)30$ ,  $i = 1(1)N$ . The percentage points of the Weibull order statistics are given by

$$x(p,i,N) = (-\ln p)^{1/c} \quad (3.5)$$

where  $c$  denotes the shape parameter of the Weibull distribution, the c.d.f. of which is given by  $1-\exp(-x^c)$ . The percentage points of the Weibull order statistics accurate to five decimal places are presented in Table 4 for

$N = 1(1)30$ ,  $i = 1(1)N$ ,  $c = 2.0, 2.5$  and  $5.0$ .

Certain minor errors have been uncovered in the tables of Thompson [10]. These are presented in Table 3.1.

Table 3.1

| $\alpha$ | $i$ | $N$ | Ours       | Thompson's |
|----------|-----|-----|------------|------------|
| 0.01     | 13  | 27  | 0.25722525 | 0.25722    |
| 0.01     | 1   | 30  | 0.00033495 | 0.00033496 |
| 0.025    | 4   | 15  | 0.07787154 | 0.077871   |
| 0.05     | 4   | 23  | 0.06167552 | 0.061675   |

All the computations were done on Burroughs 220. The computations of the tables presented here took about thirty hours of machine time.

#### 4. APPLICATIONS

4.1 The percentile points of the uniform order statistics can be used to find the percentile points of the Fisher's F distribution. If  $F_{\alpha, 2m, 2n}$  denotes the  $\alpha^{th}$  percentage points on the F distribution with  $2m, 2n$  degrees of freedom, then

$$F_{\alpha, 2m, 2n} = n p(\alpha, m, m+n-1) / m[1-p(\alpha, m, m+n-1)] \quad (4.1)$$

where  $p(\alpha, m, m+n-1)$  is the  $\alpha^{th}$  percentage point of the  $m^{th}$  smallest order statistic in random samples of size  $m+n-1$  drawn from the uniform population on (0,1). Obviously, Table 1 is useful in life-testing problems as indicated by Leone et al [8] and in approximating the percentage points of the hypergeometric distribution as suggested by Thompson [10].

An application of the percentile points of the chi-order statistics is as follows: consider a random variable  $X$  having the density function given by

$$f(x,\theta) = (2/\pi)^{\frac{1}{2}} e^{-\frac{1}{2}(x-\theta)^2}, \quad x > \theta$$

$$= 0 \quad \text{otherwise.}$$

Let  $X_{1,N} \leq X_{2,N} \leq \dots \leq X_{N,N}$  be the order statistics in a random sample of size  $N$  drawn from this population. We wish to test the hypothesis:  $\theta=0$  against the hypothesis:  $\theta > 0$ .  $X_{1,N}$  can be a reasonable test statistic. The percentile points of the smallest chi-order statistic can be used to obtain the critical values of  $X_{1,N}$ .

Similarly, let  $X_{1,N} \leq X_{2,N} \leq \dots \leq X_{N,N}$  be the order statistics in a random sample of size  $N$  drawn from a Weibull population having the following density function.

$$f(x,\theta) = c(x-\theta)^{c-1} e^{-(x-\theta)^c}, \quad x > \theta$$

$$= 0 \quad \text{otherwise,}$$

where  $c$  is assumed to be known exactly. Then, a reasonable test statistic for testing the hypothesis:  $\theta=0$  against the hypothesis:  $\theta > 0$ , could be  $X_{1,N}$ . In order to carry out the test procedure, the percentile points of the smallest Weibull order statistic are required.

## 5. CONCLUSION

Our tables are more extensive and more accurate than tables available at present. No attempts were made to propose interpolation and extrapolation methods. The harmonic interpolation method proposed by Comrie and Hartley [2] is also applicable here but it involves use of special tables. Linear interpolation for a fixed percentage seems to give 3 to 4 decimal accuracy for  $N \leq 15$ .

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## DIFERENTILE POINTS OF THE ACTA DISTRIBUTION

| N  | 1 | .01        | .025       | .05        | .10        | .25        | .50        | .75        | .90         | .95        | .975       | .99        |
|----|---|------------|------------|------------|------------|------------|------------|------------|-------------|------------|------------|------------|
| 2  | 1 | .00501256  | .01257912  | .02537057  | .05111671  | .13397459  | .29239321  | .50000000  | .63177221   | .77649320  | .84188601  | .90000000  |
| 3  | 1 | .00734461  | .00846176  | .01695263  | .04511663  | .09149371  | .21629945  | .37002951  | .51586112   | .63150685  | .70759823  | .78455653  |
| 4  | 2 | .00890314  | .00420933  | .12515637  | .19580111  | .32636183  | .50000000  | .57364820  | .96419989   | .96464964  | .60570069  | .94100284  |
| 5  | 1 | .00750943  | .00630948  | .07650675  | .1076145   | .16939514  | .16510755  | .20289312  | .44776586   | .52717037  | .60220643  | .68177223  |
| 6  | 2 | .00619086  | .00675485  | .00761146  | .12425502  | .26102207  | .38577755  | .54616787  | .57951942   | .75110527  | .80547971  | .846012740 |
| 7  | 1 | .00280085  | .00527045  | .01720852  | .01722469  | .05501260  | .10246492  | .24214165  | .45904266   | .52182275  | .60189088  |            |
| 8  | 2 | .002266507 | .00661926  | .07644638  | .07644638  | .19376361  | .31510511  | .46418061  | .54880074   | .65746052  | .71641717  | .77792771  |
| 9  | 3 | .016564985 | .04652280  | .18029551  | .24665445  | .35063616  | .50000000  | .64605637  | .81173633   | .85336720  | .89416016  |            |
| 10 | 1 | .00167366  | .00421074  | .00951744  | .01746899  | .046691571 | .101910176 | .201629947 | .311870793  | .393034777 | .459255813 | .51584112  |
| 11 | 2 | .02676219  | .014327787 | .062846088 | .09256525  | .16116222  | .26464496  | .38047249  | .51011634   | .58180144  | .64123458  | .70566613  |
| 12 | 3 | .008477995 | .01181175  | .01516111  | .020000887 | .020000887 | .020000887 | .020000887 | .05411905   | .56630561  | .72964161  | .77722190  |
| 13 | 1 | .001642673 | .003461310 | .00730063  | .01491879  | .016026648 | .016026648 | .016026648 | .17966664   | .240031433 | .34816166  | .40961576  |
| 14 | 2 | .002266507 | .00661926  | .07644638  | .07644638  | .19376361  | .31510511  | .46418061  | .54880074   | .65746052  | .71641717  | .77792771  |
| 15 | 3 | .070810383 | .09898827  | .12875664  | .16953862  | .25107400  | .36411611  | .48460969  | .59617973   | .65877856  | .70577914  | .76167595  |
| 16 | 4 | .14227728  | .18445157  | .22032166  | .279845295 | .379845295 | .50000000  | .62115156  | .72139705   | .77467842  | .81504844  | .84777062  |
| 17 | 1 | .00167366  | .00421074  | .00951744  | .01746899  | .046691571 | .101910176 | .201629947 | .311870793  | .393034777 | .459255813 | .51584112  |
| 18 | 2 | .01055787  | .021864603 | .04652280  | .062846088 | .10246492  | .24214165  | .45904266  | .52182275   | .60189088  |            |            |
| 19 | 3 | .006013950 | .00827361  | .1111271   | .14685714  | .22057714  | .32705157  | .43205157  | .53212562   | .59968931  | .65085570  | .70676768  |
| 20 | 4 | .129565017 | .15702777  | .172961182 | .212961182 | .32908246  | .44011522  | .55543612  | .655517681  | .71017598  | .74511721  | .80175598  |
| 21 | 1 | .001116078 | .002980914 | .00661926  | .01168484  | .01168484  | .01168484  | .01168484  | .01911035   | .275010574 | .31234198  | .36941665  |
| 22 | 2 | .001755645 | .002521167 | .046402316 | .06167608  | .10711257  | .17961051  | .27276365  | .340624549  | .47067131  | .52650967  | .5899200   |
| 23 | 3 | .00534874  | .017485662 | .07774665  | .129460721 | .16550724  | .28626657  | .390554108 | .49068119   | .549664165 | .59968931  | .65085570  |
| 24 | 4 | .105226230 | .12699466  | .168156648 | .2111924   | .301084881 | .45102088  | .55962014  | .655501863  | .70704093  | .74997155  |            |
| 25 | 5 | .170635511 | .21070851  | .25116078  | .301084881 | .38116384  | .50000000  | .60000000  | .60000000   | .748631237 | .787091460 | .82904889  |
| 26 | 1 | .001116078 | .002980914 | .00661926  | .01168484  | .01168484  | .01168484  | .01168484  | .01911035   | .275010574 | .31234198  | .36941665  |
| 27 | 2 | .001755645 | .002521167 | .046402316 | .06167608  | .10711257  | .17961051  | .27276365  | .340624549  | .47067131  | .52650967  | .5899200   |
| 28 | 3 | .007515100 | .00827361  | .1111271   | .14685714  | .22057714  | .32705157  | .43205157  | .53212562   | .59968931  | .65085570  | .70676768  |
| 29 | 4 | .09212182  | .12155729  | .154652784 | .218756271 | .30485061  | .44510997  | .545769615 | .645662376  | .65551721  | .70704093  |            |
| 30 | 5 | .150642284 | .197084806 | .222646111 | .26721808  | .363086808 | .463086808 | .464578187 | .6964646779 | .77467842  | .80175598  |            |
| 31 | 1 | .001116078 | .002980914 | .00661926  | .01168484  | .01168484  | .01168484  | .01168484  | .01911035   | .275010574 | .31234198  | .36941665  |
| 32 | 2 | .001755645 | .002521167 | .046402316 | .06167608  | .10711257  | .17961051  | .27276365  | .340624549  | .47067131  | .52650967  | .5899200   |
| 33 | 3 | .007515100 | .00827361  | .1111271   | .14685714  | .22057714  | .32705157  | .43205157  | .53212562   | .59968931  | .65085570  | .70676768  |
| 34 | 4 | .09212182  | .12155729  | .154652784 | .218756271 | .30485061  | .44510997  | .545769615 | .645662376  | .65551721  | .70704093  |            |
| 35 | 5 | .150642284 | .197084806 | .222646111 | .26721808  | .363086808 | .463086808 | .464578187 | .6964646779 | .77467842  | .80175598  |            |
| 36 | 6 | .19391672  | .23179261  | .27124932  | .31771582  | .411771582 | .50000000  | .59862018  | .728750099  |            |            |            |
| 37 | 1 | .000001375 | .002281119 | .003231972 | .00405184  | .0045184   | .0045184   | .0045184   | .019460872  | .278464019 | .326941615 | .362064766 |
| 38 | 2 | .015658114 | .02521167  | .03277144  | .044520562 | .056450385 | .062262774 | .062262774 | .072662750  | .112012435 | .14277992  | .165011611 |
| 39 | 3 | .007515100 | .00827361  | .1111271   | .14685714  | .22057714  | .32705157  | .43205157  | .53212562   | .59968931  | .65085570  | .70676768  |
| 40 | 4 | .09212182  | .12155729  | .154652784 | .218756271 | .30485061  | .44510997  | .545769615 | .645662376  | .65551721  | .70704093  |            |
| 41 | 5 | .150642284 | .197084806 | .222646111 | .26721808  | .363086808 | .463086808 | .464578187 | .6964646779 | .77467842  | .80175598  |            |
| 42 | 6 | .19391672  | .23179261  | .27124932  | .31771582  | .411771582 | .50000000  | .59862018  |             |            |            |            |
| 43 | 7 | .000001375 | .002281119 | .003231972 | .00405184  | .0045184   | .0045184   | .0045184   | .019460872  | .278464019 | .326941615 | .362064766 |

TABLE 1

## PERCENTILE POINTS OF THE BETA DISTRIBUTION

| N  | 1          | .01        | .025       | .05        | .10          | .25        | .50        | .75        | .90        | .95        | .975       | .99        |
|----|------------|------------|------------|------------|--------------|------------|------------|------------|------------|------------|------------|------------|
| 17 | 3          | .019898214 | .054950664 | .271870225 | .095652291   | .14585204  | .21668637  | .30117800  | .38552211  | .43810544  | .49411777  | .53744291  |
| 4  | .07594665  | .0924608   | .1228565   | .15418765  | .21616503    | .29757561  | .38877792  | .47526656  | .52732660  | .57185824  | .62219301  |            |
| 5  | .121466660 | .15165223  | .18102475  | .20868114  | .24529981    | .30817244  | .366631865 | .455950719 | .55465831  | .61772406  | .68476221  | .76510731  |
| 6  | .17460918  | .210944664 | .24529981  | .30817244  | .366631865   | .455950719 | .55465831  | .61772406  | .68476221  | .7233077   | .76510731  |            |
| 13 | 1          | .00077280  | .00194563  | .01920667  | .02805317    | .06169104  | .07409501  | .12579068  | .16232207  | .20581667  | .24705214  | .29829617  |
| 2  | .01182391  | .01220667  | .016644556 | .016644556 | .016644556   | .016644556 | .016644556 | .016644556 | .016644556 | .016644556 | .016644556 | .016644556 |
| 3  | .01577552  | .0158107   | .0158107   | .0158107   | .0158107     | .0158107   | .0158107   | .0158107   | .0158107   | .0158107   | .0158107   | .0158107   |
| 4  | .016945535 | .01692038  | .01692038  | .01692038  | .01692038    | .01692038  | .01692038  | .01692038  | .01692038  | .01692038  | .01692038  | .01692038  |
| 5  | .11682465  | .13557934  | .16565246  | .20050204  | .26676124    | .25016336  | .446028416 | .52342816  | .57261931  | .61426220  | .66089956  | .66089956  |
| 6  | .1581841   | .1922244   | .22395541  | .2637025   | .31681145    | .42507656  | .51560410  | .59823816  | .64200772  | .69422240  | .7211260   | .7211260   |
| 7  | .21287771  | .25134550  | .28706702  | .310685920 | .40901671    | .500000000 | .559058134 | .666914082 | .71295100  | .74865452  | .78112767  | .78112767  |
| 14 | 1          | .00071762  | .01180678  | .01165710  | .01165710    | .01165710  | .01165710  | .01165710  | .01165710  | .01165710  | .01165710  | .01165710  |
| 2  | .01095157  | .01179452  | .01207214  | .01207214  | .01207214    | .01207214  | .01207214  | .01207214  | .01207214  | .01207214  | .01207214  | .01207214  |
| 3  | .013065388 | .013065388 | .013065388 | .013065388 | .013065388   | .013065388 | .013065388 | .013065388 | .013065388 | .013065388 | .013065388 | .013065388 |
| 4  | .01640287  | .01689932  | .01689932  | .01689932  | .01689932    | .01689932  | .01689932  | .01689932  | .01689932  | .01689932  | .01689932  | .01689932  |
| 5  | .10192661  | .12751983  | .15271762  | .18458795  | .24757516    | .275513416 | .3117460   | .41167601  | .491196221 | .5600545   | .59105331  | .62743469  |
| 6  | .14568246  | .17661108  | .20607334  | .24315700  | .311744146   | .348351315 | .48315700  | .56311C759 | .60958513  | .64861989  | .6923023   | .6923023   |
| 7  | .19471782  | .24016054  | .26358594  | .304555391 | .37826537    | .465114666 | .553044660 | .63038683  | .67139060  | .715120041 | .75120041  | .75120041  |
| 15 | 1          | .000666980 | .01168643  | .01168643  | .01168643    | .01168643  | .01168643  | .01168643  | .01168643  | .01168643  | .01168643  | .01168643  |
| 2  | .01011918  | .011657591 | .01242575  | .01503698  | .01641909    | .01939610  | .016560506 | .013555685 | .017939619 | .019441457 | .01789056  | .01789056  |
| 3  | .01307218  | .01421119  | .01778154  | .01778154  | .01778154    | .01778154  | .01778154  | .01778154  | .01778154  | .01778154  | .01778154  | .01778154  |
| 4  | .016939019 | .01887154  | .019665835 | .019665835 | .019665835   | .019665835 | .019665835 | .019665835 | .019665835 | .019665835 | .019665835 | .019665835 |
| 5  | .019435642 | .01824111  | .016161294 | .017196803 | .021193039   | .021919319 | .011691098 | .01727311  | .01723711  | .01723711  | .01723711  | .01723711  |
| 6  | .17455763  | .15366432  | .16561692  | .19086770  | .227559130   | .29016962  | .4526429   | .57147759  | .61616627  | .65971022  | .6971022   | .6971022   |
| 7  | .17946610  | .22266673  | .24327742  | .28218421  | .31212771    | .414813270 | .50208616  | .596456881 | .660334767 | .6771053   | .71771053  | .71771053  |
| 8  | .22872790  | .25586135  | .29996646  | .34152084  | .41458947    | .500000000 | .54351n5   | .658447916 | .700C1353  | .73413864  | .77127417  | .77127417  |
| 16 | 1          | .000672795 | .011581111 | .011320669 | .011656339   | .011781194 | .016229672 | .018299596 | .013405568 | .017074972 | .02050721  | .25010579  |
| 2  | .01054358  | .01151361  | .012067877 | .01374982  | .015117407   | .01270302  | .01561071  | .022121203 | .02695740  | .03021074  | .04883832  | .04883832  |
| 3  | .02869976  | .03047373  | .031154597 | .031154597 | .031154597   | .031154597 | .031154597 | .029588919 | .029588919 | .03049327  | .03049327  | .03049327  |
| 4  | .05538108  | .07266294  | .09205244  | .11380218  | .16107953    | .224774629 | .298684697 | .37122224  | .41657228  | .45464155  | .50293639  | .50293639  |
| 5  | .08743773  | .11016495  | .13211095  | .16055945  | .2158294     | .28588592  | .376424000 | .41892195  | .44439642  | .52371142  | .56897086  | .56897086  |
| 6  | .125515897 | .15198367  | .17775584  | .21041255  | .27180648    | .34705038  | .503505974 | .54834708  | .58662064  | .62994567  | .66654592  | .66654592  |
| 7  | .166445567 | .19753414  | .226660156 | .262291544 | .320888953   | .40822650  | .549093377 | .565464095 | .59898842  | .645652191 | .68654093  | .68654093  |
| 8  | .21117164  | .26651012  | .27866167  | .31782734  | .4876226     | .646940827 | .65224787  | .62495337  | .66662581  | .70122130  | .73930772  | .73930772  |
| 17 | 1          | .00059107  | .001488117 | .001301271 | .001617851   | .011995311 | .017811036 | .012666738 | .016156528 | .019506277 | .023730141 | .023730141 |
| 2  | .00896121  | .014577932 | .01798506  | .04988215  | .066666754   | .102514749 | .15421749  | .21021099  | .25012445  | .28688940  | .33163330  | .33163330  |
| 3  | .02692222  | .01798506  | .04988215  | .066666754 | .066666754   | .066666754 | .066666754 | .066666754 | .066666754 | .066666754 | .06692343  | .06692343  |
| 4  | .051088448 | .06110774  | .084664508 | .106816655 | .151440314   | .21178500  | .28207632  | .35186893  | .41654143  | .43421787  | .4774104   | .4774104   |
| 5  | .08216364  | .10135552  | .123777092 | .15057692  | .20203033    | .26940046  | .344316893 | .416338919 | .46054867  | .49899177  | .54318762  | .54318762  |
| 6  | .11680177  | .14209747  | .15636267  | .19711645  | .25433304    | .32703812  | .401512716 | .47807148  | .52191769  | .55953180  | .60251329  | .60251329  |
| 7  | .15523681  | .184643696 | .21199815  | .24613683  | .309818072   | .374668723 | .4655626   | .51735687  | .561029465 | .61671634  | .657070948 | .657070948 |
| 8  | .19710564  | .22967268  | .26011442  | .297275716 | .34631801442 | .442324232 | .522287088 | .594468970 | .63599123  | .67075285  | .70938332  | .70938332  |

TABLE 1 Contd.

TABLE I. Contd.

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PERCENTILE POINTS OF THE REFTA DISTRIBUTION

| N  | 1  | .01        | .025       | .05        | .10        | .25        | .50         | .75        | .90        | .95        | .975       | .99        |
|----|----|------------|------------|------------|------------|------------|-------------|------------|------------|------------|------------|------------|
| 17 | 9  | .26224774  | .27811832  | .31032956  | .35039484  | .41992277  | .50000000   | .58007729  | .64960517  | .68917043  | .72188170  | .75775164  |
| 18 | 1  | .00045620  | .00140556  | .00282557  | .00583626  | .0158528   | .01777516   | .07412529  | .12007746  | .1531755   | .18530197  | .22575637  |
|    | 2  | .00046652  | .01375122  | .02611067  | .02994652  | .05367784  | .06150567   | .14271635  | .1966775   | .2375002   | .2794345   | .31602487  |
|    | 3  | .0259356   | .0158508   | .041048    | .0528636   | .09675645  | .10561052   | .16271632  | .1966775   | .2375002   | .2794345   | .31602485  |
|    | 4  | .04870717  | .06409204  | .07065158  | .107664101 | .14281645  | .200200277  | .266736195 | .32144256  | .37667015  | .4147769   | .45829789  |
|    | 5  | .07718512  | .086494919 | .116252557 | .14176766  | .190200277 | .266736195  | .32144256  | .37667015  | .4147769   | .45829789  | .49808061  |
|    | 6  | .10308778  | .13242778  | .15442444  | .19560700  | .24045660  | .300200277  | .37667015  | .432656098 | .49620108  | .56237277  | .6198061   |
|    | 7  | .14546155  | .1729885   | .1989131   | .22112000  | .27008700  | .3267371387 | .404688700 | .5118309   | .556004555 | .60007275  | .65709576  |
|    | 8  | .18621111  | .21520152  | .24391126  | .270270087 | .31022261  | .362700292  | .426271387 | .5118309   | .556004555 | .60007275  | .65709576  |
|    | 9  | .2262573   | .261019060 | .27412106  | .328846579 | .392650292 | .462050292  | .526271387 | .566771546 | .62856487  | .68142471  | .72608697  |
| 19 | 1  | .000652882 | .001332160 | .002616760 | .005652006 | .015627709 | .025822500  | .070736565 | .1141321   | .145366950 | .17466501  | .21524003  |
|    | 2  | .000652882 | .001332160 | .002616760 | .005652006 | .015627709 | .025822500  | .070736565 | .1141321   | .145366950 | .17466501  | .21524003  |
|    | 3  | .023066160 | .03826262  | .04646492  | .07172370  | .09234746  | .13025076   | .17827116  | .206872001 | .23137666  | .276056487 | .30180103  |
|    | 4  | .046627468 | .06052456  | .07172370  | .09234746  | .13025076  | .17827116   | .206872001 | .23137666  | .276056487 | .30180103  | .32574002  |
|    | 5  | .07277506  | .09146577  | .11976354  | .13238554  | .17617664  | .213676705  | .25154245  | .27752591  | .31350508  | .349725171 | .38256309  |
|    | 6  | .103021261 | .12676664  | .14611065  | .17617664  | .213676705 | .25154245   | .27752591  | .31350508  | .349725171 | .38256309  | .420101135 |
|    | 7  | .145215076 | .16238586  | .18756133  | .218227174 | .25717325  | .295490754  | .34106615  | .38804738  | .425956437 | .465565057 | .505202925 |
|    | 8  | .17222211  | .195257144 | .22077153  | .252427214 | .292594754 | .330651754  | .374106615 | .41306615  | .454132711 | .491627008 | .535231014 |
|    | 9  | .212332763 | .24647467  | .27292586  | .307146801 | .347300292 | .383700292  | .426287000 | .462050292 | .50189470  | .541002116 | .581935553 |
|    | 10 | .24305311  | .285664325 | .317004552 | .357004552 | .397004552 | .437004552  | .477004552 | .517004552 | .557004552 | .591935553 | .635231014 |
| 20 | 1  | .000652882 | .001332160 | .002616760 | .005652006 | .015627709 | .025822500  | .070736565 | .1141321   | .145366950 | .17466501  | .21524003  |
|    | 2  | .000652882 | .001332160 | .002616760 | .005652006 | .015627709 | .025822500  | .070736565 | .1141321   | .145366950 | .17466501  | .21524003  |
|    | 3  | .023066160 | .03826262  | .04646492  | .07172370  | .09234746  | .13025076   | .17827116  | .206872001 | .23137666  | .276056487 | .30180103  |
|    | 4  | .046627468 | .06052456  | .07172370  | .09234746  | .13025076  | .17827116   | .206872001 | .23137666  | .276056487 | .30180103  | .32574002  |
|    | 5  | .07277506  | .09146577  | .11976354  | .13238554  | .17617664  | .213676705  | .25154245  | .27752591  | .31350508  | .349725171 | .38256309  |
|    | 6  | .103021261 | .12676664  | .14611065  | .17617664  | .213676705 | .25154245   | .27752591  | .31350508  | .349725171 | .38256309  | .420101135 |
|    | 7  | .145215076 | .16238586  | .18756133  | .218227174 | .25717325  | .295490754  | .34106615  | .38804738  | .425956437 | .465565057 | .505202925 |
|    | 8  | .17222211  | .195257144 | .22077153  | .252427214 | .292594754 | .330651754  | .374106615 | .41306615  | .454132711 | .491627008 | .535231014 |
|    | 9  | .212332763 | .24647467  | .27292586  | .307146801 | .347300292 | .383700292  | .426287000 | .462050292 | .50189470  | .541002116 | .581935553 |
|    | 10 | .24305311  | .285664325 | .317004552 | .357004552 | .397004552 | .437004552  | .477004552 | .517004552 | .557004552 | .591935553 | .635231014 |
| 21 | 1  | .000652882 | .001332160 | .002616760 | .005652006 | .015627709 | .025822500  | .070736565 | .1141321   | .145366950 | .17466501  | .21524003  |
|    | 2  | .000652882 | .001332160 | .002616760 | .005652006 | .015627709 | .025822500  | .070736565 | .1141321   | .145366950 | .17466501  | .21524003  |
|    | 3  | .023066160 | .03826262  | .04646492  | .07172370  | .09234746  | .13025076   | .17827116  | .206872001 | .23137666  | .276056487 | .30180103  |
|    | 4  | .046627468 | .06052456  | .07172370  | .09234746  | .13025076  | .17827116   | .206872001 | .23137666  | .276056487 | .30180103  | .32574002  |
|    | 5  | .07277506  | .09146577  | .11976354  | .13238554  | .17617664  | .213676705  | .25154245  | .27752591  | .31350508  | .349725171 | .38256309  |
|    | 6  | .103021261 | .12676664  | .14611065  | .17617664  | .213676705 | .25154245   | .27752591  | .31350508  | .349725171 | .38256309  | .420101135 |
|    | 7  | .145215076 | .16238586  | .18756133  | .218227174 | .25717325  | .295490754  | .34106615  | .38804738  | .425956437 | .465565057 | .505202925 |
|    | 8  | .17222211  | .195257144 | .22077153  | .252427214 | .292594754 | .330651754  | .374106615 | .41306615  | .454132711 | .491627008 | .535231014 |
|    | 9  | .212332763 | .24647467  | .27292586  | .307146801 | .347300292 | .383700292  | .426287000 | .462050292 | .50189470  | .541002116 | .581935553 |
|    | 10 | .24305311  | .285664325 | .317004552 | .357004552 | .397004552 | .437004552  | .477004552 | .517004552 | .557004552 | .591935553 | .635231014 |
| 22 | 1  | .000652882 | .001332160 | .002616760 | .005652006 | .015627709 | .025822500  | .070736565 | .1141321   | .145366950 | .17466501  | .21524003  |

PERCENTILE POINTS OF THF RETA DISTRIBUTION

| N  | I  | .01        | .025       | .05        | .10        | .25         | .50        | .75         | .90        | .95        | .975       | .99        |
|----|----|------------|------------|------------|------------|-------------|------------|-------------|------------|------------|------------|------------|
| 22 | 2  | .006876765 | .011205558 | .016397552 | .024440668 | .043741068  | .075123998 | .11777056   | .16558937  | .19812213  | .228444440 | .245840047 |
|    | 3  | .020567004 | .020565885 | .038223551 | .05117613  | .07904265   | .11972605  | .17052794   | .2242239   | .259466653 | .27161274  | .310490095 |
|    | 4  | .05062986  | .051867370 | .064669562 | .08174680  | .11657817   | .16488642  | .22119397   | .27892779  | .3159120   | .349727696 |            |
|    | 5  | .0213623   | .07820625  | .09490553  | .11490553  | .15568898   | .20910638  | .27458887   | .31310637  | .36909113  | .40285578  | .44263344  |
|    | 6  | .08789305  | .10728224  | .12602401  | .15002156  | .19564528   | .25384337  | .31866422   | .38111717  | .41979995  | .45370362  | .49326073  |
|    | 7  | .11620744  | .13864653  | .15994128  | .18673900  | .216559905  | .29829186  | .366670506  | .42989681  | .468640456 | .50222120  | .541205572 |
|    | 8  | .14615940  | .17197454  | .19216258  | .24484554  | .28136629   | .34336550  | .41260251   | .476164127 | .51545674  | .54872444  | .58493952  |
|    | 9  | .17913782  | .20709313  | .23222386  | .26416181  | .32068322   | .38810157  | .45852408   | .52274997  | .56086784  | .59362333  | .63010190  |
|    | 10 | .21280582  | .24396185  | .27131321  | .30666175  | .36716792   | .43289509  | .50785025   | .55751572  | .59084422  | .63655304  | .67234765  |
|    | 11 | .25081172  | .28210583  | .31126361  | .34671889  | .40726112   | .47761194  | .54857986   | .61119410  | .64745592  | .67789525  | .71197077  |
| 23 | 1  | .000637688 | .001200117 | .00222766  | .004550462 | .012429990  | .02968725  | .05869316   | .095266428 | .12222319  | .14818513  | .18145227  |
|    | 2  | .01063928  | .01063926  | .02776151  | .04890177  | .07552222   | .11457554  | .16242846   | .21584097  | .24924875  | .27020397  | .25567091  |
|    | 3  | .046503902 | .061651528 | .08651528  | .09480177  | .09510634   | .11457554  | .16242846   | .21584097  | .24924875  | .27020397  | .31812361  |
|    | 4  | .01762503  | .016505166 | .061675552 | .078082465 | .081675552  | .11446886  | .15716732   | .21202400  | .26721373  | .30363770  | .33288914  |
|    | 5  | .01210643  | .074661041 | .08710698  | .109710698 | .148661041  | .164866104 | .20116116   | .24716116  | .29166104  | .33181189  | .36680802  |
|    | 6  | .08113734  | .10228613  | .12021456  | .143118424 | .18695730   | .242993820 | .30519736   | .36626321  | .40380287  | .43103073  | .47581316  |
|    | 7  | .11665737  | .13216287  | .15209567  | .17811781  | .226660578  | .28570845  | .35117085   | .41317085  | .46007540  | .49305107  | .52262468  |
|    | 8  | .14961612  | .16476161  | .18641647  | .21641647  | .26561647   | .34585166  | .42561647   | .48561647  | .54687447  | .59619114  | .65261647  |
|    | 9  | .17462644  | .19776161  | .22167585  | .25181667  | .302167585  | .371624524 | .4340011608 | .50291343  | .564655586 | .572616506 | .60939821  |
|    | 10 | .203124406 | .23116118  | .258212292 | .290126864 | .347227577  | .414161452 | .48716124   | .546217669 | .587151487 | .614581104 | .65015251  |
|    | 11 | .27241474  | .29815621  | .32511436  | .36717171  | .387146161  | .45715698  | .526727704  | .587151094 | .64246064  | .655015104 | .689736161 |
|    | 12 | .27529332  | .29587798  | .325114765 | .370111620 | .432077596  | .50306000  | .569272400  | .622988380 | .66446235  | .694612700 | .72670267  |
| 24 | 1  | .000641868 | .001105645 | .001211694 | .001211694 | .001211694  | .02866806  | .05512569   | .09198242  | .117734616 | .14247264  | .17459581  |
|    | 2  | .006613032 | .01126464  | .01567400  | .023366562 | .04193706   | .04193706  | .04193706   | .04193706  | .04193706  | .04193706  | .04193706  |
|    | 3  | .01819292  | .01565312  | .031916322 | .05682277  | .072441221  | .072441221 | .072441221  | .072441221 | .072441221 | .072441221 | .072441221 |
|    | 4  | .05597841  | .04731366  | .07158746  | .08715874  | .10715874   | .142730780 | .19172406   | .244974930 | .295817921 | .3118C735  | .37784171  |
|    | 5  | .07798728  | .09772901  | .11401056  | .136694473 | .170900962  | .22986664  | .293555579  | .352766496 | .389119215 | .42151286  | .46951092  |
|    | 6  | .11616196  | .12615210  | .14616196  | .170900962 | .2170900962 | .27461607  | .331513199  | .38019762  | .44159556  | .47872791  | .51094781  |
|    | 7  | .14544864  | .18799291  | .211545555 | .240559895 | .270205843  | .335621099 | .422929082  | .494690077 | .521422289 | .55271962  | .58964984  |
|    | 8  | .15254466  | .18799291  | .211545555 | .240559895 | .270205843  | .335621099 | .422929082  | .494690077 | .521422289 | .55271962  | .58964984  |
|    | 9  | .19550865  | .22116292  | .245211629 | .263319861 | .27721297   | .312205657 | .37721297   | .43831497  | .506429219 | .562641184 | .627050567 |
|    | 10 | .22659232  | .25530622  | .282235552 | .31475515  | .3171846652 | .34381497  | .390642818  | .457624235 | .50321493  | .56782229  | .613566935 |
|    | 11 | .25593467  | .29124177  | .31317146  | .35311746  | .41195928   | .47945825  | .536746561  | .601755265 | .64243604  | .67179192  | .704666251 |
| 25 | 1  | .00064193  | .001101220 | .001204963 | .001211694 | .001211694  | .02744498  | .053946132  | .07144132  | .117292728 | .13718517  | .16823623  |
|    | 2  | .01654643  | .018583958 | .011461318 | .012147780 | .013848646  | .01662102  | .01662102   | .01662102  | .01662102  | .01662102  | .01662102  |
|    | 3  | .01801305  | .02546658  | .03511058  | .04491145  | .05949752   | .07055270  | .075186542  | .075186542 | .075186542 | .075186542 | .075186542 |
|    | 4  | .034467004 | .065377445 | .056656255 | .07166181  | .112433572  | .14422462  | .19581168   | .24861831  | .28172251  | .31219031  | .34878008  |
|    | 5  | .06421635  | .06821146  | .08220091  | .1056178   | .12661585   | .1441988   | .22956385   | .29467656  | .329608810 | .36082445  | .39792280  |
|    | 6  | .07654648  | .09356644  | .113967532 | .13631092  | .207552803  | .26314057  | .324556481  | .38310857  | .41952001  | .46128802  | .48837309  |
|    | 7  | .10171507  | .12071667  | .13947532  | .16311092  | .207552803  | .26314057  | .324556481  | .38310857  | .41952001  | .46128802  | .48837309  |
|    | 8  | .12733072  | .14949443  | .17031364  | .19624591  | .24981810   | .30265541  | .36609686   | .4252417   | .46220335  | .49187682  | .530561141 |
|    | 9  | .1522934   | .17671682  | .20237776  | .24031177  | .28086553   | .34721347  | .40709272   | .466736120 | .50364086  | .530360072 | .57106127  |
|    | 10 | .18475632  | .211253482 | .21553613  | .26529205  | .318161354  | .447676136 | .507075154  | .564393321 | .57479345  | .61002711  |            |

TABLE 1 Contd.

## PERCENTILE POINTS OF THE RTFA DISTRIBUTION

| N  | 1  | .01       | .025      | .05       | .10        | .25       | .50        | .75       | .90       | .95       | .975      | .99       |
|----|----|-----------|-----------|-----------|------------|-----------|------------|-----------|-----------|-----------|-----------|-----------|
| 26 | 1  | 21567405  | 24602165  | 26986305  | 3011212    | 35637050  | 42107480   | 48765614  | 54771701  | 5816106   | 61334650  | 66756220  |
| 26 | 12 | 24786267  | 27796502  | 30512666  | 32773605   | 39477654  | 46053719   | 52777865  | 56666788  | 62137864  | 66071837  | 68313888  |
| 26 | 13 | 29467704  | 31365704  | 34133665  | 35151648   | 433551981 | 50606060   | 55668951  | 62485852  | 65161124  | 68694996  | 71595906  |
| 26 | 14 | 30738768  | 33007729  | 37797887  | 4076066412 | 411100268 | 475670725  | 55192260  | 68475729  | 70883036  | 74227236  | 781227669 |
| 26 | 15 | 37580901  | 40005538  | 43820504  | 47064450   | 507606474 | 5706064461 | 61453161  | 6683122   | 69536955  | 72992488  | 76894486  |
| 26 | 16 | 41730072  | 47246696  | 52071821  | 56152186   | 60152682  | 67152670   | 71528052  | 76210702  | 79177145  | 821707365 | 85217092  |
| 26 | 17 | 46199219  | 51256346  | 56521165  | 60291282   | 65621266  | 72062266   | 78062266  | 82901265  | 8516066   | 88220982  | 91220982  |
| 26 | 18 | 48420752  | 54656811  | 60731652  | 65617495   | 70865609  | 76291268   | 812907552 | 85217451  | 87190126  | 9016066   | 93220982  |
| 26 | 19 | 57933054  | 64078612  | 69557446  | 74527614   | 81736577  | 87173657   | 92173657  | 972173657 | 981624942 | 981624942 | 981624942 |
| 26 | 20 | 61491562  | 67173222  | 71655746  | 76927802   | 82173657  | 87173657   | 92173657  | 972173657 | 981624942 | 981624942 | 981624942 |
| 26 | 21 | 67296162  | 7179216   | 76265694  | 81625694   | 861625694 | 91625694   | 961625694 | 101625694 | 10625694  | 111625694 | 11625694  |
| 26 | 22 | 71615762  | 77216     | 81721613  | 86265694   | 91625694  | 961625694  | 101625694 | 10625694  | 111625694 | 11625694  | 121625694 |
| 26 | 23 | 7762162   | 8281621   | 86265694  | 91625694   | 961625694 | 101625694  | 10625694  | 111625694 | 11625694  | 121625694 | 12625694  |
| 26 | 24 | 8281621   | 87862413  | 92816213  | 97862413   | 102816213 | 107862413  | 112816213 | 117862413 | 122816213 | 127862413 | 132816213 |
| 26 | 25 | 87862413  | 92816213  | 97862413  | 102816213  | 107862413 | 112816213  | 117862413 | 122816213 | 127862413 | 132816213 | 137862413 |
| 26 | 26 | 92816213  | 97862413  | 102816213 | 107862413  | 112816213 | 117862413  | 122816213 | 127862413 | 132816213 | 137862413 | 142816213 |
| 26 | 27 | 97862413  | 102816213 | 107862413 | 112816213  | 117862413 | 122816213  | 127862413 | 132816213 | 137862413 | 142816213 | 147862413 |
| 26 | 28 | 102816213 | 107862413 | 112816213 | 117862413  | 122816213 | 127862413  | 132816213 | 137862413 | 142816213 | 147862413 | 152816213 |
| 26 | 29 | 107862413 | 112816213 | 117862413 | 122816213  | 127862413 | 132816213  | 137862413 | 142816213 | 147862413 | 152816213 | 157862413 |
| 26 | 30 | 112816213 | 117862413 | 122816213 | 127862413  | 132816213 | 137862413  | 142816213 | 147862413 | 152816213 | 157862413 | 162816213 |
| 26 | 31 | 117862413 | 122816213 | 127862413 | 132816213  | 137862413 | 142816213  | 147862413 | 152816213 | 157862413 | 162816213 | 167862413 |
| 26 | 32 | 122816213 | 127862413 | 132816213 | 137862413  | 142816213 | 147862413  | 152816213 | 157862413 | 162816213 | 167862413 | 172816213 |
| 26 | 33 | 127862413 | 132816213 | 137862413 | 142816213  | 147862413 | 152816213  | 157862413 | 162816213 | 167862413 | 172816213 | 177862413 |
| 26 | 34 | 132816213 | 137862413 | 142816213 | 147862413  | 152816213 | 157862413  | 162816213 | 167862413 | 172816213 | 177862413 | 182816213 |
| 26 | 35 | 137862413 | 142816213 | 147862413 | 152816213  | 157862413 | 162816213  | 167862413 | 172816213 | 177862413 | 182816213 | 187862413 |
| 26 | 36 | 142816213 | 147862413 | 152816213 | 157862413  | 162816213 | 167862413  | 172816213 | 177862413 | 182816213 | 187862413 | 192816213 |
| 26 | 37 | 147862413 | 152816213 | 157862413 | 162816213  | 167862413 | 172816213  | 177862413 | 182816213 | 187862413 | 192816213 | 197862413 |
| 26 | 38 | 152816213 | 157862413 | 162816213 | 167862413  | 172816213 | 177862413  | 182816213 | 187862413 | 192816213 | 197862413 | 202816213 |
| 26 | 39 | 157862413 | 162816213 | 167862413 | 172816213  | 177862413 | 182816213  | 187862413 | 192816213 | 197862413 | 202816213 | 207862413 |
| 26 | 40 | 162816213 | 167862413 | 172816213 | 177862413  | 182816213 | 187862413  | 192816213 | 197862413 | 202816213 | 207862413 | 212816213 |
| 26 | 41 | 167862413 | 172816213 | 177862413 | 182816213  | 187862413 | 192816213  | 197862413 | 202816213 | 207862413 | 212816213 | 217862413 |
| 26 | 42 | 172816213 | 177862413 | 182816213 | 187862413  | 192816213 | 197862413  | 202816213 | 207862413 | 212816213 | 217862413 | 222816213 |
| 26 | 43 | 177862413 | 182816213 | 187862413 | 192816213  | 197862413 | 202816213  | 207862413 | 212816213 | 217862413 | 222816213 | 227862413 |
| 26 | 44 | 182816213 | 187862413 | 192816213 | 197862413  | 202816213 | 207862413  | 212816213 | 217862413 | 222816213 | 227862413 | 232816213 |
| 26 | 45 | 187862413 | 192816213 | 197862413 | 202816213  | 207862413 | 212816213  | 217862413 | 222816213 | 227862413 | 232816213 | 237862413 |
| 26 | 46 | 192816213 | 197862413 | 202816213 | 207862413  | 212816213 | 217862413  | 222816213 | 227862413 | 232816213 | 237862413 | 242816213 |
| 26 | 47 | 197862413 | 202816213 | 207862413 | 212816213  | 217862413 | 222816213  | 227862413 | 232816213 | 237862413 | 242816213 | 247862413 |
| 26 | 48 | 202816213 | 207862413 | 212816213 | 217862413  | 222816213 | 227862413  | 232816213 | 237862413 | 242816213 | 247862413 | 252816213 |
| 26 | 49 | 207862413 | 212816213 | 217862413 | 222816213  | 227862413 | 232816213  | 237862413 | 242816213 | 247862413 | 252816213 | 257862413 |
| 26 | 50 | 212816213 | 217862413 | 222816213 | 227862413  | 232816213 | 237862413  | 242816213 | 247862413 | 252816213 | 257862413 | 262816213 |
| 26 | 51 | 217862413 | 222816213 | 227862413 | 232816213  | 237862413 | 242816213  | 247862413 | 252816213 | 257862413 | 262816213 | 267862413 |
| 26 | 52 | 222816213 | 227862413 | 232816213 | 237862413  | 242816213 | 247862413  | 252816213 | 257862413 | 262816213 | 267862413 | 272816213 |
| 26 | 53 | 227862413 | 232816213 | 237862413 | 242816213  | 247862413 | 252816213  | 257862413 | 262816213 | 267862413 | 272816213 | 277862413 |
| 26 | 54 | 232816213 | 237862413 | 242816213 | 247862413  | 252816213 | 257862413  | 262816213 | 267862413 | 272816213 | 277862413 | 282816213 |
| 26 | 55 | 237862413 | 242816213 | 247862413 | 252816213  | 257862413 | 262816213  | 267862413 | 272816213 | 277862413 | 282816213 | 287862413 |
| 26 | 56 | 242816213 | 247862413 | 252816213 | 257862413  | 262816213 | 267862413  | 272816213 | 277862413 | 282816213 | 287862413 | 292816213 |
| 26 | 57 | 247862413 | 252816213 | 257862413 | 262816213  | 267862413 | 272816213  | 277862413 | 282816213 | 287862413 | 292816213 | 297862413 |
| 26 | 58 | 252816213 | 257862413 | 262816213 | 267862413  | 272816213 | 277862413  | 282816213 | 287862413 | 292816213 | 297862413 | 302816213 |
| 26 | 59 | 257862413 | 262816213 | 267862413 | 272816213  | 277862413 | 282816213  | 287862413 | 292816213 | 297862413 | 302816213 | 307862413 |
| 26 | 60 | 262816213 | 267862413 | 272816213 | 277862413  | 282816213 | 287862413  | 292816213 | 297862413 | 302816213 | 307862413 | 312816213 |
| 26 | 61 | 267862413 | 272816213 | 277862413 | 282816213  | 287862413 | 292816213  | 297862413 | 302816213 | 307862413 | 312816213 | 317862413 |
| 26 | 62 | 272816213 | 277862413 | 282816213 | 287862413  | 292816213 | 297862413  | 302816213 | 307862413 | 312816213 | 317862413 | 322816213 |
| 26 | 63 | 277862413 | 282816213 | 287862413 | 292816213  | 297862413 | 302816213  | 307862413 | 312816213 | 317862413 | 322816213 | 327862413 |
| 26 | 64 | 282816213 | 287862413 | 292816213 | 297862413  | 302816213 | 307862413  | 312816213 | 317862413 | 322816213 | 327862413 | 332816213 |
| 26 | 65 | 287862413 | 292816213 | 297862413 | 302816213  | 307862413 | 312816213  | 317862413 | 322816213 | 327862413 | 332816213 | 337862413 |
| 26 | 66 | 292816213 | 297862413 | 302816213 | 307862413  | 312816213 | 317862413  | 322816213 | 327862413 | 332816213 | 337862413 | 342816213 |
| 26 | 67 | 297862413 | 302816213 | 307862413 | 312816213  | 317862413 | 322816213  | 327862413 | 332816213 | 337862413 | 342816213 | 347862413 |
| 26 | 68 | 302816213 | 307862413 | 312816213 | 317862413  | 322816213 | 327862413  | 332816213 | 337862413 | 342816213 | 347862413 | 352816213 |
| 26 | 69 | 307862413 | 312816213 | 317862413 | 322816213  | 327862413 | 332816213  | 337862413 | 342816213 | 347862413 | 352816213 | 357862413 |
| 26 | 70 | 312816213 | 317862413 | 322816213 | 327862413  | 332816213 | 337862413  | 342816213 | 347862413 | 352816213 | 357862413 | 362816213 |
| 26 | 71 | 317862413 | 322816213 | 327862413 | 332816213  | 337862413 | 342816213  | 347862413 | 352816213 | 357862413 | 362816213 | 367862413 |
| 26 | 72 | 322816213 | 327862413 | 332816213 | 337862413  | 342816213 | 347862413  | 352816213 | 357862413 | 362816213 | 367862413 | 372816213 |
| 26 | 73 | 327862413 | 332816213 | 337862413 | 342816213  | 347862413 | 352816213  | 357862413 | 362816213 | 367862413 | 372816213 | 377862413 |
| 26 | 74 | 332816213 | 337862413 | 342816213 | 347862413  | 352816213 | 357862413  | 362816213 | 367862413 | 372816213 | 377862413 | 382816213 |
| 26 | 75 | 337862413 | 342816213 | 347862413 | 352816213  | 357862413 | 362816213  | 367862413 | 372816213 | 377862413 | 382816213 | 387862413 |
| 26 | 76 | 342816213 | 347862413 | 352816213 | 357862413  | 362816213 | 367862413  | 372816213 | 377862413 | 382816213 | 387862413 | 392816213 |
| 26 | 77 | 347862413 | 352816213 | 357862413 | 362816213  | 367862413 | 372816213  | 377862413 | 382816213 | 387862413 | 392816213 | 397862413 |
| 26 | 78 | 352816213 | 357862413 | 362816213 | 367862413  | 37281621  |            |           |           |           |           |           |

## PERCENTILE POINTS OF THF BETA DISTRIBUTION

| I  | .01        | .02*       | .05        | .10        | .25        | .50         | .75         | .90         | .95         | .975        | .99        |
|----|------------|------------|------------|------------|------------|-------------|-------------|-------------|-------------|-------------|------------|
| 1  | .00034660  | .00081265  | .00176717  | .00162653  | .00236103  | .002361818  | .004667867  | .007632914  | .009814463  | .1119444687 | .146832125 |
| 2  | .00019772  | .000846396 | .01230353  | .011849034 | .013317318 | .005720226  | .009107773  | .012761889  | .01539174   | .017764410  | .020787799 |
| 3  | .00145964  | .002185633 | .018707549 | .013861547 | .059860377 | .01145526   | .13075685   | .17226534   | .20156099   | .225616189  | .25963269  |
| 4  | .00262067  | .003884882 | .018857006 | .01616498  | .03817622  | .012518615  | .16981642   | .21306820   | .24611302   | .27751520   | .306627281 |
| 5  | .006345153 | .00799184  | .016845607 | .017049297 | .01753070  | .014764834  | .117453070  | .20787931   | .245686406  | .28887201   | .31646061  |
| 6  | .006646405 | .010233455 | .010161642 | .022696066 | .017850520 | .027350072  | .10321947   | .24520520   | .29610168   | .32887211   | .35203461  |
| 7  | .002125952 | .012711084 | .012711564 | .016746462 | .018250520 | .027350072  | .28194642   | .242946558  | .36799559   | .419726703  | .43172701  |
| 8  | .013171171 | .015281564 | .017245478 | .01977115  | .024118061 | .026154647  | .26119463   | .40721756   | .40566958   | .433400054  | .460848780 |
| 9  | .014650093 | .017032366 | .020642971 | .022611503 | .027227656 | .030078462  | .280466427  | .40423827   | .46423827   | .49032225   | .54221336  |
| 10 | .012110793 | .01681988  | .020681725 | .022909442 | .028781675 | .032826466  | .307174927  | .474616192  | .540730567  | .56730573   | .58730571  |
| 11 | .020613594 | .023522002 | .024845363 | .02644532  | .030921146 | .031971100  | .311971100  | .49389116   | .54559101   | .610625058  | .61011095  |
| 12 | .0236932   | .02644532  | .027421625 | .031971100 | .031971100 | .043182261  | .49389116   | .58255527   | .61563008   | .64257203   | .67408120  |
| 13 | .026553167 | .029445367 | .029445367 | .031971100 | .031971100 | .465615627  | .547817031  | .561247606  | .61563008   | .67408120   | .67408120  |
| 14 | .009336565 | .025251497 | .038459324 | .038459324 | .042817150 | .050000000  | .556184817  | .561340066  | .64709337   | .704669500  | .704669500 |
| 15 | .000336565 | .025251497 | .038459324 | .038459324 | .042817150 | .050000000  | .556184817  | .64709337   | .704669500  | .704669500  | .704669500 |
| 1  | .000303475 | .000814357 | .011718729 | .011780585 | .011780585 | .012028470  | .014515819  | .017981727  | .020513826  | .021503111  | .14221170  |
| 2  | .000303385 | .000814383 | .011975729 | .011888957 | .013206667 | .015531690  | .087255673  | .12156999   | .14859607   | .17216945   | .20169718  |
| 3  | .001493067 | .021117171 | .02181554  | .032730777 | .037545482 | .038446008  | .12651961   | .1481294    | .19532621   | .22075540   | .25189984  |
| 4  | .002845536 | .046845363 | .046845363 | .046845363 | .050621113 | .051216061  | .16420961   | .207991947  | .252978786  | .29741885   | .329741886 |
| 5  | .00472236  | .056642168 | .056642168 | .056642168 | .058326556 | .059365050  | .113565500  | .15396801   | .201222343  | .242122343  | .246026250 |
| 6  | .00614597  | .057711562 | .058745243 | .058745243 | .060355556 | .061565556  | .18696804   | .217295654  | .2427295654 | .28176463   | .313897118 |
| 7  | .002927724 | .039331785 | .011946901 | .013497473 | .017081659 | .0217081659 | .27197776   | .32179576   | .356168901  | .385656651  | .41719004  |
| 8  | .012356533 | .016197682 | .016197682 | .016197682 | .020741826 | .021140161  | .30116167   | .37114702   | .403393762  | .42728772   | .451577731 |
| 9  | .015017986 | .017424650 | .017424650 | .017424650 | .020505041 | .020574009  | .32084039   | .36584039   | .44992400   | .45498965   | .49265577  |
| 10 | .017556435 | .017876728 | .019340586 | .019842554 | .021842554 | .023844686  | .318212114  | .431899193  | .481686691  | .48650271   | .517446455 |
| 11 | .021296173 | .022156767 | .026570544 | .026570544 | .026750692 | .029506926  | .41123760   | .466281118  | .496943870  | .52812006   | .561182006 |
| 12 | .022760651 | .024567075 | .027666055 | .027666055 | .030760075 | .031061629  | .446497028  | .50112643   | .533016523  | .561140015  | .593164652 |
| 13 | .025513092 | .028161811 | .028464403 | .028464403 | .030861629 | .045615591  | .456155901  | .543623765  | .56606574   | .59275007   | .625767940 |
| 14 | .028306494 | .032979712 | .032979712 | .032979712 | .035696939 | .042818295  | .542818295  | .59551242   | .63001244   | .655744775  | .68684660  |
| 15 | .000287211 | .001072211 | .001464465 | .001620577 | .00818578  | .019609319  | .038834625  | .061667079  | .08203164   | .100032464  | .12328761  |
| 1  | .00029715  | .001529851 | .017248278 | .017460979 | .017509378 | .017509378  | .104955398  | .104955398  | .14996524   | .12854631   | .17583996  |
| 2  | .012747702 | .01803764  | .022730909 | .031517009 | .031517009 | .031517009  | .103914682  | .103914682  | .14991706   | .119517141  | .212914660 |
| 3  | .024240068 | .022031114 | .028992887 | .03078678  | .03078678  | .03078678   | .107296725  | .107296725  | .146160500  | .120880902  | .259444820 |
| 4  | .038000003 | .048460003 | .050000003 | .050000003 | .057115200 | .057115200  | .107174164  | .107174164  | .147448009  | .121552808  | .26737504  |
| 5  | .055626073 | .065562178 | .077330442 | .092600000 | .122000140 | .160046275  | .2047670627 | .24859529   | .27718664   | .30757135   | .332978791 |
| 6  | .07040263  | .084426082 | .091401765 | .091401765 | .091401765 | .091401765  | .10824877   | .1205650577 | .128122726  | .1305650577 | .136766328 |
| 7  | .088425600 | .104426082 | .11729546  | .11729546  | .11729546  | .11729546   | .17297546   | .217094946  | .26592705   | .3138657    | .343536269 |
| 8  | .12765539  | .12489306  | .14121665  | .161650114 | .19898166  | .245310078  | .2960120078 | .34466154   | .374770117  | .441363276  | .43275874  |
| 9  | .12737764  | .138535474 | .168546968 | .185583703 | .225786468 | .271626468  | .32581777   | .375300000  | .443555885  | .525767940  | .562767940 |
| 10 | .14815711  | .16851574  | .18192874  | .18192874  | .18192874  | .18192874   | .319191974  | .355395525  | .40556675   | .43625980   | .46104464  |
| 11 | .16958255  | .191324607 | .211192275 | .215337873 | .279461176 | .33021572   | .43471870   | .45464166   | .46614746   | .492288000  | .52378068  |
| 12 | .191752712 | .234702123 | .235507812 | .26060245  | .28670526  | .33282803   | .386809219  | .44272404   | .49332076   | .52440019   | .552167884 |
| 13 | .21675916  | .233705812 | .26060245  | .28670526  | .33282803  | .386809219  | .44272404   | .49332076   | .52440019   | .552167884  | .58108357  |

## PERCENTILE POINTS OF THE BFITA DISTRIBUTION

| N  | !           | .01         | .025        | .05         | .10         | .25         | .50         | .75         | .90          | .95         | .975        | .99          |
|----|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|--------------|-------------|-------------|--------------|
| 35 | 15          | .23803575   | .26222723   | .28584683   | .31292932   | .36023589   | .41510677   | .47142768   | .52246664    | .55282449   | .57688228   | .60871476    |
| 16 | 26210163    | .28821164   | .31165317   | .33550675   | .38793669   | .443260442  | .49994181   | .55075712   | .58079671    | .60646294   | .64571487   |              |
| 17 | .28676235   | .31329252   | .34789493   | .36663021   | .41561674   | .47170215   | .52827099   | .57810180   | .60382981    | .63254198   | .66245575   |              |
| 18 | .31201073   | .33989138   | .36456192   | .39160451   | .44354213   | .50000000   | .556641787  | .60630548   | .63243204    | .667994577  |             |              |
| 48 | 1           | .60025123   | .88865374   | .88120151   | .80262654   | .807176674  | .807176674  | .807176674  | .805503912   | .8080730    | .84806730   | .10872906    |
| 2  | .60075613   | .88611264   | .88956746   | .88374651   | .88224653   | .88160484   | .88160484   | .8805912    | .88379710    | .88118836   | .88115886   | .1547307     |
| 3  | .60112106   | .88156217   | .88075646   | .88297022   | .88224653   | .88160484   | .88160484   | .8805912    | .88379710    | .88118836   | .88115886   |              |
| 4  | .601211636  | .88725539   | .88488464   | .88432181   | .88437024   | .88313441   | .88243230   | .881544931  | .8858585     | .88386475   | .882990680  |              |
| 5  | .603212785  | .88485563   | .88570533   | .88206813   | .88491965   | .881570856  | .88126032   | .88098154   | .88433754    | .882663376  | .882161365  |              |
| 6  | .604655134  | .88711225   | .88764225   | .88673178   | .88673178   | .88658120   | .88657227   | .88790284   | .887145910   | .88680292   | .88577844   |              |
| 7  | .606114840  | .88748774   | .88511257   | .88611197   | .882863894  | .881535240  | .882076417  | .88284513   | .8874451     | .88845267   | .8872627    |              |
| 8  | .607772483  | .880052247  | .880052247  | .880052247  | .880052247  | .880052247  | .880052247  | .880052247  | .882776582   | .882776582  | .882776582  |              |
| 9  | .609214266  | .88028056   | .88277154   | .88168512   | .88172522   | .881492706  | .881492706  | .881492706  | .882776582   | .882776582  | .882776582  |              |
| 10 | .610931065  | .882691677  | .882691677  | .882691677  | .882691677  | .882691677  | .882691677  | .882691677  | .88297023    | .88297023   | .88297023   |              |
| 11 | .62812376   | .88620897   | .88620897   | .88620897   | .88620897   | .88620897   | .88620897   | .88620897   | .88378782    | .88378782   | .88378782   |              |
| 12 | .646655229  | .88622797   | .88622797   | .88622797   | .88622797   | .88622797   | .88622797   | .88622797   | .88378782    | .88378782   | .88378782   |              |
| 13 | .646646405  | .8857895    | .8857895    | .88511438   | .885650337  | .885650337  | .885650337  | .885650337  | .884115008   | .884115008  | .884115008  |              |
| 14 | .685056264  | .880282847  | .880282847  | .880282847  | .880282847  | .880282847  | .880282847  | .880282847  | .88378782    | .88378782   | .88378782   |              |
| 15 | .620505988  | .88226277   | .88226277   | .88226277   | .88226277   | .88226277   | .88226277   | .88226277   | .88378782    | .88378782   | .88378782   |              |
| 16 | .622554016  | .884864006  | .88604675   | .88611187   | .88654240   | .887070726  | .887070726  | .887070726  | .88378782    | .88378782   | .88378782   |              |
| 17 | .624667845  | .870162703  | .881846462  | .883779367  | .883779367  | .883779367  | .883779367  | .883779367  | .883779367   | .883779367  | .883779367  |              |
| 18 | .626785413  | .882048874  | .883661115  | .883677950  | .883685404  | .883685404  | .883685404  | .883685404  | .883779367   | .883779367  | .883779367  |              |
| 19 | .628666427  | .881511077  | .882769417  | .884661405  | .884103056  | .884103056  | .884103056  | .884103056  | .883779367   | .883779367  | .883779367  |              |
| 20 | .63190356   | .8830101778 | .8836101056 | .883820609  | .883820609  | .883820609  | .883820609  | .883820609  | .883779367   | .883779367  | .883779367  |              |
| 21 |             |             |             |             |             |             |             |             |              |             |             |              |
| 45 | 1           | .60022332   | .880056246  | .880113220  | .88012226   | .880167224  | .880167224  | .880167224  | .88064406220 | .880780510  | .880780510  | .880780510   |
| 2  | .60333206   | .8800422848 | .880705619  | .881190056  | .881213718  | .8813701586 | .8813701586 | .8813701586 | .88064406220 | .880780510  | .880780510  | .880780510   |
| 3  | .603936376  | .881196510  | .881184185  | .881474124  | .881474124  | .881474124  | .881474124  | .881474124  | .880780510   | .880780510  | .880780510  | .880780510   |
| 4  | .601875444  | .880122205  | .880122205  | .880122205  | .880122205  | .8805664647 | .880890430  | .8811889203 | .8812475764  | .8812475764 | .8812475764 | .8812475764  |
| 5  | .6079332754 | .88307665   | .882468116  | .880506216  | .8817561085 | .8813092760 | .8813092760 | .8813092760 | .8819083631  | .8819083631 | .8819083631 | .8819083631  |
| 6  | .604117752  | .88456278   | .88456278   | .88456278   | .88456278   | .8819083631 | .8819083631 | .8819083631 | .8819083631  | .8819083631 | .8819083631 | .8819083631  |
| 7  | .606417728  | .886460118  | .88654574   | .886870560  | .886870560  | .8811617034 | .8814711646 | .8818476411 | .8826722620  | .8826722620 | .8826722620 | .8826722620  |
| 8  | .606776320  | .880801796  | .88165582   | .88165582   | .88165582   | .8813601351 | .8816916652 | .8820871906 | .8826721665  | .8826721665 | .8826721665 | .8826721665  |
| 9  | .608200210  | .880555721  | .880555721  | .880555721  | .880555721  | .8815401817 | .8815401817 | .8815401817 | .882121703   | .882121703  | .882121703  | .882121703   |
| 10 | .609727327  | .881120456  | .881281456  | .881281456  | .881281456  | .881743117  | .8821327009 | .8825620743 | .8829728574  | .8832061650 | .8832061650 | .8832061650  |
| 11 | .612900804  | .881282282  | .881455192  | .881671431  | .8819419952 | .8823532560 | .8827027666 | .8827027666 | .8827027666  | .8827027666 | .8827027666 | .8827027666  |
| 12 | .612900805  | .881464072  | .881666215  | .881800093  | .882143718  | .882450815  | .8827573797 | .8830558254 | .883455194   | .8837201642 | .8837201642 | .8837201642  |
| 13 | .614666623  | .881666255  | .881800093  | .8818111724 | .882001780  | .8823616313 | .8827043490 | .8832664490 | .8836021367  | .883905856  | .8841052367 | .8841052367  |
| 14 | .616271306  | .881865377  | .8819889155 | .8821979715 | .882505332  | .8830149006 | .8834685763 | .8839265290 | .8841957854  | .8844314528 | .8847068574 | .8847068574  |
| 15 | .618016913  | .882000575  | .882179664  | .882179664  | .882179664  | .8824452448 | .8827656777 | .8831746456 | .8834508745  | .8837097151 | .884064103  | .8843977213  |
| 16 | .618700692  | .8821684602 | .8823731949 | .882992727  | .882992727  | .882992727  | .882992727  | .882992727  | .8834844155  | .8836597747 | .8839867659 | .88415967659 |
| 17 | .621621823  | .8824176782 | .8825696011 | .8828002611 | .8832002611 | .8832002611 | .8832002611 | .8832002611 | .884162766   | .884462766  | .884710890  | .8851210890  |
| 18 | .624678006  | .8825677587 | .8827612423 | .883151098  | .883412047  | .883712174  | .8840898927 | .884481597  | .884881597   | .8851549863 |             |              |
| 19 | .625368395  | .8827656703 | .8829695612 | .8832120513 | .8836321513 | .8839212513 | .8841775257 | .8846144594 | .885065694   | .885337645  | .8856635645 | .8858136764  |
| 20 | .627922105  | .8829644393 | .8831732880 | .8834209643 | .8838488012 | .8841382926 | .8848370058 | .8852872433 | .8855694354  | .885784572  | .886089045  | .8862505670  |
| 21 | .629468475  | .8831660082 | .8834394473 | .883730174  | .8840650114 | .8845588620 | .885055532  | .8855071341 | .8857727207  | .8860026565 | .8862505670 |              |

TABLE I Contd.

## PERCENTILE POINTS OF THE RTIA DISTRIBUTION

| N  | 1          | .01         | .025        | .05        | .10        | .25        | .50        | .75        | .90         | .95         | .975       | .99        |
|----|------------|-------------|-------------|------------|------------|------------|------------|------------|-------------|-------------|------------|------------|
| 45 | 22         | .31237053   | .33703374   | .25879256  | .38442120  | .42826871  | .47794312  | .52791148  | .57251850   | .59881620   | .62127799  | .64660033  |
| 55 | 24         | .32575776   | .35714036   | .2798722K  | .40501300  | .45013000  | .50000000  | .54987007  | .59413977   | .62012774   | .64225961  | .66742427  |
| 55 | 1          | .00020099   | .00006623   | .00102534  | .00210498  | .00573712  | .01376730  | .02740505  | .04500741   | .07501550   | .07112174  | .073498016 |
| 2  | .007294676 | .00481443   | .00715637   | .010248678 | .01655185  | .02276395  | .03312227  | .05202486  | .07505806   | .10546955   | .12562372  | .12646955  |
| 3  | .00886076  | .01264857   | .01655185   | .02276395  | .03466410  | .05312227  | .07691227  | .09295921  | .11261416   | .12712762   | .1576675   | .1576675   |
| 4  | .01683612  | .02227795   | .0278766    | .04526761  | .06595170  | .07264975  | .09006663  | .12875550  | .1483718    | .16548195   | .1870026   | .1870026   |
| 5  | .02640978  | .04374567   | .06462367   | .07817462  | .09507809  | .112646642 | .146487619 | .15356815  | .17791116   | .19224279   | .21692002  | .21692002  |
| 6  | .02640978  | .04526761   | .06595170   | .07264975  | .09507809  | .112646642 | .146487619 | .15356815  | .17791116   | .19224279   | .21692002  | .21692002  |
| 7  | .04962528  | .06819167   | .06750667   | .0782977   | .102464657 | .12505321  | .16675318  | .17113095  | .22169660   | .24157264   | .24157264  | .24157264  |
| 8  | .06197862  | .07116075   | .08246490   | .10818566  | .12046490  | .142616269 | .180241801 | .20241922  | .26473626   | .267195785  | .267195785 | .267195785 |
| 9  | .07355553  | .08562008   | .097264609  | .11664653  | .129896    | .136       | .14222320  | .15000105  | .24648746   | .26730626   | .27195785  | .27195785  |
| 10 | .08707395  | .10050222   | .11272157   | .12171715  | .156654506 | .16208442  | .18021201  | .20241922  | .27222004   | .29172727   | .31135441  | .31135441  |
| 11 | .11593153  | .115654506  | .12171715   | .12846746  | .14648746  | .16208442  | .17492727  | .20241922  | .27222004   | .29172727   | .31135441  | .31135441  |
| 12 | .115279062 | .13016992   | .14471814   | .162066952 | .193666070 | .2118140   | .22656647  | .241310705 | .27277242   | .30576186   | .34542528  | .34542528  |
| 13 | .13055972  | .14660054   | .1617455    | .1735170   | .21088704  | .25167817  | .27274840  | .29468584  | .32576570   | .34916705   | .38765440  | .38765440  |
| 14 | .14621077  | .162110462  | .17706821   | .195046021 | .21301071  | .27156301  | .311751    | .35666278  | .38126355   | .4030346769 | .42950772  | .42950772  |
| 15 | .16069748  | .17661784   | .19488486   | .21458666  | .24006945  | .29146816  | .32568076  | .36568076  | .40241759   | .44240654   | .46101142  | .46101142  |
| 16 | .17655914  | .19536416   | .21216101   | .23240110  | .24245617  | .31127248  | .35242759  | .39817450  | .42237293   | .46402323   | .47218688  | .47218688  |
| 17 | .19262861  | .21254667   | .22954730   | .24726591  | .26488201  | .30520692  | .35113906  | .39761273  | .441897138  | .4845662330 | .516559786 | .516559786 |
| 18 | .20904163  | .22915705   | .24726591   | .26488201  | .30520692  | .35113906  | .39761273  | .441897138 | .4845662330 | .516559786  | .516559786 | .516559786 |
| 19 | .22573661  | .24656106   | .26556106   | .28727348  | .32505772  | .37087058  | .41179452  | .46495975  | .50576015   | .54030686   | .57190782  | .57190782  |
| 20 | .242707390 | .26447840   | .28447840   | .316512059 | .34651900  | .39073660  | .43799427  | .49033096  | .550606075  | .58232508   | .61192020  | .61192020  |
| 21 | .25993566  | .28188724   | .30138638   | .3245254   | .36456557  | .41606816  | .4557257   | .50257257  | .54211075   | .57256537   | .61766726  | .61766726  |
| 22 | .27747581  | .29909723   | .3118291    | .343019251 | .38309384  | .43036855  | .47777380  | .51536392  | .56610185   | .61709554   | .65315500  | .65315500  |
| 23 | .29516944  | .31814918   | .33846156   | .373651872 | .40302347  | .45026707  | .501030560 | .556571753 | .587655550  | .617738857  | .641737187 | .641737187 |
| 24 | .31316315  | .33665609   | .35722876   | .381562556 | .4221157   | .47020166  | .51764427  | .560112196 | .60456902   | .640512700  | .684469705 | .684469705 |
| 25 | .31316315  | .33665609   | .35722876   | .381562556 | .4221157   | .47020166  | .51764427  | .560112196 | .60456902   | .640512700  | .684469705 | .684469705 |
| 55 | 1          | .000118272  | .000466022  | .00093217  | .00191191  | .005521697 | .01254255  | .02489035  | .04116094   | .05501105   | .064687076 | .080932096 |
| 2  | .00077218  | .0004649454 | .0006464948 | .000971102 | .017184466 | .030332797 | .04820926  | .06880505  | .08337134   | .09710102   | .114650324 | .114650324 |
| 3  | .01801341  | .01130301   | .01500330   | .020270466 | .03485257  | .069322257 | .09004255  | .09388382  | .11017945   | .1252662    | .1442105   | .1442105   |
| 4  | .01527288  | .02017053   | .02522227   | .036209575 | .046209571 | .06161397  | .08446094  | .11401074  | .14010745   | .15876742   | .17178857  | .17178857  |
| 5  | .02484545  | .03018085   | .036571715  | .044488248 | .061613975 | .084460944 | .11401074  | .14010745  | .15876742   | .17178857   | .17178857  | .17178857  |
| 6  | .03245557  | .04110151   | .04858184   | .058312956 | .07278432  | .102466816 | .13197849  | .161211817 | .18168989   | .19251962   | .2225042   | .2225042   |
| 7  | .043381235 | .05273516   | .06128657   | .07223972  | .09305371  | .12050371  | .15196957  | .18161071  | .201999948  | .2274091091 | .2448136   | .2448136   |
| 8  | .05449664  | .06495139   | .07424880   | .08656780  | .10936532  | .13856532  | .17174561  | .207673947 | .24480272   | .26767925   | .26767925  | .26767925  |
| 9  | .06653735  | .07765882   | .08811126   | .10102321  | .12577642  | .155666255 | .19136250  | .22551098  | .262717555  | .285551327  | .32895946  | .32895946  |
| 10 | .07865917  | .08079047   | .10208181   | .11618560  | .1422312   | .17423108  | .207856    | .2459474   | .268194212  | .28804000   | .31177631  | .31177631  |
| 11 | .091257115 | .10429548   | .11670455   | .13130148  | .15885156  | .18130148  | .20706505  | .220030319 | .246227385  | .28886455   | .309064851 | .31307074  |
| 12 | .10420242  | .11813575   | .13099648   | .14682394  | .175651021 | .212081772 | .24928127  | .285622658 | .309223356  | .322727851  | .35400918  | .35400918  |
| 13 | .11749712  | .13227809   | .14584672   | .16546609  | .192947401 | .22894716  | .25160254  | .28140992  | .31601021   | .34294092   | .37458992  | .37458992  |
| 14 | .13112043  | .14670044   | .16094694   | .17828520  | .20947700  | .24700717  | .28133903  | .32556505  | .349290930  | .372195018  | .39486261  | .39486261  |
| 15 | .14504111  | .16137954   | .17522191   | .19428257  | .22646040  | .2550775   | .28622592  | .314507229 | .35897792   | .39078244   | .41470770  | .41470770  |
| 16 | .15922277  | .17629066   | .19146157   | .20436172  | .23637700  | .26437749  | .29436172  | .325436705 | .364361728  | .407077307  | .444545772 | .444545772 |
| 17 | .17370185  | .19144637   | .20755834   | .22675262  | .25658605  | .30121281  | .330746694 | .363074669 | .407077307  | .444545772  | .444545772 | .444545772 |
| 18 | .18864423  | .20680812   | .223346455  | .24332075  | .278161190 | .31928902  | .352230750 | .392455076 | .426682744  | .444862975  | .444862975 | .444862975 |

TABLE I Contd.

## PERCENTILE POINTS OF THE RETA DISTRIBUTION

| N  | 1          | .01        | .025       | .05        | .10        | .25        | .50        | .75        | .90        | .95        | .975       | .99        |
|----|------------|------------|------------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 55 | 19         | .20338001  | .222237485 | .230460691 | .25979961  | .29553550  | .33735967  | .38096110  | .42129100  | .44574965  | .46707104  | .47190750  |
| 20 | .2185560   | .23813885  | .25637935  | .26545078  | .27024685  | .29337554  | .30690595  | .373501738 | .41205176  | .44003657  | .466505454 | .51068168  |
| 21 | .22397293  | .25637915  | .27024685  | .27022887  | .28857012  | .31036675  | .36876751  | .39157580  | .42676227  | .45858162  | .48309814  | .50436854  |
| 22 | .24659536  | .27022887  | .28857012  | .28857012  | .32744347  | .36578704  | .40166207  | .44657526  | .47704849  | .50151547  | .52277774  | .54726826  |
| 23 | .26562776  | .2864525   | .30154097  | .32744347  | .36578704  | .40166207  | .44657526  | .49553085  | .53092764  | .56529237  | .58311299  | .60568164  |
| 24 | .281466424 | .30154097  | .32744347  | .32744347  | .36465825  | .38151068  | .4272113   | .47286097  | .5136429   | .54582160  | .576374752 | .60773052  |
| 25 | .29779266  | .311707068 | .32910566  | .32910566  | .361107068 | .36117626  | .40167262  | .44657526  | .49553085  | .53092764  | .56529237  | .58311299  |
| 26 | .31413087  | .32613033  | .34424162  | .34424162  | .37061360  | .41010802  | .45428754  | .49553085  | .53092764  | .56529237  | .59641661  | .6181470   |
| 27 | .320761684 | .32359867  | .34732027  | .34732027  | .37061360  | .41010802  | .45428754  | .49553085  | .53092764  | .56529237  | .59641661  | .6181470   |
| 28 | .347361683 | .32707858  | .36090646  | .36090646  | .37061360  | .41010802  | .45428754  | .49553085  | .53092764  | .56529237  | .59641661  | .6181470   |
| 66 | 1          | .00016740  | .000167187 | .000167187 | .000167187 | .000167187 | .000167187 | .000167187 | .000167187 | .000167187 | .000167187 | .000167187 |
| 2  | .00026060  | .000167262 | .000167262 | .000167262 | .000167262 | .000167262 | .000167262 | .000167262 | .000167262 | .000167262 | .000167262 | .000167262 |
| 3  | .00074617  | .01174617  | .01174617  | .01174617  | .01174617  | .01174617  | .01174617  | .01174617  | .01174617  | .01174617  | .01174617  | .01174617  |
| 4  | .01207702  | .011646176 | .011646176 | .011646176 | .011646176 | .011646176 | .011646176 | .011646176 | .011646176 | .011646176 | .011646176 | .011646176 |
| 5  | .02181903  | .02165221  | .02165221  | .02165221  | .02165221  | .02165221  | .02165221  | .02165221  | .02165221  | .02165221  | .02165221  | .02165221  |
| 6  | .03338494  | .032790126 | .03464095  | .03464095  | .03464095  | .03464095  | .03464095  | .03464095  | .03464095  | .03464095  | .03464095  | .03464095  |
| 7  | .05008781  | .048211696 | .05008781  | .05008781  | .05008781  | .05008781  | .05008781  | .05008781  | .05008781  | .05008781  | .05008781  | .05008781  |
| 8  | .06511985  | .064036139 | .064036139 | .064036139 | .064036139 | .064036139 | .064036139 | .064036139 | .064036139 | .064036139 | .064036139 | .064036139 |
| 9  | .07070667  | .070086640 | .070086640 | .070086640 | .070086640 | .070086640 | .070086640 | .070086640 | .070086640 | .070086640 | .070086640 | .070086640 |
| 10 | .07184608  | .082707882 | .093139692 | .093139692 | .10625271  | .12327772  | .14029207  | .16029207  | .18029207  | .20029207  | .22029207  | .24029207  |
| 11 | .0832218   | .09525682  | .09525682  | .09525682  | .12013222  | .146464222 | .176821672 | .211510172 | .251510172 | .291510172 | .331510172 | .371510172 |
| 12 | .09508803  | .107811678 | .11161321  | .11161321  | .13138778  | .14648234  | .161646483 | .176821672 | .19029121  | .211510172 | .231510172 | .251510172 |
| 13 | .10774087  | .12071160  | .12071160  | .12071160  | .13138778  | .14648234  | .161646483 | .176821672 | .19029121  | .211510172 | .231510172 | .251510172 |
| 14 | .11952234  | .12081274  | .12081274  | .12081274  | .134602237 | .14648234  | .161646483 | .176821672 | .19029121  | .211510172 | .231510172 | .251510172 |
| 15 | .13211656  | .147186015 | .147186015 | .147186015 | .161716645 | .177198464 | .192272067 | .207198464 | .222198464 | .237198464 | .252198464 | .267198464 |
| 16 | .14505666  | .161716644 | .161716644 | .161716644 | .174671644 | .189628298 | .20709298  | .226868298 | .246480298 | .266256677 | .286053677 | .30603930  |
| 17 | .158878    | .17465526  | .17465526  | .17465526  | .189628298 | .20709298  | .226868298 | .246480298 | .266256677 | .286053677 | .30603930  | .32603930  |
| 18 | .171121164 | .18945145  | .18945145  | .18945145  | .20709298  | .226868298 | .246480298 | .266256677 | .286053677 | .30603930  | .32603930  | .34603930  |
| 19 | .18505802  | .202575667 | .202575667 | .202575667 | .218575667 | .23711602  | .25711602  | .27711602  | .29711602  | .31711602  | .33711602  | .35711602  |
| 20 | .1984548   | .21686046  | .21686046  | .21686046  | .232227701 | .25228567  | .27228567  | .29228567  | .31228567  | .33228567  | .35228567  | .37228567  |
| 21 | .2171616   | .23137663  | .23137663  | .23137663  | .247186015 | .26722248  | .28714062  | .31811073  | .359121264 | .39124382  | .42129100  | .44574965  |
| 22 | .22653876  | .24594062  | .24594062  | .24594062  | .26722248  | .28714062  | .31811073  | .359121264 | .39124382  | .42129100  | .44574965  | .47190750  |
| 23 | .241118616 | .26070176  | .26070176  | .26070176  | .278056018 | .29867210  | .33450588  | .375669706 | .41823420  | .457191940 | .50101072  | .542666607 |
| 24 | .255565968 | .27572113  | .27572113  | .27572113  | .314610212 | .354505846 | .392276172 | .434505846 | .47111657  | .51125663  | .55790262  | .59790262  |
| 25 | .270302664 | .29058005  | .29058005  | .29058005  | .32711337  | .330120820 | .36675240  | .409866477 | .451869795 | .49303930  | .531635567 | .573450555 |
| 26 | .28511153  | .3058143   | .3058143   | .3058143   | .324212707 | .34584957  | .383010163 | .425611795 | .465618260 | .50766970  | .54101425  | .587460165 |
| 27 | .300011364 | .321217152 | .321217152 | .321217152 | .34394254  | .36176332  | .39129977  | .441199112 | .484301655 | .524305935 | .56745035  | .607646915 |
| 28 | .315216858 | .336699008 | .336699008 | .336699008 | .355681359 | .37776852  | .416466480 | .458565317 | .50189973  | .54082229  | .587178849 | .621380985 |
| 29 | .33054972  | .34231293  | .34231293  | .34231293  | .37144001  | .39386435  | .43261198  | .475133916 | .51848575  | .557303879 | .593030440 | .630005110 |
| 30 | .345959114 | .36806198  | .36806198  | .36806198  | .40105016  | .448848499 | .49171111  | .53502431  | .57367415  | .595650383 | .616505198 | .64842932  |

PERCENTILE POINTS OF THE RTFA DISTRIBUTION

| $n$ | 1  | .25         | .50         | .75         | N           | 1  | .25 | .50        | .75         |
|-----|----|-------------|-------------|-------------|-------------|----|-----|------------|-------------|
| 64  | 1  | .0104416708 | .0110500713 | .012116178  | .012116178  | 76 | 1   | .010410131 | .010985124  |
|     | 2  | .0114703667 | .0125485645 | .013088918  | .013088918  |    | 2   | .011735557 | .0119500198 |
|     | 3  | .012664117  | .013692619  | .014592606  | .014592606  |    | 3   | .012375004 | .0123401751 |
|     | 4  | .013914872  | .015620215  | .017334662  | .017334662  |    | 4   | .013642257 | .015220606  |
|     | 5  | .015208463  | .017143069  | .019684177  | .019684177  |    | 5   | .014147116 | .018817098  |
|     | 6  | .016521645  | .019679560  | .021906210  | .021906210  |    | 6   | .015640847 | .019816157  |
|     | 7  | .017872744  | .021098292  | .023904556  | .023904556  |    | 7   | .0161248   | .019002017  |
|     | 8  | .019246781  | .021738207  | .024592222  | .024592222  |    | 8   | .016875261 | .0190609851 |
|     | 9  | .02161062   | .024264109  | .027457210  | .027457210  |    | 9   | .017501538 | .019205217  |
|     | 10 | .0241062    | .027179567  | .030176787  | .030176787  |    | 10  | .018162682 | .019706660  |
|     | 11 | .02411907   | .027378014  | .030557758  | .030557758  |    | 11  | .01842250  | .019102762  |
|     | 12 | .02487684   | .0317469215 | .034719721  | .034719721  |    | 12  | .018489782 | .019714648  |
|     | 13 | .027467664  | .0320280630 | .032911856  | .032911856  |    | 13  | .0186695   | .021220861  |
|     | 14 | .02872720   | .0320020127 | .032635982  | .032635982  |    | 14  | .01892558  | .02273406   |
|     | 15 | .031461626  | .032265208  | .033194538  | .033194538  |    | 15  | .01923651  | .024724628  |
|     | 16 | .03424626   | .0329811036 | .0327667230 | .0327667230 |    | 16  | .01959621  | .025731271  |
|     | 17 | .037029162  | .035171517  | .032950600  | .032950600  |    | 17  | .02001812  | .027220251  |
|     | 18 | .03948568   | .037192721  | .037192721  | .037192721  |    | 18  | .021519841 | .02870307   |
|     | 19 | .04031081   | .038672601  | .037670727  | .037670727  |    | 19  | .021018116 | .03018298   |
|     | 20 | .04237000   | .039112004  | .038611650  | .038611650  |    | 20  | .024640562 | .027082068  |
|     | 21 | .04524915   | .041432615  | .040484850  | .040484850  |    | 21  | .02930768  | .030326764  |
|     | 22 | .04926437   | .043186535  | .041593222  | .041593222  |    | 22  | .027986709 | .030866494  |
|     | 23 | .05235274   | .046206446  | .047725016  | .047725016  |    | 23  | .029466948 | .032298210  |
|     | 24 | .05709033   | .05272516   | .047287300  | .047287300  |    | 24  | .032361946 | .035509409  |
|     | 25 | .05770517   | .057755447  | .041966165  | .041966165  |    | 25  | .03109117  | .038067157  |
|     | 26 | .059729462  | .059298152  | .042209807  | .042209807  |    | 26  | .02209837  | .026402111  |
|     | 27 | .062197114  | .048167745  | .046948850  | .046948850  |    | 27  | .03476230  | .0418580    |
|     | 28 | .062776997  | .062746726  | .066692300  | .066692300  |    | 28  | .03645171  | .04227115   |
|     | 29 | .06777797   | .062877770  | .068092651  | .068092651  |    | 29  | .024557408 | .040738617  |
|     | 30 | .0728750    | .064569456  | .064571722  | .064571722  |    | 30  | .042180348 | .042180348  |
|     | 31 | .07801174   | .066975006  | .051106076  | .051106076  |    | 31  | .03952677  | .043662170  |
|     | 32 | .082318746  | .068469052  | .052624620  | .052624620  |    | 32  | .041055227 | .04507287   |
|     | 33 | .08646282   | .069605073  | .051150721  | .051150721  |    | 33  | .042761070 | .051846705  |
|     |    |             |             |             |             |    |     |            | .047867365  |
|     |    |             |             |             |             |    |     |            | .049280175  |
|     |    |             |             |             |             |    |     |            | .053301174  |

TABLE I Contd.

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TABLE 1 Contd.

## PERCENTILE POINTS OF THE RETA DISTRIBUTION

| n   | 1  | .25        | .50         | .75        | 9          | 1  | .25        | .50        | .75        | 9          | 1  | .25        | .50        | .75        | 9          |
|-----|----|------------|-------------|------------|------------|----|------------|------------|------------|------------|----|------------|------------|------------|------------|
| 75  | 1  | .010482661 | .0104915929 | .01081414  | .010862691 | 1  | .010458955 | .010862691 | .011717940 | .011717940 | 2  | .012011924 | .012011924 | .013301360 | .013301360 |
| 76  | 2  | .010482664 | .022727278  | .010500888 | .010500888 | 2  | .012011924 | .012011924 | .013301360 | .013301360 | 3  | .01262880  | .01262880  | .014819112 | .014819112 |
| 77  | 3  | .010482664 | .010491594  | .010500888 | .010500888 | 3  | .01262880  | .01262880  | .014819112 | .014819112 | 4  | .01670868  | .01670868  | .016322774 | .016322774 |
| 78  | 4  | .010482667 | .010491597  | .01081414  | .01081414  | 4  | .01670868  | .01670868  | .016322774 | .016322774 | 5  | .01686210  | .01686210  | .01771160  | .01771160  |
| 79  | 5  | .010482667 | .010491597  | .01081414  | .01081414  | 5  | .01686210  | .01686210  | .01771160  | .01771160  | 6  | .017327952 | .017327952 | .017327952 | .017327952 |
| 80  | 6  | .010482667 | .010491597  | .01081414  | .01081414  | 6  | .017327952 | .017327952 | .017327952 | .017327952 | 7  | .017327952 | .017327952 | .017327952 | .017327952 |
| 81  | 7  | .010482667 | .010491597  | .01081414  | .01081414  | 7  | .017327952 | .017327952 | .017327952 | .017327952 | 8  | .01786256  | .01786256  | .01857264  | .01857264  |
| 82  | 8  | .010482667 | .010491597  | .01081414  | .01081414  | 8  | .01786256  | .01786256  | .01857264  | .01857264  | 9  | .01857264  | .01857264  | .01901258  | .01901258  |
| 83  | 9  | .010482667 | .010491597  | .01081414  | .01081414  | 9  | .01857264  | .01857264  | .01901258  | .01901258  | 10 | .01861907  | .01861907  | .01924686  | .01924686  |
| 84  | 10 | .010482667 | .010491597  | .01081414  | .01081414  | 10 | .01861907  | .01861907  | .01924686  | .01924686  | 11 | .018728211 | .018728211 | .01968247  | .01968247  |
| 85  | 11 | .010482667 | .010491597  | .01081414  | .01081414  | 11 | .018728211 | .018728211 | .01968247  | .01968247  | 12 | .018728211 | .018728211 | .01968247  | .01968247  |
| 86  | 12 | .010482667 | .010491597  | .01081414  | .01081414  | 12 | .018728211 | .018728211 | .01968247  | .01968247  | 13 | .018728211 | .018728211 | .01968247  | .01968247  |
| 87  | 13 | .010482667 | .010491597  | .01081414  | .01081414  | 13 | .018728211 | .018728211 | .01968247  | .01968247  | 14 | .018728211 | .018728211 | .01968247  | .01968247  |
| 88  | 14 | .010482667 | .010491597  | .01081414  | .01081414  | 14 | .018728211 | .018728211 | .01968247  | .01968247  | 15 | .018728211 | .018728211 | .01968247  | .01968247  |
| 89  | 15 | .010482667 | .010491597  | .01081414  | .01081414  | 15 | .018728211 | .018728211 | .01968247  | .01968247  | 16 | .018728211 | .018728211 | .01968247  | .01968247  |
| 90  | 16 | .010482667 | .010491597  | .01081414  | .01081414  | 16 | .018728211 | .018728211 | .01968247  | .01968247  | 17 | .018728211 | .018728211 | .01968247  | .01968247  |
| 91  | 17 | .010482667 | .010491597  | .01081414  | .01081414  | 17 | .018728211 | .018728211 | .01968247  | .01968247  | 18 | .018728211 | .018728211 | .01968247  | .01968247  |
| 92  | 18 | .010482667 | .010491597  | .01081414  | .01081414  | 18 | .018728211 | .018728211 | .01968247  | .01968247  | 19 | .018728211 | .018728211 | .01968247  | .01968247  |
| 93  | 19 | .010482667 | .010491597  | .01081414  | .01081414  | 19 | .018728211 | .018728211 | .01968247  | .01968247  | 20 | .018728211 | .018728211 | .01968247  | .01968247  |
| 94  | 20 | .010482667 | .010491597  | .01081414  | .01081414  | 20 | .018728211 | .018728211 | .01968247  | .01968247  | 21 | .018728211 | .018728211 | .01968247  | .01968247  |
| 95  | 21 | .010482667 | .010491597  | .01081414  | .01081414  | 21 | .018728211 | .018728211 | .01968247  | .01968247  | 22 | .018728211 | .018728211 | .01968247  | .01968247  |
| 96  | 22 | .010482667 | .010491597  | .01081414  | .01081414  | 22 | .018728211 | .018728211 | .01968247  | .01968247  | 23 | .018728211 | .018728211 | .01968247  | .01968247  |
| 97  | 23 | .010482667 | .010491597  | .01081414  | .01081414  | 23 | .018728211 | .018728211 | .01968247  | .01968247  | 24 | .018728211 | .018728211 | .01968247  | .01968247  |
| 98  | 24 | .010482667 | .010491597  | .01081414  | .01081414  | 24 | .018728211 | .018728211 | .01968247  | .01968247  | 25 | .018728211 | .018728211 | .01968247  | .01968247  |
| 99  | 25 | .010482667 | .010491597  | .01081414  | .01081414  | 25 | .018728211 | .018728211 | .01968247  | .01968247  | 26 | .018728211 | .018728211 | .01968247  | .01968247  |
| 100 | 26 | .010482667 | .010491597  | .01081414  | .01081414  | 26 | .018728211 | .018728211 | .01968247  | .01968247  | 27 | .018728211 | .018728211 | .01968247  | .01968247  |
| 101 | 27 | .010482667 | .010491597  | .01081414  | .01081414  | 27 | .018728211 | .018728211 | .01968247  | .01968247  | 28 | .018728211 | .018728211 | .01968247  | .01968247  |
| 102 | 28 | .010482667 | .010491597  | .01081414  | .01081414  | 28 | .018728211 | .018728211 | .01968247  | .01968247  | 29 | .018728211 | .018728211 | .01968247  | .01968247  |
| 103 | 29 | .010482667 | .010491597  | .01081414  | .01081414  | 29 | .018728211 | .018728211 | .01968247  | .01968247  | 30 | .018728211 | .018728211 | .01968247  | .01968247  |
| 104 | 30 | .010482667 | .010491597  | .01081414  | .01081414  | 30 | .018728211 | .018728211 | .01968247  | .01968247  | 31 | .018728211 | .018728211 | .01968247  | .01968247  |
| 105 | 31 | .010482667 | .010491597  | .01081414  | .01081414  | 31 | .018728211 | .018728211 | .01968247  | .01968247  | 32 | .018728211 | .018728211 | .01968247  | .01968247  |
| 106 | 32 | .010482667 | .010491597  | .01081414  | .01081414  | 32 | .018728211 | .018728211 | .01968247  | .01968247  | 33 | .018728211 | .018728211 | .01968247  | .01968247  |
| 107 | 33 | .010482667 | .010491597  | .01081414  | .01081414  | 33 | .018728211 | .018728211 | .01968247  | .01968247  | 34 | .018728211 | .018728211 | .01968247  | .01968247  |
| 108 | 34 | .010482667 | .010491597  | .01081414  | .01081414  | 34 | .018728211 | .018728211 | .01968247  | .01968247  | 35 | .018728211 | .018728211 | .01968247  | .01968247  |
| 109 | 35 | .010482667 | .010491597  | .01081414  | .01081414  | 35 | .018728211 | .018728211 | .01968247  | .01968247  | 36 | .018728211 | .018728211 | .01968247  | .01968247  |
| 110 | 36 | .010482667 | .010491597  | .01081414  | .01081414  | 36 | .018728211 | .018728211 | .01968247  | .01968247  | 37 | .018728211 | .018728211 | .01968247  | .01968247  |
| 111 | 37 | .010482667 | .010491597  | .01081414  | .01081414  | 37 | .018728211 | .018728211 | .01968247  | .01968247  | 38 | .018728211 | .018728211 | .01968247  | .01968247  |
| 112 | 38 | .010482667 | .010491597  | .01081414  | .01081414  | 38 | .018728211 | .018728211 | .01968247  | .01968247  | 39 | .018728211 | .018728211 | .01968247  | .01968247  |
| 113 | 39 | .010482667 | .010491597  | .01081414  | .01081414  | 39 | .018728211 | .018728211 | .01968247  | .01968247  | 40 | .018728211 | .018728211 | .01968247  | .01968247  |

PERCENTILE POINTS OF THE RETA DISTRIBUTION

MAY 1943

PERCENTILE POINTS OF THE METAL DISTRIBUTION

| N  | 1  | .25        | .50        | .75        | N   | 1          | .25        | .50         | .75         |
|----|----|------------|------------|------------|-----|------------|------------|-------------|-------------|
| 05 | 1  | .220227364 | .210726972 | .214486667 | 100 | 1          | .00287257  | .00690744   | .012672720  |
| 06 | 2  | .10107086  | .011763988 | .025069211 | 2   | .00051473  | .016726667 | .026669460  | .027665068  |
| 07 | 3  | .1820870   | .02806837  | .040851665 | 3   | .01229698  | .02665068  | .038622875  | .038622875  |
| 08 | 4  | .2654224   | .03851696  | .05118749  | 4   | .02541130  | .04659748  | .05556137   | .05556137   |
| 09 | 5  | .3557967   | .04890674  | .062575684 | 5   | .032379482 | .04655774  | .06201056   | .06201056   |
| 10 | 6  | .46606035  | .05907584  | .077136220 | 6   | .04236159  | .056512702 | .07335684   | .07335684   |
| 11 | 7  | .59436813  | .069049392 | .087427427 | 7   | .05666668  | .066667353 | .084467677  | .084467677  |
| 12 | 8  | .7636252   | .080464522 | .100494616 | 8   | .06588238  | .076423641 | .0955853    | .0955853    |
| 13 | 9  | .97203277  | .091901155 | .117002148 | 9   | .08478856  | .098466017 | .106501156  | .106501156  |
| 14 | 10 | .10148541  | .1014854   | .124646888 | 10  | .0977100   | .11746454  | .11746454   | .11746454   |
| 15 | 11 | .11912465  | .11106601  | .13684724  | 11  | .09861918  | .10432032  | .12821059   | .12821059   |
| 16 | 12 | .13011661  | .12220172  | .156116466 | 12  | .09509262  | .11629451  | .13861571   | .13861571   |
| 17 | 13 | .14765286  | .132984131 | .174284139 | 13  | .09126176  | .104565030 | .140565030  | .140565030  |
| 18 | 14 | .1706865   | .143236979 | .189547059 | 14  | .11428452  | .12622556  | .16038938   | .16038938   |
| 19 | 15 | .2000765   | .15368879  | .2081516   | 15  | .12152801  | .146119124 | .17088626   | .17088626   |
| 20 | 16 | .23937742  | .164361714 | .219066551 | 16  | .132811464 | .1515711   | .18157570   | .18157570   |
| 21 | 17 | .28006467  | .17683570  | .220002015 | 17  | .14212887  | .16412300  | .19212072   | .19212072   |
| 22 | 18 | .33094701  | .186327644 | .231300810 | 18  | .15147909  | .20235134  | .20235134   | .20235134   |
| 23 | 19 | .39543291  | .195432917 | .245117637 | 19  | .161826050 | .18455121  | .21342421   | .21342421   |
| 24 | 20 | .47916870  | .206242115 | .256117331 | 20  | .170264948 | .19621247  | .22360772   | .22360772   |
| 25 | 21 | .57020218  | .21670112  | .266496729 | 21  | .17070418  | .20598730  | .236636098  | .236636098  |
| 26 | 22 | .67054247  | .22727094  | .276702785 | 22  | .182746521 | .24646521  | .254646521  | .254646521  |
| 27 | 23 | .78026484  | .23776511  | .287334687 | 23  | .196465020 | .27592002  | .302592002  | .302592002  |
| 28 | 24 | .90929273  | .24926788  | .27883179  | 24  | .20615826  | .25588668  | .26520934   | .26520934   |
| 29 | 25 | .10917418  | .26027624  | .289561611 | 25  | .2178611   | .27456506  | .27456506   | .27456506   |
| 30 | 26 | .13008678  | .27021625  | .300561161 | 26  | .22727280  | .27484196  | .29481715   | .29481715   |
| 31 | 27 | .14688617  | .27977557  | .31124260  | 27  | .246465020 | .28578501  | .306636098  | .306636098  |
| 32 | 28 | .170906689 | .29021480  | .327164916 | 28  | .246465020 | .297575246 | .31677058   | .31677058   |
| 33 | 29 | .20717832  | .30070286  | .332734687 | 29  | .256600942 | .295711883 | .31677058   | .31677058   |
| 34 | 30 | .27987929  | .31110206  | .34370577  | 30  | .26563657  | .295688532 | .32896674   | .32896674   |
| 35 | 31 | .32114927  | .32156277  | .354645747 | 31  | .28565157  | .33719176  | .3715611832 | .3715611832 |
| 36 | 32 | .37907816  | .33217169  | .365170559 | 32  | .286494357 | .315561060 | .367460560  | .367460560  |
| 37 | 33 | .43064510  | .34266572  | .375547551 | 33  | .29652222  | .325584666 | .35750007   | .35750007   |
| 38 | 34 | .492666983 | .352114907 | .384845287 | 34  | .306451130 | .36777802  | .406451130  | .406451130  |
| 39 | 35 | .56211145  | .363363227 | .397232468 | 35  | .314702800 | .36551750  | .377460119  | .377460119  |
| 40 | 36 | .64117114  | .37412849  | .407788421 | 36  | .327275426 | .35648425  | .38863682   | .38863682   |
| 41 | 37 | .73144720  | .38461708  | .419521110 | 37  | .341464560 | .39819271  | .436450562  | .436450562  |
| 42 | 38 | .82617096  | .39510711  | .429146761 | 38  | .343252462 | .37441745  | .406434747  | .406434747  |
| 43 | 39 | .92726808  | .405806248 | .439744927 | 39  | .35202754  | .385528422 | .41842617   | .41842617   |
| 44 | 40 | .10367184  | .416565231 | .443031117 | 40  | .36260936  | .42852762  | .44518348   | .44518348   |
| 45 | 41 | .10950355  | .426705489 | .460702661 | 41  | .37260961  | .405317176 | .43869555   | .43869555   |
| 46 | 42 | .11650393  | .43706431  | .471135785 | 42  | .38242374  | .44528393  | .44865536   | .44865536   |
| 47 | 43 | .124146186 | .447454348 | .48109831  | 43  | .442652071 | .458484952 | .468731217  | .468731217  |
| 48 | 44 | .12982910  | .458062468 | .492522617 | 44  | .462020937 | .488752724 | .488752724  | .488752724  |
| 49 | 45 | .136367184 | .468562700 | .50303217  | 45  | .47194980  | .498717092 | .508717092  | .508717092  |
| 50 | 46 | .144666993 | .479027462 | .513526179 | 46  | .472181004 | .505131716 | .52016695   | .52016695   |
| 51 | 47 | .15250393  | .480510659 | .524600192 | 47  | .473170192 | .505131716 | .52016695   | .52016695   |
| 52 | 48 | .160531143 | .493446657 | .53446657  | 48  | .47450816  | .518682724 | .53804905   | .53804905   |
| 53 | 49 | .168516697 | .49510804  | .54510804  | 49  | .47508350  | .518682724 | .53804905   | .53804905   |
| 54 | 50 | .17651667  | .495108110 | .545108110 | 50  | .47508350  | .518682724 | .53804905   | .53804905   |

## PERCENTILE POINTS OF THE NORMAL ORDER STATISTICS

| N  | I       | .01     | .025    | .05     | .10     | .25     | .50     | .75     | .90     | .95     | .975    | .99     |
|----|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| 2  | 1       | -2.5750 | -2.7390 | -1.9545 | -1.6322 | -1.1078 | -0.5450 | -0.0000 | 0.4783  | 0.7601  | 1.0022  | 1.2816  |
| 3  | 1       | -2.7119 | -2.3909 | -2.1212 | -1.8183 | -1.3319 | -0.8193 | -0.3317 | 0.0900  | 0.3361  | 0.5464  | 0.7877  |
| 2  | -1.5660 | -1.9147 | -1.0115 | -0.8567 | -0.4500 | 0.0000  | 0.4500  | 0.8567  | 1.1015  | 1.3147  | 1.5640  |         |
| 4  | 1       | -2.8058 | -2.6943 | -2.2340 | -1.9432 | -1.4803 | -0.9981 | -0.5450 | -0.1569 | 0.0681  | 0.2595  | 0.4783  |
| 2  | -1.7229 | -1.6940 | -1.2953 | -1.0689 | -0.6966 | -0.2905 | 0.1697  | 0.4664  | 0.6789  | 0.8628  | 1.0764  |         |
| 5  | 1       | -2.8769 | -2.6723 | -2.3187 | -2.0365 | -1.5900 | -1.1290 | -0.6994 | -0.3344 | -0.1238 | 0.0547  | 0.2582  |
| 2  | -1.8428 | -1.6188 | -1.4294 | -1.2147 | -0.8641 | -0.4851 | -0.1151 | 0.2110  | 0.4054  | 0.5722  | 0.7657  |         |
| 3  | -1.2501 | -1.0510 | -0.8805 | -0.6851 | -0.3600 | 0.0000  | 0.3600  | 0.6851  | 0.8806  | 1.0510  | 1.2501  |         |
| 6  | 1       | -2.9319 | -2.6347 | -2.1105 | -1.6765 | -1.2113 | -0.8193 | -0.4713 | -0.2114 | -0.1023 | 0.0900  | 0.9000  |
| 2  | -1.9306 | -1.7139 | -1.5313 | -1.3249 | -0.9897 | -0.6297 | -0.2807 | 0.0259  | 0.3618  | 0.5418  |         |         |
| 3  | -1.3739 | -1.1845 | -1.0230 | -0.884  | -0.5332 | -0.1983 | 0.1337  | 0.4111  | 0.6088  | 0.7628  | 0.9421  |         |
| 7  | 1       | -2.9814 | -2.6865 | -2.4421 | -2.1717 | -1.7476 | -1.3149 | -0.9166 | -0.5810 | -0.3903 | -0.2285 | -0.6450 |
| 2  | -2.6616 | -1.7064 | -1.6130 | -1.4136 | -1.0895 | -0.7438 | -0.4105 | -0.1192 | 0.5119  | 0.7986  | 0.9675  |         |
| 3  | -1.4678 | -1.2873 | -1.1323 | -0.9556 | -0.6648 | -0.3675 | -0.1449 | 0.2435  | 0.4790  | 0.5522  | 0.7882  |         |
| 4  | -1.0102 | -0.9000 | -0.7563 | -0.5870 | -0.3085 | 0.0000  | 0.3085  | 0.5870  | 0.7543  | 0.9000  | 1.0702  |         |
| 8  | 1       | -3.0270 | -2.7307 | -2.4898 | -2.2237 | -1.8078 | -1.3852 | -0.9981 | -0.6742 | -0.4892 | -0.3334 | -0.1569 |
| 2  | -2.6679 | -1.8542 | -1.6809 | -1.4861 | -1.1718 | -0.8376 | -0.5167 | -0.2372 | -0.1736 | 0.0665  | 0.2274  |         |
| 3  | -1.5478 | -1.3707 | -1.2206 | -1.0500 | -0.7702 | -0.4662 | -0.1682 | 0.0959  | 0.2525  | 0.3876  | 0.5440  |         |
| 4  | -1.0173 | -1.0068 | -0.8672 | -0.774  | -0.4424 | -0.1506 | 0.1395  | 0.3999  | 0.5556  | 0.6907  | 0.8181  |         |
| 9  | 1       | -3.0575 | -2.7693 | -2.5312 | -2.2689 | -1.8598 | -1.4457 | -1.0680 | -0.7530 | -0.5736 | -0.4227 | -0.2220 |
| 2  | -2.1117 | -1.9088 | -1.7189 | -1.4848 | -1.2418 | -0.9168 | -0.6060 | -0.3362 | -0.1786 | -0.0439 | -0.1106 |         |
| 3  | -1.6132 | -1.4406 | -1.2965 | -1.1288 | -0.8578 | -0.5444 | -0.2779 | -0.1249 | 0.1248  | 0.2536  | 0.4024  |         |
| 4  | -1.2521 | -1.0919 | -0.9591 | -0.8050 | -0.5505 | -0.2713 | 0.0550  | 0.2518  | 0.3900  | 0.5264  | 0.6744  |         |
| 5  | -0.9584 | -0.7095 | -0.6702 | -0.5216 | -0.2742 | 0.0000  | 0.2742  | 0.5216  | 0.6702  | 0.7995  | 0.9004  |         |
| 10 | 1       | -3.0889 | -2.8034 | -2.5679 | -2.2087 | -1.9055 | -1.4688 | -1.1290 | -0.8215 | -0.6468 | -0.5001 | -0.1444 |
| 2  | -2.6561 | -1.9566 | -1.6602 | -1.3023 | -0.9652 | -0.6828 | -0.4211 | -0.2685 | -0.1381 | 0.0109  | 0.057   |         |
| 3  | -1.6695 | -1.5005 | -1.3578 | -1.1961 | -0.9324 | -0.6477 | -0.3707 | -0.1267 | 0.0751  | 0.1811  | 0.2919  |         |
| 4  | -1.3212 | -1.1673 | -1.0363 | -0.8869 | -0.6457 | -0.3716 | -0.1602 | 0.2705  | 0.3920  | 0.5227  | 0.6744  |         |
| 5  | -1.0345 | -0.8887 | -0.7660 | -0.6209 | -0.3825 | -0.1214 | 0.1396  | 0.3740  | 0.5143  | 0.6360  | 0.7778  |         |
| 11 | 1       | -3.1171 | -2.8349 | -2.6007 | -2.1443 | -1.9462 | -1.5659 | -1.1830 | -0.8821 | -0.7114 | -0.5683 | -0.4068 |
| 2  | -2.1955 | -1.9985 | -1.8141 | -1.6502 | -1.3556 | -0.9452 | -0.7500 | -0.4952 | -0.3468 | -0.2204 | -0.057  |         |
| 3  | -1.7188 | -1.6529 | -1.4141 | -1.2548 | -0.9972 | -0.7199 | -0.4507 | -0.2143 | -0.1075 | 0.0445  | 0.1823  |         |
| 4  | -1.3889 | -1.2705 | -1.1027 | -0.9572 | -0.7170 | -0.4771 | -0.2077 | 0.1270  | 0.1621  | 0.2786  | 0.4136  |         |
| 5  | -1.0109 | -0.9641 | -0.8321 | -0.7046 | -0.4761 | -0.2227 | 0.0278  | 0.2520  | 0.2858  | 0.5018  | 0.6366  |         |
| 6  | -0.8633 | -0.7264 | -0.6000 | -0.4741 | -0.2403 | 0.0000  | 0.2493  | 0.4741  | 0.6090  | 0.7264  | 0.8633  |         |
| 12 | 1       | -3.1427 | -2.8616 | -2.6103 | -2.1764 | -1.9829 | -1.5882 | -1.2313 | -0.9362 | -0.7691 | -0.6291 | -0.4713 |

## PERCENTILE POINTS OF THE NORMAL ORDER STATISTICS

| N  | I        | .01      | .025     | .05      | .10      | .25      | .50     | .75     | .90     | .95     | .975    | .99     |
|----|----------|----------|----------|----------|----------|----------|---------|---------|---------|---------|---------|---------|
| 12 | 2        | -2.27308 | -2.01626 | -2.01624 | -1.6629  | -1.4031  | -1.0986 | -0.8096 | -0.5607 | -0.4161 | -0.2929 | -0.1521 |
| 3  | -1.62626 | -1.5092  | -1.46220 | -1.3067  | -1.0564  | -0.7834  | -0.5210 | -0.2910 | -0.1558 | -0.0938 | -0.0937 |         |
| 4  | -1.4132  | -1.28559 | -1.1609  | -1.0185  | -0.7852  | -0.5114  | -0.2825 | -0.0620 | -0.0686 | -0.1811 | -0.1112 |         |
| 5  | -1.1677  | -1.0794  | -0.9115  | -0.7767  | -0.5538  | -0.3093  | -0.1675 | -0.0484 | -0.0484 | -0.2771 | -0.1854 |         |
| 6  | -0.9361  | -0.8331  | -0.6894  | -0.5487  | -0.3416  | -0.1C17  | -0.1374 | -0.1524 | -0.4811 | -0.5928 | -0.7228 |         |
| 13 | 1        | -1.01660 | -2.08864 | -2.06574 | -2.4057  | -2.0164  | -1.5265 | -1.2750 | -0.9550 | -0.8210 | -0.6438 | -0.5293 |
| 2  | -2.26278 | -2.00704 | -1.9102  | -1.7314  | -1.4460  | -1.1264  | -0.8621 | -0.6194 | -0.4780 | -0.3577 | -0.2202 |         |
| 3  | -1.80220 | -1.6412  | -1.5059  | -1.3632  | -1.1055  | -0.8200  | -0.5835 | -0.3591 | -0.2273 | -0.1144 | -0.0155 |         |
| 4  | -1.0799  | -1.0351  | -1.0173  | -0.9731  | -0.8447  | -0.5269  | -0.3145 | -0.1402 | -0.1134 | -0.0957 | -0.2118 |         |
| 5  | -1.22221 | -1.0867  | -0.9115  | -0.8398  | -0.6226  | -0.3849  | -0.1502 | -0.0888 | -0.0888 | -0.1830 | -0.2904 |         |
| 6  | -0.9993  | -0.8567  | -0.7580  | -0.6319  | -0.4212  | -0.1F89  | -0.0419 | -0.0488 | -0.0488 | -0.1724 | -0.4795 |         |
| 7  | -0.7965  | -0.6703  | -0.5670  | -0.4375  | -0.2701  | -0.0706  | -0.2301 | -0.4175 | -0.6200 | -0.6193 | -0.7965 |         |
| 14 | 1        | -3.01875 | -2.09101 | -2.06822 | -2.4325  | -2.0468  | -1.6615 | -1.3149 | -1.0294 | -0.8662 | -0.7335 | -0.5819 |
| 2  | -2.0921  | -2.0116  | -1.9411  | -1.7665  | -1.4849  | -1.1500  | -0.9114 | -0.6724 | -0.5348 | -0.4161 | -0.2817 |         |
| 3  | -1.8377  | -1.6790  | -1.5556  | -1.3952  | -1.1456  | -0.8110  | -0.6190 | -0.4201 | -0.2914 | -0.1811 | -0.0545 |         |
| 4  | -1.5218  | -1.3796  | -1.2088  | -1.1220  | -0.8880  | -0.6555  | -0.4186 | -0.2096 | -0.1862 | -0.0200 | -0.1425 |         |
| 5  | -1.27706 | -1.01373 | -1.0148  | -0.9163  | -0.6246  | -0.4117  | -0.2242 | -0.1211 | -0.1004 | -0.0445 | -0.3251 |         |
| 6  | -1.05551 | -0.9284  | -0.8271  | -0.6962  | -0.4590  | -0.2452  | -0.1134 | -0.0580 | -0.0580 | -0.2782 | -0.4816 |         |
| 7  | -0.8656  | -0.7477  | -0.6323  | -0.5113  | -0.3101  | -0.0975  | -0.1145 | -0.1342 | -0.4537 | -0.5575 | -0.5783 |         |
| 15 | 1        | -2.02073 | -2.09316 | -2.07751 | -2.44573 | -2.0749  | -1.6937 | -1.3314 | -1.0700 | -0.9114 | -0.7789 | -0.5300 |
| 2  | -2.01189 | -2.01302 | -1.9746  | -1.7987  | -1.5225  | -1.2297  | -0.9555 | -0.7206 | -0.5846 | -0.4691 | -0.3374 |         |
| 3  | -1.8704  | -1.7145  | -1.5435  | -1.4335  | -1.1425  | -0.8727  | -0.6105 | -0.4753 | -0.4193 | -0.2177 |         |         |
| 4  | -1.6599  | -1.4105  | -1.3063  | -1.1662  | -0.9462  | -0.7083  | -0.4764 | -0.2720 | -0.1515 | -0.0479 | -0.7115 |         |
| 5  | -1.3144  | -1.01838 | -1.01729 | -0.9464  | -0.7486  | -0.5114  | -0.2586 | -0.0904 | -0.0270 | -0.1252 | -0.2453 |         |
| 6  | -1.0560  | -0.8667  | -0.8167  | -0.7514  | -0.5529  | -0.3427  | -0.1449 | -0.0796 | -0.0154 | -0.2955 | -0.4117 |         |
| 7  | -0.9174  | -0.7972  | -0.6744  | -0.5764  | -0.3804  | -0.1641  | -0.0511 | -0.0242 | -0.0242 | -0.3596 | -0.4597 |         |
| 8  | -0.7610  | -0.6254  | -0.5264  | -0.4083  | -0.2167  | -0.0006  | -0.2167 | -0.4083 | -0.5244 | -0.6254 | -0.7430 |         |
| 16 | 1        | -3.02259 | -2.09515 | -2.07265 | -2.44803 | -2.0710  | -1.7725 | -1.4075 | -1.075  | -0.9112 | -0.8227 | -0.6742 |
| 2  | -2.06338 | -2.01567 | -2.0113  | -1.8283  | -1.5533  | -1.2663  | -0.9961 | -0.6649 | -0.5312 | -0.4177 | -0.2885 |         |
| 3  | -1.86004 | -1.6151  | -1.4686  | -1.2086  | -0.9214  | -0.6795  | -0.4763 | -0.2886 | -0.1594 | -0.1751 |         |         |
| 4  | -1.45248 | -1.04662 | -1.0332  | -0.9066  | -0.9900  | -0.7563  | -0.5288 | -0.2886 | -0.2107 | -0.1094 | -0.0774 |         |
| 5  | -1.3542  | -1.02256 | -1.01165 | -0.9222  | -0.7879  | -0.5654  | -0.3471 | -0.1517 | -0.0391 | -0.1738 |         |         |
| 6  | -1.0500  | -0.8020  | -0.7949  | -0.6856  | -0.5056  | -0.3933  | -0.1807 | -0.0888 | -0.1215 | -0.2189 | -0.3117 |         |
| 7  | -0.9683  | -0.8505  | -0.7438  | -0.6344  | -0.4430  | -0.2321  | -0.0227 | -0.0168 | -0.0168 | -0.2767 | -0.4716 |         |
| 8  | -0.8006  | -0.6855  | -0.5310  | -0.4738  | -0.2853  | -0.0768  | -0.1313 | -0.1185 | -0.4306 | -0.5279 | -0.6412 |         |
| 17 | 1        | -3.02432 | -2.09702 | -2.07754 | -2.45018 | -2.07253 | -1.7512 | -1.4165 | -1.075  | -0.9880 | -0.8594 | -0.7146 |
| 2  | -2.06779 | -2.01313 | -2.00273 | -1.8559  | -1.5837  | -1.3001  | -0.9335 | -0.6017 | -0.5741 | -0.4625 | -0.3354 |         |
| 3  | -1.8628  | -1.7746  | -1.5011  | -1.2674  | -0.9185  | -0.6795  | -0.4519 | -0.2277 | -0.1367 | -0.1751 |         |         |
| 4  | -1.62629 | -1.4200  | -1.3765  | -1.2436  | -0.9303  | -0.7002  | -0.5767 | -0.303  | -0.2646 | -0.1654 |         |         |
| 5  | -1.3906  | -1.07639 | -1.01562 | -0.9340  | -0.8331  | -0.6146  | -0.4006 | -0.2111 | -0.0991 | -0.025  | -0.1090 |         |
| 6  | -1.0941  | -0.80709 | -0.7686  | -0.6518  | -0.5590  | -0.4481  | -0.2401 | -0.0950 | -0.0550 | -0.1499 | -0.2599 |         |
| 7  | -0.9142  | -0.7986  | -0.7098  | -0.6867  | -0.4993  | -0.2932  | -0.0889 | -0.0938 | -0.0266 | -0.2969 | -0.4062 |         |
| 8  | -0.8520  | -0.7394  | -0.6630  | -0.5323  | -0.3403  | -0.1450  | -0.0574 | -0.3478 | -0.4420 | -0.5516 |         |         |

TABLE 2. Contd.

## PERCENTILE POINTS OF THE NORMAL ORDER STATISTICS

| N  | I       | .01     | .025    | .05     | .10     | .25     | .50      | .75      | .90      | .95      | .975     | .99      |
|----|---------|---------|---------|---------|---------|---------|----------|----------|----------|----------|----------|----------|
| 17 | 9       | -6.6991 | -5.8884 | -4.935  | -3.9842 | -2.2021 | 0.000    | 2.2021   | 3.843    | 4.935    | 5.5884   | 5.91     |
| 18 | 1       | -3.2594 | -2.9877 | -2.7651 | -2.5219 | -2.1480 | -1.7771  | -1.4457  | -1.1746  | -1.0223  | -0.8953  | -0.7530  |
| 2  | -2.1886 | -2.2043 | -2.515  | -1.8816 | -1.6126 | -1.3315 | -1.0687  | -0.8435  | -0.7138  | -0.6119  | -0.4788  | -0.4788  |
| 3  | -1.9539 | -1.8018 | -1.6744 | -1.5312 | -1.3002 | -1.0546 | -0.8191  | -0.6146  | -0.4951  | -0.3331  | -0.2762  | -0.2762  |
| 4  | -1.6566 | -1.5212 | -1.4071 | -1.2779 | -1.0676 | -0.8608 | -0.6208  | -0.4278  | -0.3162  | -0.2168  | -0.1647  | -0.1647  |
| 5  | -1.4243 | -1.2691 | -1.1930 | -1.0724 | -0.8746 | -0.6597 | -0.4495  | -0.2637  | -0.1536  | -0.0593  | -0.0499  | -0.0499  |
| 6  | -1.2787 | -1.1102 | -1.0096 | -0.8946 | -0.7052 | -0.4981 | -0.2942  | -0.1130  | -0.0554  | -0.0297  | -0.0197  | -0.0197  |
| 7  | -1.1056 | -0.9424 | -0.8454 | -0.7343 | -0.5725 | -0.3485 | -0.1487  | -0.0297  | -0.0159  | -0.0077  | -0.0043  | -0.0043  |
| 8  | -0.8987 | -0.7882 | -0.6936 | -0.5852 | -0.4051 | -0.2064 | -0.0600  | -0.01680 | -0.0297  | -0.0553  | -0.0717  | -0.0717  |
| 9  | -0.7511 | -0.6428 | -0.5499 | -0.4431 | -0.2653 | -0.0684 | -0.01281 | -0.0050  | -0.0108  | -0.0277  | -0.0698  | -0.0698  |
| 19 | 1       | -3.2747 | -3.0042 | -2.7826 | -2.5408 | -2.1802 | -1.8013  | -1.4711  | -1.2048  | -1.0543  | -0.9289  | -0.7884  |
| 2  | -2.4089 | -2.2258 | -2.0741 | -1.9056 | -1.6385 | -1.3409 | -1.0705  | -0.8788  | -0.7503  | -0.6425  | -0.5192  | -0.5192  |
| 3  | -1.9781 | -1.8273 | -1.7011 | -1.5593 | -1.3085 | -1.0981 | -0.8557  | -0.6542  | -0.5365  | -0.4361  | -0.3211  | -0.3211  |
| 4  | -1.6843 | -1.5504 | -1.475  | -1.3097 | -1.1019 | -0.8783 | -0.6616  | -0.4716  | -0.3600  | -0.2644  | -0.1542  | -0.1542  |
| 5  | -1.4554 | -1.3318 | -1.2270 | -1.080  | -0.912  | -0.7013 | -0.4946  | -0.2941  | -0.1114  | -0.0644  | -0.0044  | -0.0044  |
| 6  | -1.2635 | -1.1667 | -1.0473 | -0.9361 | -0.7476 | -0.5440 | -0.348   | -0.1661  | -0.0607  | -0.0302  | -0.0152  | -0.0152  |
| 7  | -1.0947 | -0.9827 | -0.8871 | -0.7779 | -0.5712 | -0.3891 | -0.2043  | -0.0287  | -0.0752  | -0.1649  | -0.2689  | -0.2689  |
| 8  | -0.9413 | -0.8326 | -0.7398 | -0.6333 | -0.4667 | -0.2621 | -0.0691  | -0.0138  | -0.0268  | -0.0961  | -0.1997  | -0.1997  |
| 9  | -0.7983 | -0.6920 | -0.6009 | -0.4963 | -0.3223 | -0.1309 | -0.0617  | -0.0139  | -0.0368  | -0.0462  | -0.0300  | -0.0300  |
| 10 | -0.6521 | -0.5874 | -0.4675 | -0.3640 | -0.1914 | -0.000  | -0.01915 | -0.03640 | -0.04675 | -0.0574  | -0.0621  | -0.0621  |
| 20 | 1       | -3.2893 | -3.0197 | -2.7992 | -2.5586 | -2.1896 | -1.8242  | -1.4988  | -1.2332  | -1.0861  | -0.9604  | -0.8217  |
| 2  | -2.4280 | -2.2461 | -2.0955 | -1.9282 | -1.6633 | -1.3884 | -1.1400  | -0.9117  | -0.7854  | -0.6815  | -0.5569  | -0.5569  |
| 3  | -2.0007 | -1.8512 | -1.7260 | -1.5856 | -1.3596 | -1.1103 | -0.8899  | -0.6911  | -0.5751  | -0.4762  | -0.3629  | -0.3629  |
| 4  | -1.7102 | -1.5776 | -1.4658 | -1.3396 | -1.1140 | -0.9133 | -0.6095  | -0.5124  | -0.4025  | -0.3083  | -0.2000  | -0.2000  |
| 5  | -1.4844 | -1.3622 | -1.2586 | -1.1410 | -0.9865 | -0.7399 | -0.5361  | -0.3567  | -0.2507  | -0.1596  | -0.0545  | -0.0545  |
| 6  | -1.2957 | -1.1803 | -1.0323 | -0.9706 | -0.7668 | -0.5864 | -0.3895  | -0.2150  | -0.1116  | -0.0224  | -0.0806  | -0.0806  |
| 7  | -1.1293 | -1.0198 | -0.8267 | -0.8181 | -0.6097 | -0.4556 | -0.2571  | -0.0821  | -0.0196  | -0.0175  | -0.0292  | -0.0292  |
| 8  | -0.9805 | -0.8735 | -0.7821 | -0.6774 | -0.5040 | -0.3131 | -0.1219  | -0.0452  | -0.0160  | -0.0132  | -0.0433  | -0.0433  |
| 9  | -0.8414 | -0.7369 | -0.6475 | -0.5448 | -0.3743 | -0.1859 | -0.0015  | -0.0696  | -0.0270  | -0.0370  | -0.0481  | -0.0481  |
| 10 | -0.7097 | -0.6069 | -0.5188 | -0.4175 | -0.2487 | -0.0617 | -0.01250 | -0.02930 | -0.03936 | -0.04809 | -0.05826 | -0.05826 |
| 21 | 1       | -3.3029 | -3.0345 | -2.8149 | -2.5755 | -2.2085 | -1.8457  | -1.5230  | -1.2599  | -1.1126  | -0.9900  | -0.8527  |
| 2  | -2.4460 | -2.2652 | -2.1156 | -1.9495 | -1.6867 | -1.4143 | -1.1594  | -0.9626  | -0.8178  | -0.7122  | -0.5922  | -0.5922  |
| 3  | -2.0020 | -1.8737 | -1.7495 | -1.6103 | -1.3862 | -1.1488 | -0.9220  | -0.7256  | -0.6111  | -0.5136  | -0.4119  | -0.4119  |
| 4  | -1.7345 | -1.6030 | -1.4923 | -1.3673 | -1.1640 | -0.9459 | -0.7350  | -0.5504  | -0.4421  | -0.3421  | -0.2427  | -0.2427  |
| 5  | -1.5116 | -1.3906 | -1.2882 | -1.1710 | -0.9817 | -0.7759 | -0.5751  | -0.3982  | -0.2939  | -0.2043  | -0.1010  | -0.1010  |
| 6  | -1.3257 | -1.2117 | -1.1149 | -1.0046 | -0.8273 | -0.6257 | -0.4319  | -0.2685  | -0.1586  | -0.0300  | -0.0300  | -0.0300  |
| 7  | -1.1633 | -1.0543 | -0.9614 | -0.8553 | -0.6885 | -0.4885 | -0.2996  | -0.1314  | -0.0316  | -0.0155  | -0.0153  | -0.0153  |
| 8  | -0.9167 | -0.8113 | -0.8212 | -0.7182 | -0.5675 | -0.3600 | -0.1763  | -0.0695  | -0.0902  | -0.0175  | -0.0245  | -0.0245  |
| 9  | -0.8811 | -0.7783 | -0.6903 | -0.5894 | -0.4219 | -0.2371 | -0.0535  | -0.1059  | -0.0291  | -0.0191  | -0.0398  | -0.0398  |
| 10 | -0.7532 | -0.6522 | -0.5657 | -0.4663 | -0.3008 | -0.1177 | -0.0648  | -0.2297  | -0.0368  | -0.0119  | -0.0509  | -0.0509  |
| 11 | -0.6304 | -0.507  | -0.4451 | -0.3466 | -0.1823 | -0.0000 | -0.01823 | -0.03456 | -0.04451 | -0.05307 | -0.06304 | -0.06304 |
| 22 | 1       | -3.3159 | -3.0485 | -2.8298 | -2.5916 | -2.2265 | -1.8459  | -1.5461  | -1.2851  | -1.1392  | -0.9821  | -0.821   |
| 2  | -2.4631 | -2.2843 | -2.1346 | -1.9696 | -1.7988 | -1.4387 | -1.1862  | -0.9717  | -0.8483  | -0.7440  | -0.6264  | -0.6264  |

## PERCENTILE POINTS OF THE NORMAL ORDER STATISTICS

| N  | 1        | .01      | .025    | .05     | .10     | .25      | .50     | .75      | .90     | .95     | .975    | .99     |
|----|----------|----------|---------|---------|---------|----------|---------|----------|---------|---------|---------|---------|
| 22 | 3        | -2.0422  | -1.6949 | -1.7717 | -1.6336 | -1.4115  | -1.1765 | -0.9521  | -0.7580 | -0.6450 | -0.5487 | -0.4385 |
| 4  | -1.7571  | -1.6270  | -1.5173 | -1.3936 | -1.1923 | -0.9766  | -0.7682 | -0.5860  | -0.4792 | -0.3877 | -0.2826 |         |
| 5  | -1.6371  | -1.6172  | -1.2159 | -1.2009 | -1.0128 | -0.8095  | -0.6114 | -0.4370  | -0.3343 | -0.2460 | -0.1643 |         |
| 6  | -1.5338  | -1.2741  | -1.1453 | -1.0363 | -0.8773 | -0.6624  | -0.4714 | -0.3024  | -0.2024 | -0.1163 | -0.0767 |         |
| 7  | -1.4942  | -1.0864  | -0.9947 | -0.8900 | -0.7173 | -0.5285  | -0.3425 | -0.1712  | -0.0791 | -0.0756 | -0.0353 |         |
| 8  | -1.4504  | -0.9464  | -0.8576 | -0.7560 | -0.5879 | -0.4034  | -0.2209 | -0.0581  | -0.0388 | -0.1224 | -0.2194 |         |
| 9  | -0.9179  | -0.8165  | -0.7299 | -0.6306 | -0.4558 | -0.2843  | -0.1041 | -0.0571  | -0.0364 | -0.2364 | -0.2129 |         |
| 10 | -0.7933  | -0.6919  | -0.6788 | -0.5111 | -0.3486 | -0.1491  | -0.0097 | -0.0170  | -0.0265 | -0.1490 | -0.4556 |         |
| 11 | -0.6742  | -0.5763  | -0.4921 | -0.3956 | -0.2346 | -0.0561  | -0.1221 | -0.2824  | -0.3785 | -0.4518 | -0.589  |         |
| 23 | 1        | -3.3284  | -3.0618 | -2.8440 | -2.6067 | -2.2436  | -1.8854 | -1.5675  | -1.1090 | -1.1644 | -1.0442 | -0.9098 |
| 2  | -2.4793  | -2.3075  | -2.1526 | -1.9887 | -1.7298 | -1.4617  | -1.2116 | -0.9892  | -0.8771 | -0.7739 | -0.6667 |         |
| 3  | -2.0612  | -1.9149  | -1.7926 | -1.6556 | -1.4554 | -1.2025  | -0.9805 | -0.7881  | -0.6769 | -0.5317 | -0.4710 |         |
| 4  | -1.7789  | -1.6496  | -1.5409 | -1.4181 | -1.2189 | -1.0054  | -0.7995 | -0.6194  | -0.5140 | -0.4237 | -0.3101 |         |
| 5  | -1.5611  | -1.4423  | -1.3419 | -1.2281 | -1.0221 | -0.8411  | -0.6455 | -0.4774  | -0.3720 | -0.2850 | -0.1848 |         |
| 6  | -1.3803  | -1.2686  | -1.1779 | -1.0661 | -0.8692 | -0.6968  | -0.5082 | -0.3418  | -0.2443 | -0.1585 | -0.0607 |         |
| 7  | -1.2230  | -1.1165  | -1.0259 | -0.9224 | -0.7519 | -0.5657  | -0.3824 | -0.2197  | -0.1232 | -0.0400 | -0.0562 |         |
| 8  | -1.0819  | -0.9791  | -0.8915 | -0.7912 | -0.6555 | -0.4437  | -0.2641 | -0.1061  | -0.0089 | -0.0732 | -0.1884 |         |
| 9  | -0.9521  | -0.8621  | -0.7667 | -0.6688 | -0.5065 | -0.3280  | -0.1500 | -0.0073  | -0.0161 | -0.1831 | -0.2778 |         |
| 10 | -0.8304  | -0.7326  | -0.6488 | -0.5526 | -0.3928 | -0.2165  | -0.0411 | -0.1161  | -0.2160 | -0.2913 | -0.1857 |         |
| 11 | -0.7146  | -0.6183  | -0.5357 | -0.4407 | -0.2826 | -0.1076  | -0.0669 | -0.2228  | -0.3176 | -0.3990 | -0.4917 |         |
| 12 | -0.6029  | -0.5076  | -0.4257 | -0.3215 | -0.1744 | -0.0000  | -0.1744 | -0.1415  | -0.4257 | -0.5075 | -0.6020 |         |
| 74 | 1        | -3.34602 | -3.0745 | -2.8575 | -2.6213 | -2.2500  | -1.8038 | -1.5882  | -1.3317 | -1.1884 | -1.0692 | -0.9167 |
| 2  | -2.4947  | -2.3168  | -2.1168 | -1.9059 | -1.6766 | -1.4826  | -1.2356 | -1.0253  | -0.8044 | -0.8023 | -0.6864 |         |
| 3  | -2.0793  | -1.9341  | -1.8125 | -1.5765 | -1.4581 | -1.2272  | -1.0073 | -0.8774  | -0.7669 | -0.6129 | -0.5054 |         |
| 4  | -1.7794  | -1.6711  | -1.5632 | -1.4414 | -1.2440 | -1.0327  | -0.8288 | -0.6510  | -0.5468 | -0.4576 | -0.3553 |         |
| 5  | -1.5838  | -1.4660  | -1.2537 | -1.0596 | -0.8708 | -0.6775  | -0.5016 | -0.4075  | -0.3217 | -0.2229 |         |         |
| 6  | -1.4052  | -1.2946  | -1.2008 | -1.0961 | -0.9191 | -0.7290  | -0.5430 | -0.3787  | -0.2816 | -0.1980 | -0.1016 |         |
| 7  | -1.2502  | -1.1448  | -1.0551 | -0.9428 | -0.7844 | -0.6006  | -0.4198 | -0.2595  | -0.1644 | -0.0825 | -0.0122 |         |
| 8  | -1.1114  | -1.0096  | -0.9232 | -0.8242 | -0.6606 | -0.4814  | -0.3044 | -0.1469  | -0.0533 | -0.1210 | -0.2266 |         |
| 9  | -0.9840  | -0.8853  | -0.8010 | -0.7044 | -0.5445 | -0.3886  | -0.1944 | -0.0189  | -0.0537 | -0.1338 |         |         |
| 10 | -0.8650  | -0.7685  | -0.6859 | -0.5911 | -0.4330 | -0.2604  | -0.0880 | -0.0663  | -0.1583 | -0.2380 | -0.3305 |         |
| 11 | -0.7521  | -0.6572  | -0.5759 | -0.4824 | -0.3270 | -0.1551  | -0.0161 | -0.1698  | -0.2617 | -0.3413 | -0.4339 |         |
| 12 | -0.6435  | -0.5498  | -0.4693 | -0.3768 | -0.2225 | -0.0515  | -0.1193 | -0.2729  | -0.3650 | -0.4449 | -0.5379 |         |
| 75 | 1        | -3.3515  | -3.0866 | -2.8774 | -2.6351 | -2.2754  | -1.9213 | -1.67078 | -1.3512 | -1.2111 | -1.0931 | -0.9612 |
| 2  | -2.0594  | -1.8661  | -1.7024 | -1.5045 | -1.2685 | -1.05045 | -0.8050 | -0.5284  | -0.303  | -0.8291 | -0.7144 |         |
| 3  | -2.0966  | -1.9571  | -1.8314 | -1.6963 | -1.4795 | -1.2506  | -1.0327 | -0.8447  | -0.7354 | -0.6424 | -0.5361 |         |
| 4  | -1.8188  | -1.6914  | -1.5843 | -1.4635 | -1.2678 | -1.0585  | -0.8567 | -0.6807  | -0.5777 | -0.4897 | -0.3886 |         |
| 5  | -1.6053  | -1.4885  | -1.3898 | -1.2780 | -1.0957 | -0.8989  | -0.7077 | -0.5398  | -0.4410 | -0.3562 | -0.2587 |         |
| 6  | -1.42787 | -1.3191  | -1.2262 | -1.1206 | -0.9474 | -0.795   | -0.5757 | -0.4114  | -0.3176 | -0.2352 | -0.1401 |         |
| 7  | -1.2758  | -1.1714  | -1.0877 | -0.9815 | -0.8150 | -0.6334  | -0.4550 | -0.2968  | -0.2031 | -0.1224 | -0.0291 |         |
| 8  | -1.0786  | -0.9510  | -0.8510 | -0.7511 | -0.6551 | -0.5167  | -0.3422 | -0.1870  | -0.0949 | -0.0153 | -0.0767 |         |
| 9  | -0.9164  | -0.8140  | -0.7332 | -0.7378 | -0.5800 | -0.4656  | -0.3020 | -0.0880  | -0.0691 | -0.0878 | -0.1791 |         |
| 10 | -0.8021  | -0.7065  | -0.6271 | -0.6271 | -0.4824 | -0.3012  | -0.1317 | -0.0199  | -0.1103 | -0.2100 | -0.3788 |         |
| 11 | -0.7870  | -0.6934  | -0.6133 | -0.5212 | -0.3682 | -0.1691  | -0.0309 | -0.1199  | -0.2081 | -0.3788 |         |         |
| 12 | -0.6812  | -0.5889  | -0.5097 | -0.4187 | -0.2670 | -0.0591  | -0.0684 | -0.2691  | -0.3691 | -0.3871 | -0.4782 |         |

| PERCENTILE POINTS OF THE NORMAL ORDER STATISTICS |         |         |          |          |         |          |         |          |         |         |         |
|--|---------|---------|----------|----------|---------|----------|---------|----------|---------|---------|---------|
| N  | I       | .01     | .025     | .05      | .10     | .25      | .50     | .75      | .90     | .95     | .99     |
| 25   | 13      | -5.787  | -4.672   | -4.087   | -3.183  | -2.1674  | -0.5000 | -0.1674  | .3183   | .4087   | .5787   |
| 26   | 1       | -3.3624 | -3.0983  | -2.8828  | -2.6484 | -2.2907  | -1.9383 | -1.6265  | -1.3738 | -1.1157 | -0.9850 |
| 2  | -2.5245 | -2.3473 | -2.2017  | -2.0406  | -1.7866 | -1.5243  | -1.2802 | -1.0735  | -0.9543 | -0.8467 | -0.7211 |
| 3  | -2.1100 | -1.9693 | -1.8494  | -1.7152  | -1.5000 | -1.2729  | -1.0659 | -0.8707  | -0.7623 | -0.6704 | -0.5653 |
| 4  | -1.8373 | -1.7108 | -1.6046  | -1.4865  | -1.2906 | -1.0829  | -0.8811 | -0.7090  | -0.6071 | -0.5200 | -0.4201 |
| 5  | -1.6557 | -1.5098 | -1.4119  | -1.3011  | -1.1203 | -0.9255  | -0.7163 | -0.5703  | -0.4726 | -0.3889 | -0.2926 |
| 6  | -1.4510 | -1.3424 | -1.2503  | -1.1456  | -0.9742 | -0.7882  | -0.6465 | -0.4462  | -0.3515 | -0.2702 | -0.1764 |
| 7  | -1.3000 | -1.1966 | -1.1087  | -1.0086  | -0.8438 | -0.6443  | -0.4881 | -0.3319  | -0.2395 | -0.1559 | -0.0680 |
| 8  | -1.1653 | -1.0658 | -0.9811  | -0.8863  | -0.7276 | -0.5499  | -0.3777 | -0.2247  | -0.1338 | -0.0555 | -0.051  |
| 9  | -1.0422 | -0.9457 | -0.8674  | -0.7572  | -0.6134 | -0.4422  | -0.2731 | -0.1222  | -0.0426 | -0.0449 | -0.1346 |
| 10   | -0.9277 | -0.8236 | -0.7277  | -0.6236  | -0.5079 | -0.3395  | -0.1725 | -0.0233  | -0.0233 | -0.0233 | -0.2317 |
| 11   | -0.8197 | -0.7273 | -0.6082  | -0.5574  | -0.4066 | -0.2602  | -0.0767 | -0.0735  | -0.1620 | -0.2286 | -0.2776 |
| 12   | -0.7164 | -0.6253 | -0.5473  | -0.4575  | -0.3084 | -0.1432  | -0.0213 | -0.1691  | -0.2574 | -0.3440 | -0.4231 |
| 13   | -0.6166 | -0.5265 | -0.4492  | -0.3603  | -0.2120 | -0.0475  | -0.1166 | -0.2644  | -0.3529 | -0.4297 | -0.5191 |
| 27   | 1       | -3.1728 | -2.1095  | -2.0947  | -2.0611 | -2.0046  | -1.9541 | -1.6444  | -1.3934 | -1.2535 | -1.1077 |
| 2  | -2.5369 | -2.1615 | -2.1617  | -2.0564  | -1.8038 | -1.5432  | -1.3009 | -1.0959  | -0.9783 | -0.8790 | -0.7665 |
| 3  | -2.1287 | -1.9268 | -1.8666  | -1.7232  | -1.5195 | -1.2064  | -1.0790 | -0.8951  | -0.7882 | -0.6970 | -0.5930 |
| 4  | -1.8549 | -1.7202 | -1.6236  | -1.5046  | -1.3119 | -1.0662  | -0.9082 | -0.7358  | -0.6349 | -0.5488 | -0.4500 |
| 5  | -1.6451 | -1.5301 | -1.4330  | -1.3220  | -1.1418 | -0.9508  | -0.7634 | -0.5992  | -0.5026 | -0.4198 | -0.3246 |
| 6  | -1.4722 | -1.3644 | -1.2731  | -1.1694  | -0.9995 | -0.8154  | -0.6356 | -0.4771  | -0.3816 | -0.3013 | -0.2177 |
| 7  | -1.3229 | -1.2706 | -1.1334  | -1.0142  | -0.8711 | -0.6935  | -0.5193 | -0.3651  | -0.2739 | -0.1953 | -0.1016 |
| 8  | -1.1900 | -1.0915 | -1.0076  | -0.9118  | -0.7539 | -0.5812  | -0.4112 | -0.2601  | -0.1705 | -0.0933 | -0.0339 |
| 9  | -1.0588 | -0.9744 | -0.8919  | -0.7987  | -0.6447 | -0.4754  | -0.3088 | -0.2082  | -0.1078 | -0.0445 | -0.0299 |
| 10   | -0.9563 | -0.8632 | -0.7837  | -0.6925  | -0.5414 | -0.4426  | -0.2786 | -0.1157  | -0.0638 | -0.0194 | -0.0172 |
| 11   | -0.8504 | -0.7501 | -0.6810  | -0.5914  | -0.4626 | -0.3470  | -0.1844 | -0.0226  | -0.0302 | -0.1172 | -0.2799 |
| 12   | -0.7443 | -0.6505 | -0.5825  | -0.4821  | -0.3625 | -0.2470  | -0.1018 | -0.0226  | -0.1226 | -0.2094 | -0.2846 |
| 13   | -0.6519 | -0.5631 | -0.4870  | -0.3994  | -0.2918 | -0.0945  | -0.0645 | -0.0118  | -0.2145 | -0.3012 | -0.3719 |
| 14   | -0.5571 | -0.4691 | -0.3925  | -0.3025  | -0.1617 | -0.0000  | -0.1612 | -0.0065  | -0.1612 | -0.3935 | -0.4691 |
| 28   | 1       | -3.3628 | -2.1027  | -2.0960  | -2.0773 | -2.0181  | -1.9694 | -1.6615  | -1.4122 | -1.2742 | -1.1580 |
| 2  | -2.5499 | -2.3752 | -2.2310  | -2.0775  | -1.8204 | -1.5614  | -1.3207 | -1.1173  | -0.9005 | -0.9022 | -0.7907 |
| 3  | -2.1447 | -2.0016 | -1.8820  | -1.7505  | -1.5361 | -1.3144  | -1.0118 | -0.9189  | -0.8127 | -0.7224 | -0.6193 |
| 4  | -1.8718 | -1.7468 | -1.6419  | -1.5237  | -1.3225 | -1.0784  | -0.9211 | -0.7613  | -0.6614 | -0.5761 | -0.4784 |
| 5  | -1.6637 | -1.5494 | -1.4530  | -1.3639  | -1.1661 | -0.9748  | -0.7892 | -0.6266  | -0.5311 | -0.4492 | -0.3551 |
| 6  | -1.4974 | -1.3854 | -1.2510  | -1.1920  | -1.0236 | -0.8413  | -0.6613 | -0.5065  | -0.4141 | -0.3347 | -0.2432 |
| 7  | -1.3468 | -1.2431 | -1.1568  | -1.0586  | -0.8970 | -0.7213  | -0.5490 | -0.3955  | -0.3063 | -0.2288 | -0.1392 |
| 8  | -1.2135 | -1.1150 | -1.0128  | -0.9280  | -0.7816 | -0.6108  | -0.4628 | -0.3051  | -0.2051 | -0.1289 | -0.0408 |
| 9  | -1.0940 | -0.9945 | -0.9180  | -0.8267  | -0.6744 | -0.5074  | -0.3426 | -0.1958  | -0.1087 | -0.0314 | -0.0537 |
| 10   | -0.9813 | -0.8912 | -0.8125  | -0.7224  | -0.5732 | -0.4091  | -0.2668 | -0.1018  | -0.0156 | -0.0500 | -0.1454 |
| 11   | -0.8793 | -0.7800 | -0.7119  | -0.6224  | -0.4765 | -0.3167  | -0.1541 | -0.0164  | -0.0752 | -0.1403 | -0.2353 |
| 12   | -0.7803 | -0.6915 | -0.6155  | -0.5287  | -0.3837 | -0.2230  | -0.0616 | -0.0793  | -0.1646 | -0.2884 | -0.4243 |
| 13   | -0.6851 | -0.5974 | -0.5223  | -0.4610  | -0.2922 | -0.1331  | -0.0256 | -0.1680  | -0.2532 | -0.3271 | -0.4130 |
| 14   | -0.5927 | -0.5059 | -0.4314  | -0.3457  | -0.2027 | -0.0642  | -0.1141 | -0.2566  | -0.3419 | -0.4160 | -0.5022 |
| 29   | 1       | -3.3923 | -2.1305  | -2.09170 | -2.0650 | -2.03112 | -1.9842 | -1.65779 | -1.4302 | -1.2922 | -1.0501 |
| 2  | -2.5623 | -2.1881 | -2.02447 | -2.0060  | -1.8661 | -1.55787 | -1.3197 | -1.0220  | -0.9244 | -0.8138 |         |

## PERCENTILE POINTS OF THE NORMAL ORDER STATISTICS

| N  | I  | .01     | .025    | .05     | .10     | .25     | .50     | .75     | .90      | .95      | .975     | .99      |
|----|----|---------|---------|---------|---------|---------|---------|---------|----------|----------|----------|----------|
| 79 | 3  | -2.1581 | -2.0167 | -1.8998 | -1.7670 | -1.5559 | -1.3337 | -1.1228 | -0.9413  | -0.8261  | -0.7466  | -0.6445  |
| 79 | 4  | -1.8879 | -1.7637 | -1.6594 | -1.5420 | -1.3521 | -1.1655 | -0.9549 | -0.7856  | -0.6867  | -0.6022  | -0.5054  |
| 79 | 5  | -1.6814 | -1.5679 | -1.4721 | -1.3638 | -1.1876 | -0.9977 | -0.8138 | -0.6527  | -0.5581  | -0.4771  | -0.3840  |
| 79 | 6  | -1.5116 | -1.4055 | -1.3156 | -1.2136 | -1.0466 | -0.8659 | -0.6897 | -0.5345  | -0.4330  | -0.3645  | -0.2740  |
| 79 | 7  | -1.3656 | -1.2647 | -1.1791 | -1.0817 | -0.9217 | -0.7476 | -0.5771 | -0.4263  | -0.3312  | -0.2605  | -0.1720  |
| 79 | 8  | -1.2558 | -1.1791 | -1.0567 | -0.9228 | -0.8080 | -0.6390 | -0.4728 | -0.3253  | -0.2379  | -0.1626  | -0.0756  |
| 79 | 9  | -1.180  | -1.0743 | -0.9445 | -0.8532 | -0.7025 | -0.5374 | -0.3745 | -0.2296  | -0.1335  | -0.0693  | -0.0166  |
| 79 | 10 | -1.0889 | -0.9177 | -0.8399 | -0.7507 | -0.6031 | -0.4411 | -0.2807 | -0.1377  | -0.0526  | -0.0209  | -0.0060  |
| 79 | 11 | -0.9666 | -0.8173 | -0.7411 | -0.6535 | -0.5084 | -0.3687 | -0.1902 | -0.0486  | -0.0358  | -0.0188  | -0.0034  |
| 79 | 12 | -0.8094 | -0.7217 | -0.6466 | -0.5604 | -0.4172 | -0.2592 | -0.1021 | -0.0386  | -0.0225  | -0.0125  | -0.0052  |
| 79 | 13 | -0.7162 | -0.6297 | -0.5555 | -0.4703 | -0.3285 | -0.1717 | -0.0155 | -0.0124  | -0.0084  | -0.0016  | -0.0003  |
| 79 | 14 | -0.6160 | -0.5403 | -0.4669 | -0.3824 | -0.2416 | -0.0925 | -0.0702 | -0.02102 | -0.0094  | -0.0007  | -0.0001  |
| 79 | 15 | -0.5179 | -0.4579 | -0.3799 | -0.2949 | -0.1557 | -0.0000 | -0.0000 | -0.0000  | -0.0000  | -0.0000  | -0.0000  |
| 30 | 1  | -3.4017 | -1.1405 | -0.9275 | -0.6963 | -0.3438 | -0.1993 | -0.1693 | -0.14475 | -0.13104 | -0.11967 | -0.10700 |
| 30 | 2  | -2.742  | -2.4009 | -2.2579 | -2.0999 | -1.8513 | -1.5954 | -1.3523 | -1.1573  | -1.0425  | -0.9456  | -0.8360  |
| 30 | 3  | -2.1719 | -2.0312 | -1.9119 | -1.7828 | -1.5730 | -1.3523 | -1.1429 | -0.9628  | -0.8584  | -0.7697  | -0.6685  |
| 30 | 4  | -1.933  | -1.7798 | -1.6761 | -1.5595 | -1.3708 | -1.1608 | -0.9767 | -0.8089  | -0.7108  | -0.6271  | -0.5313  |
| 30 | 5  | -1.6983 | -1.5883 | -1.4904 | -1.3829 | -1.2078 | -1.0196 | -0.8373 | -0.6777  | -0.5840  | -0.5038  | -0.4116  |
| 30 | 6  | -1.5300 | -1.4246 | -1.3254 | -1.2241 | -1.0685 | -0.8893 | -0.7148 | -0.5611  | -0.4706  | -0.3929  | -0.3034  |
| 30 | 7  | -1.4054 | -1.2953 | -1.2004 | -1.1038 | -0.9451 | -0.7727 | -0.6038 | -0.4546  | -0.3665  | -0.2906  | -0.2032  |
| 30 | 8  | -1.2571 | -1.1611 | -1.0795 | -0.9864 | -0.8330 | -0.6657 | -0.5012 | -0.3554  | -0.2690  | -0.1946  | -0.1087  |
| 30 | 9  | -1.1407 | -1.0679 | -0.9688 | -0.8784 | -0.7292 | -0.5658 | -0.4247 | -0.2615  | -0.1765  | -0.1032  | -0.0184  |
| 30 | 10 | -1.0332 | -0.9429 | -0.8648 | -0.7775 | -0.6315 | -0.4713 | -0.3128 | -0.1716  | -0.0877  | -0.0151  | -0.0088  |
| 30 | 11 | -0.9325 | -0.8441 | -0.7686 | -0.6321 | -0.5186 | -0.3808 | -0.2244 | -0.0846  | -0.0014  | -0.0005  | -0.0001  |
| 30 | 12 | -0.8170 | -0.7502 | -0.6760 | -0.5208 | -0.4493 | -0.2931 | -0.1384 | -0.0030  | -0.0003  | -0.0001  | -0.0000  |
| 30 | 13 | -0.7456 | -0.6601 | -0.5868 | -0.5026 | -0.3627 | -0.2080 | -0.0561 | -0.0339  | -0.0163  | -0.0037  | -0.0007  |
| 30 | 14 | -0.6573 | -0.5727 | -0.5002 | -0.4168 | -0.2780 | -0.1242 | -0.0290 | -0.0168  | -0.0091  | -0.0026  | -0.0006  |
| 30 | 15 | -0.5713 | -0.4876 | -0.4155 | -0.3327 | -0.1945 | -0.0413 | -0.0117 | -0.0045  | -0.0017  | -0.0005  | -0.0001  |

TABLE 2 Contd.

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## PERCENTILE POINTS OF THF CHI (1 D.F.) ORDER STATISTICS

| N | 1 | .01   | .025  | .05    | .10    | .25    | .50    | .75    | .90    | .95    | .975   | .99    |
|---|---|-------|-------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 2 | 1 | .0153 | .0317 | .0644  | .1687  | .3757  | .6745  | .9022  | .2170  | .4114  | .6449  |        |
| 2 | 2 | .1257 | .1005 | .2840  | .4073  | .6745  | .9518  | .4986  | .9488  | .2345  | .4955  | .8067  |
| 3 | 1 | .0042 | .0105 | .0212  | .0433  | .1149  | .2615  | .4818  | .7320  | .8995  | .0529  | .2387  |
| 3 | 2 | .0739 | .1185 | .1705  | .2470  | .4211  | .6745  | .9811  | .936   | .4933  | .6731  | .8899  |
| 3 | 3 | .2734 | .4751 | .6795  | .6191  | .8964  | .2538  | .6871  | .1141  | .3877  | .6334  | .9747  |
| 4 | 1 | .0031 | .0079 | .0160  | .0326  | .0871  | .2007  | .3757  | .5794  | .7178  | .8459  | .0022  |
| 4 | 2 | .0527 | .0848 | .1226  | .1796  | .3095  | .5040  | .7445  | .935   | .1537  | .2985  | .6726  |
| 4 | 3 | .1775 | .2457 | .3168  | .4131  | .6073  | .8674  | .1657  | .4663  | .6565  | .8278  | .9395  |
| 4 | 4 | .4073 | .5210 | .6374  | .7767  | .10518 | .46081 | .8155  | .2267  | .4099  | .7313  | .9722  |
| 5 | 1 | .0025 | .0053 | .0128  | .0261  | .0761  | .1630  | .3087  | .4804  | .5988  | .7092  | .8450  |
| 5 | 2 | .0410 | .0662 | .0960  | .1411  | .2451  | .4660  | .6745  | .8132  | .9491  | .10723 | .2210  |
| 5 | 3 | .1328 | .1748 | .2305  | .3142  | .4660  | .6745  | .9164  | .1586  | .3128  | .4515  | .6181  |
| 5 | 4 | .2800 | .3673 | .4425  | .5477  | .7485  | .10073 | .2295  | .5882  | .7717  | .9370  | .1360  |
| 5 | 5 | .5217 | .6406 | .7562  | .8082  | .1697  | .5163  | .9117  | .2107  | .5688  | .8038  | .9891  |
| 6 | 1 | .0021 | .0052 | .0107  | .0228  | .0587  | .1372  | .2615  | .4167  | .5144  | .6117  | .7320  |
| 6 | 2 | .0235 | .0356 | .0789  | .1163  | .2024  | .4378  | .5903  | .9078  | .1072  | .2177  | .4487  |
| 6 | 3 | .1064 | .1485 | .2132  | .2945  | .4812  | .5554  | .7608  | .9677  | .1060  | .2192  | .4624  |
| 6 | 4 | .2186 | .2820 | .3405  | .4305  | .5930  | .8064  | .10431 | .2790  | .4245  | .5627  | .7339  |
| 6 | 5 | .3777 | .4460 | .5509  | .6582  | .8606  | .1159  | .3612  | .6819  | .8603  | .9211  | .2156  |
| 6 | 6 | .6191 | .7401 | .8541  | .9971  | .16022 | .19880 | .3780  | .6310  | .8613  | .9428  |        |
| 7 | 1 | .0018 | .0045 | .0092  | .0187  | .0565  | .1184  | .2271  | .3589  | .4512  | .5183  | .6465  |
| 7 | 2 | .0216 | .0365 | .0660  | .1000  | .1738  | .2904  | .4409  | .6016  | .7074  | .8042  | .9218  |
| 7 | 3 | .0819 | .1244 | .1621  | .2167  | .3227  | .4745  | .6528  | .8348  | .9517  | .1057  | .1862  |
| 7 | 4 | .1793 | .2286 | .2666  | .3462  | .4942  | .6745  | .8800  | .1035  | .2125  | .3284  | .4674  |
| 7 | 5 | .2607 | .3274 | .4417  | .5709  | .6065  | .9075  | .1420  | .3746  | .5190  | .6608  | .8057  |
| 7 | 6 | .4630 | .5553 | .6423  | .7511  | .9528  | .12043 | .14834 | .17476 | .1914  | .20892 | .2790  |
| 7 | 7 | .7030 | .9244 | .9287  | .10766 | .13418 | .16793 | .20510 | .24339 | .26828 | .3104  | .3876  |
| 8 | 1 | .0016 | .0040 | .0080  | .0164  | .0464  | .1062  | .2007  | .3188  | .4020  | .4809  | .5794  |
| 8 | 2 | .0216 | .0370 | .0682  | .0861  | .1518  | .2568  | .3809  | .5334  | .6299  | .7168  | .8238  |
| 8 | 3 | .0765 | .1070 | .1407  | .1861  | .2801  | .4132  | .5728  | .7350  | .8411  | .9151  |        |
| 8 | 4 | .1527 | .1981 | .2442  | .3080  | .4246  | .5821  | .7446  | .8451  | .9508  | .10620 | .2867  |
| 8 | 5 | .2610 | .3119 | .3708  | .4463  | .5896  | .7719  | .9760  | .11758 | .13020 | .14147 | .5508  |
| 8 | 6 | .3762 | .4526 | .5248  | .6155  | .7837  | .9334  | .12250 | .14507 | .15932 | .17211 | .8747  |
| 8 | 7 | .5289 | .6223 | .7214  | .8105  | .10307 | .12282 | .15521 | .18209 | .19918 | .21462 | .23278 |
| 8 | 8 | .7762 | .8976 | .10112 | .1501  | .14081 | .17436 | .21047 | .24415 | .27270 | .29518 | .32260 |
| 9 | 1 | .0014 | .0035 | .0071  | .0146  | .0394  | .0930  | .1799  | .2368  | .3162  | .4348  | .5251  |
| 9 | 2 | .0218 | .0352 | .0514  | .0762  | .1247  | .2271  | .3481  | .4794  | .5668  | .6472  | .7455  |
| 9 | 3 | .0660 | .0940 | .1278  | .1630  | .2475  | .3668  | .5108  | .6550  | .7548  | .8418  | .9060  |
| 9 | 4 | .1223 | .1726 | .2111  | .2668  | .3792  | .5145  | .6776  | .8406  | .9444  | .10379 | .15070 |

| PERCENTILE POINTS OF THE CHI (1 D.F.) ORDER STATISTICS |    |       |         |         |         |         |         |         |         |         |         |         |
|--|----|-------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| N  | I  | .01   | .02     | .05     | .10     | .25     | .50     | .75     | .90     | .95     | .975    | .99     |
| 9  | 5  | .2149 | .2689   | .3204   | .3866   | .5129   | .6745   | .8561   | .1.0344 | .1.1470 | .1.2481 | .1.3491 |
| 9  | 6  | .2187 | .2864   | .4467   | .5252   | .6714   | .8540   | .1.0560 | .1.2525 | .1.3752 | .1.4871 | .1.5100 |
| 7  | 4  | .4450 | .5262   | .5982   | .6902   | .8586   | .1.0666 | .1.2945 | .1.5161 | .1.6559 | .1.7814 | .1.9321 |
| 8  | 7  | .6967 | .7073   | .7967   | .8995   | .1.979  | .1.3619 | .1.6111 | .1.8752 | .2.0493 | .2.1953 | .2.3791 |
| 9  | 8  | .8407 | .9616   | .1.0732 | .1.2114 | .1.4656 | .1.7858 | .2.1512 | .2.4229 | .2.7655 | .2.9879 | .3.2505 |
| 10   | 1  | .6013 | .6042   | .7064   | .8461   | .1.0131 | .1.3555 | .1.0840 | .1.1510 | .1.2607 | .1.3394 | .1.3668 |
| 10   | 2  | .6195 | .7316   | .8837   | .1.056  | .1.457  | .2.210  | .2.048  | .1.152  | .4.3556 | .5160   | .5903   |
| 3  | 3  | .6506 | .6827   | .1.171  | .1.892  | .2.374  | .3.300  | .4.613  | .5.972  | .6.8556 | .7.655  | .8.628  |
| 4  | 4  | .1897 | .2367   | .2825   | .3416   | .4547   | .6003   | .6063   | .7583   | .8515   | .9394   | .1.0426 |
| 5  | 5  | .2350 | .2772   | .3250   | .3971   | .4506   | .5895   | .7526   | .9264   | .1.0289 | .1.1093 | .1.2310 |
| 6  | 7  | .4506 | .4514   | .5140   | .5052   | .7426   | .9247   | .1.1724 | .1.3178 | .1.4394 | .1.5483 | .1.6797 |
| 7  | 8  | .5814 | .5887   | .6627   | .7561   | .9241   | .1.1298 | .1.3465 | .1.5725 | .1.7100 | .1.8734 | .1.9818 |
| 8  | 9  | .6075 | .6677   | .7618   | .9521   | .9604   | .1.1558 | .1.3975 | .1.6625 | .1.9226 | .2.0883 | .2.4136 |
| 9  | 10 | .6983 | .1.0184 | 1.1291  | 1.2656  | 1.3163  | 1.8119  | 2.1973  | 2.6595  | 2.7995  | 3.0109  | 3.2891  |
| 11   | 1  | .6011 | .6020   | .6858   | .8119   | .9324   | .1.0766 | .1.1600 | .1.2390 | .1.3050 | .1.4228 | .1.5277 |
| 11   | 2  | .6176 | .6285   | .6418   | .6620   | .7167   | .1.165  | .1.280  | .1.4092 | .1.4755 | .1.5429 | .1.6277 |
| 2  | 3  | .6537 | .6755   | .6990   | .7317   | .7910   | .1.3000 | .1.408  | .1.5463 | .1.6281 | .1.7027 | .1.7932 |
| 4  | 4  | .1165 | .1274   | .1761   | .2127   | .2708   | .4177   | .5641   | .6915   | .7796   | .8502   | .9550   |
| 5  | 5  | .1602 | .2115   | .2456   | .2758   | .3468   | .4088   | .5416   | .6521   | .7467   | .8456   | .1.0196 |
| 6  | 6  | .2074 | .2074   | .2456   | .3468   | .5267   | .6745   | .8206   | .9888   | .9992   | 1.1002  | 1.1980  |
| 7  | 7  | .3248 | .3268   | .4525   | .5252   | .6572   | .8206   | .9999   | 1.1737  | 1.2828  | 1.3803  | 1.4970  |
| 8  | 8  | .4303 | .5104   | .5764   | .6157   | .7477   | .8056   | .867    | 1.1830  | 1.4944  | 1.6015  | 1.7298  |
| 9  | 9  | .5644 | .6648   | .7271   | .8149   | .8820   | .1.1856 | .1.4073 | .1.6721 | .1.7576 | .1.8792 | .2.0254 |
| 10   | 10 | .7279 | .7701   | .8071   | .1.0167 | 1.2001  | .4468   | .1.7081 | .2.0447 | .2.1287 | .2.2757 | .2.4556 |
| 11   | 11 | .9501 | 1.0693  | 1.1700  | 1.3139  | 1.5615  | 1.8730  | 2.2200  | 2.5923  | 2.8102  | 3.0486  | 3.3160  |
| 12   | 1  | .6010 | .6026   | .6853   | .8110   | .9297   | .1.0704 | .1.1377 | .1.2206 | .1.3800 | .1.4107 | .1.5027 |
| 12   | 2  | .6161 | .6262   | .6382   | .6667   | .7088   | .1.173  | .1.2651 | .1.3685 | .1.4281 | .1.5027 | .1.5822 |
| 3  | 3  | .6489 | .6688   | .6907   | .7202   | .7838   | .1.2750 | .1.3669 | .1.5037 | .1.5800 | .1.6497 | .1.7445 |
| 4  | 4  | .1163 | .1247   | .1546   | .1945   | .2763   | .3820   | .5081   | .6361   | .7181   | .7924   | .8819   |
| 5  | 5  | .1678 | .1912   | .2280   | .2776   | .3124   | .4766   | .6121   | .7127   | .8048   | .9368   | 1.0713  |
| 6  | 6  | .2205 | .2625   | .3124   | .3694   | .4766   | .6762   | .9110   | 1.0878  | 1.1878  | 1.2878  | 1.3755  |
| 7  | 7  | .3540 | .4060   | .4709   | .5098   | .7197   | .9014   | 1.06621 | 1.1618  | 1.2510  | 1.3575  | 1.4510  |
| 8  | 8  | .4288 | .4522   | .5113   | .5775   | .8846   | .1.0585 | 1.1210  | 1.2316  | 1.3437  | 1.4546  | 1.5486  |
| 9  | 9  | .5886 | .6427   | .6653   | .6321   | .7130   | .8618   | .1.0416 | .1.2364 | .1.4249 | .1.6484 | .1.7750 |
| 10   | 10 | .7168 | .6007   | .7754   | .8678   | 1.0010  | .1.2354 | .1.4543 | .1.6667 | .1.7909 | .1.9200 | 2.0644  |
| 11   | 11 | .8691 | .9568   | .7730   | .9616   | 1.2961  | 1.4090  | .1.7400 | 2.01024 | 2.1641  | 2.3105  | 2.4840  |
| 12   | 12 | .9971 | 1.1155  | 1.2741  | 1.3576  | 1.5072  | 1.9101  | 2.2621  | 2.6220  | 2.8578  | 3.0747  | 3.2402  |
| 13   | 1  | .6010 | .6024   | .6859   | .8101   | .9274   | .1.0651 | .1.1271 | .1.2240 | .1.3600 | .1.4148 | .1.4840 |
| 13   | 2  | .6162 | .6261   | .6352   | .6623   | .6930   | .1.583  | .2457   | .3472   | .4075   | .4681   | .5250   |
| 3  | 3  | .6449 | .6649   | .6820   | .7105   | .7193   | .2579   | .3587   | .4667   | .5390   | .6045   | .6842   |
| 4  | 4  | .8774 | .1142   | .1142   | .1142   | .1142   | .2782   | .3522   | .4698   | .5492   | .6661   | .7454   |
| 5  | 5  | .1294 | .1746   | .2091   | .2540   | .3008   | .4540   | .5833   | .7118   | .8674   | .9559   | 1.0700  |
| 6  | 6  | .2484 | .2484   | .2484   | .2484   | .2484   | .4455   | .5508   | .7010   | .8185   | .9253   | 1.0063  |

| PERCENTILE POINTS OF THE CHI (1 D.F.) ORDER STATISTICS |    |        |        |        |        |        |        |        |        |         |         |         |
|--|----|--------|--------|--------|--------|--------|--------|--------|--------|---------|---------|---------|
| N  | I  | .01    | .025   | .05    | .10    | .25    | .50    | .75    | .90    | .95     | .975    | .99     |
| 13   | 7  | .7790  | .3706  | .3670  | .4273  | .5374  | .6745  | .8256  | .9724  | .9646   | .9471   | .9457   |
| 8  | 8  | .7490  | .4067  | .4604  | .5260  | .6484  | .7076  | .9605  | .1176  | .1216   | .1040   | .1040   |
| 9  | 9  | .6387  | .5040  | .5667  | .6181  | .7717  | .9363  | .1106  | .1261  | .1363   | .1491   | .1501   |
| 10   | 10 | .6471  | .6156  | .6820  | .7550  | .9125  | .10010 | .12840 | .14698 | .15863  | .16906  | .16154  |
| 11   | 11 | .6648  | .7490  | .8237  | .8158  | .10808 | .12083 | .14967 | .17061 | .18181  | .19567  | .19905  |
| 12   | 12 | .8189  | .9189  | .10220 | .10881 | .12987 | .15309 | .17360 | .20166 | .241965 | .24315  | .25174  |
| 13   | 13 | 1.0461 | 1.1575 | 1.2452 | 1.2973 | 1.6439 | 1.6438 | 2.2973 | 2.6491 | 2.6831  | 2.6984  | 2.624   |
| 14   | 1  | .6009  | .6024  | .6446  | .6094  | .6255  | .6166  | .1186  | .1012  | .2448   | .2945   | .2589   |
| 2  | 2  | .6137  | .6223  | .6326  | .6485  | .6863  | .6472  | .2289  | .3195  | .3809   | .4281   | .4188   |
| 3  | 3  | .6114  | .6584  | .6767  | .6923  | .7470  | .7459  | .3335  | .4361  | .5035   | .5651   | .4407   |
| 4  | 4  | .6803  | .1053  | .1308  | .1649  | .2414  | .2467  | .4368  | .5690  | .6214   | .6871   | .7566   |
| 5  | 5  | .1291  | .1606  | .1926  | .2342  | .3148  | .4203  | .6412  | .6610  | .7389   | .8082   | .8917   |
| 6  | 6  | .1836  | .2242  | .2612  | .3006  | .4012  | .5179  | .6488  | .7775  | .8589   | .9310   | .9194   |
| 7  | 7  | .2465  | .3028  | .3366  | .3915  | .4934  | .6205  | .7513  | .8981  | .9842   | .10612  | .10532  |
| 8  | 8  | .3770  | .4193  | .4895  | .5925  | .7304  | .8311  | .10767 | .1180  | .11994  | .12067  | .12067  |
| 9  | 9  | .3961  | .4557  | .5107  | .5782  | .7007  | .8498  | .10116 | .11671 | .12644  | .13513  | .14550  |
| 10   | 10 | .4853  | .5619  | .6128  | .6872  | .8209  | .9827  | .11574 | .12751 | .144300 | .15236  | .16556  |
| 11   | 11 | .5878  | .6629  | .7296  | .8117  | .9586  | .11757 | .13268 | .15126 | .16255  | .17286  | .18210  |
| 12   | 12 | .7091  | .7094  | .8680  | .9507  | .11234 | .12711 | .15616 | .17472 | .18777  | .19901  | .20114  |
| 13   | 13 | .8513  | .9563  | 1.0425 | 1.0487 | 1.3376 | 1.5674 | 1.8178 | 2.0778 | 2.2262  | 2.3600  | 2.5167  |
| 14   | 14 | 1.0796 | 1.1062 | 1.2028 | 1.4237 | 1.6732 | 1.9747 | 2.3206 | 2.6730 | 2.9065  | 3.1204  | 3.3223  |
| 15   | 1  | .6009  | .6021  | .6043  | .6088  | .6238  | .6566  | .1169  | .1793  | .2289   | .2767   | .2376   |
| 2  | 2  | .6178  | .6298  | .6364  | .6452  | .6845  | .7175  | .2143  | .2997  | .3577   | .4118   | .4783   |
| 3  | 3  | .6185  | .6443  | .6713  | .6862  | .7167  | .7702  | .3120  | .4210  | .5025   | .5710   | .6225   |
| 4  | 4  | .6745  | .6978  | .7214  | .7432  | .7173  | .8067  | .4681  | .5467  | .6447   | .7201   | .7601   |
| 5  | 5  | .1185  | .1487  | .1795  | .2172  | .2926  | .3014  | .5551  | .6188  | .6915   | .7577   | .8161   |
| 6  | 6  | .1605  | .2062  | .2415  | .2866  | .3721  | .4813  | .6442  | .7253  | .8020   | .8709   | .9344   |
| 7  | 7  | .2259  | .2698  | .3104  | .4563  | .5742  | .7069  | .8153  | .9162  | .9886   | .10752  |         |
| 8  | 8  | .2206  | .3853  | .4420  | .5461  | .6745  | .8151  | .9512  | .10365 | .11126  | .12016  |         |
| 9  | 9  | .4162  | .4671  | .5295  | .6254  | .7483  | .8780  | .9711  | .10754 | .12463  | .14274  |         |
| 10   | 10 | .4603  | .5012  | .5571  | .6274  | .7483  | .8971  | .10577 | .12118 | .13080  | .143938 | .14667  |
| 11   | 11 | .5289  | .5963  | .6577  | .7323  | .8650  | 1.0266 | 1.2700 | 1.3550 | 1.4696  | 1.5522  | 1.6729  |
| 12   | 12 | .6304  | .7040  | .7846  | .8646  | 1.0008 | 1.1762 | 1.3557 | 1.5474 | 1.6612  | 1.7642  | 1.8954  |
| 13   | 13 | .7501  | .8334  | .9088  | 1.0000 | 1.1527 | 1.2485 | 1.5703 | 1.7757 | 1.9045  | 2.0207  | 2.1506  |
| 14   | 14 | .9004  | .9981  | 1.0817 | 1.1861 | 1.3733 | 1.4600 | 1.8509 | 2.0965 | 2.2535  | 2.43960 | 2.65690 |
| 15   | 15 | 1.1162 | 1.3176 | 1.4473 | 1.7046 | 2.0032 | 2.4256 | 2.6760 | 2.9278 | 3.1405  | 3.30117 |         |
| 16   | 1  | .6009  | .6020  | .6043  | .6087  | .6223  | .6532  | .1169  | .1793  | .2289   | .2767   | .2376   |
| 2  | 2  | .6120  | .6194  | .6284  | .6423  | .6755  | .7201  | .2014  | .2832  | .3371   | .4085   | .4521   |
| 3  | 3  | .6360  | .6567  | .6667  | .6891  | .7170  | .7667  | .2031  | .3147  | .4462   | .5008   | .5688   |
| 4  | 4  | .6695  | .6917  | .7134  | .7431  | .2033  | .2855  | .3823  | .4834  | .5484   | .6075   | .6701   |
| 5  | 5  | .1173  | .1385  | .1662  | .2026  | .2733  | .3663  | .4817  | .5817  | .6724   | .7874   |         |
| 6  | 6  | .1574  | .1916  | .2247  | .2668  | .3460  | .4497  | .5656  | .6880  | .7527   | .8180   | .8964   |
| 7  | 7  | .2102  | .2502  | .2881  | .3357  | .4246  | .5363  | .6603  | .7814  | .8578   | .9262   | 1.0081  |
| 8  | 8  | .2140  | .2685  | .3095  | .4088  | .5094  | .6271  | .7502  | .8871  | .9677   | 1.0301  | 1.1248  |
| 9  | 9  | .2328  | .2817  | .4208  | .4888  | .5924  | .7234  | .8638  | .9289  | 1.0835  | 1.1589  | 1.2489  |

TABLE 3 Cont'd.

| PERCENTILE POINTS OF THE CHI (1 D.F.) OPERATOR STATISTICS |         |         |         |        |         |        |         |         |         |        |        |
|---|---------|---------|---------|--------|---------|--------|---------|---------|---------|--------|--------|
| N   | I       | .01     | .025    | .05    | .10     | .25    | .50     | .75     | .90     | .95    |        |
| 16  | 10      | .4035   | .4498   | .5115  | .5748   | .6888  | .8270   | .9764   | 1.1195  | 1.2089 | 1.2886 |
| 11  | 4818    | .5437   | .6002   | .6690  | .7921   | .9203  | 1.0998  | 1.2524  | 1.4277  | 1.4326 | 1.5310 |
| 12  | 5696    | .6275   | .6952   | .7740  | .9073   | 1.0672 | 1.2369  | 1.4032  | 1.5058  | 1.5974 | 1.7640 |
| 13  | 6699    | .7447   | .8124   | .8942  | 1.0397  | 1.2140 | 1.4015  | 1.5813  | 1.6661  | 1.7949 | 1.9149 |
| 14  | 7883    | .8715   | .9466   | 1.0374 | 1.1988  | 1.3929 | 1.6028  | 1.8057  | 1.9337  | 2.0489 | 2.1776 |
| 15  | 9368    | 1.0215  | 1.1171  | 1.2208 | 1.4064  | 1.6319 | 1.8795  | 2.1231  | 2.2788  | 2.4262 | 2.5017 |
| 16  | 1.1501  | 1.2649  | 1.3698  | 1.4984 | 1.7334  | 2.0295 | 2.3693  | 2.7182  | 3.1594  | 3.4193 |        |
| 17  | 1       | .2067   | .3010   | .3938  | .4077   | .4216  | .4521   | .4982   | .5392   | .5639  | .5939  |
| 2   | .0112   | .0183   | .0267   | .0368  | .0716   | .1216  | .1906   | .2666   | .3188   | .3677  | .4284  |
| 3   | .0337   | .0476   | .0626   | .0817  | .1288   | .1945  | .2765   | .3626   | .4200   | .4739  | .5387  |
| 4   | .0651   | .0855   | .1063   | .1163  | .1910   | .2686  | .3612   | .4564   | .5181   | .5746  | .6478  |
| 5   | .1072   | .1206   | .1558   | .1699  | .2465   | .3443  | .4460   | .5481   | .6136   | .6720  | .7444  |
| 6   | .1469   | .1700   | .2100   | .2497  | .3252   | .4271  | .5218   | .6246   | .7094   | .7715  | .8461  |
| 7   | .1958   | .2133   | .2688   | .3135  | .3972   | .5025  | .6198   | .7345   | .8069   | .8719  | .9496  |
| 8   | .2406   | .2927   | .3320   | .3816  | .4730   | .5863  | .6719   | .8318   | .9078   | .9756  | 1.0668 |
| 9   | .3004   | .3650   | .4000   | .4544  | .5521   | .6745  | .8000   | .9338   | .1.0125 | 1.0844 | 1.1904 |
| 10  | .3727   | .4251   | .4733   | .5323  | .6389   | .7482  | .8982   | .1.0423 | 1.1261  | 1.2098 | 1.2898 |
| 11  | .4431   | .5015   | .5520   | .6168  | .7313   | .8693  | .1.0178 | 1.1598  | 1.2483  | 1.3272 | 1.4211 |
| 12  | .5208   | .5835   | .6404   | .7054  | .8225   | .9801  | 1.1384  | 1.2897  | 1.3840  | 1.4681 | 1.5581 |
| 13  | .6077   | .6761   | .7370   | .8127  | .9456   | 1.1044 | 1.2747  | 1.4375  | 1.5391  | 1.6298 | 1.7083 |
| 14  | .7069   | .7818   | .8494   | .9310  | 1.0757  | 1.2487 | 1.4345  | 1.6127  | 1.7243  | 1.8243 | 1.9441 |
| 15  | .8260   | .9070   | .9818   | 1.0720 | 1.2324  | 1.4243 | 1.6328  | 1.8130  | 1.9608  | 2.0756 |        |
| 16  | .9708   | 1.0650  | 1.1500  | 1.2530 | 1.4371  | 1.6607 | 1.9062  | 2.1477  | 2.3023  | 2.4427 | 2.6133 |
| 17  | .1.0257 | .1.1818 | .1.2998 | 1.5274 | 1.7606  | 2.0582 | 2.3915  | 2.7382  | 2.9564  | 3.1777 | 3.4157 |
| 18  | 1       | .0007   | .0018   | .0036  | .0073   | .0190  | .0474   | .0930   | .1511   | .1934  | .2344  |
| 2   | .0106   | .0172   | .0252   | .0375  | .0671   | .1149  | .1798   | .2527   | .3024   | .3491  | .4070  |
| 3   | .0318   | .0449   | .0690   | .0789  | .1216   | .1838  | .2616   | .3444   | .3992   | .4498  | .5118  |
| 4   | .0612   | .0804   | .1050   | .1265  | .1801   | .2537  | .3416   | .4322   | .4911   | .5449  | .6102  |
| 5   | .0965   | .1218   | .1464   | .1786  | .2416   | .3249  | .4214   | .5187   | .5812   | .6378  | .7061  |
| 6   | .1378   | .1680   | .1972   | .2446  | .3059   | .3978  | .5020   | .6053   | .6711   | .7303  | .8016  |
| 7   | .1833   | .2185   | .2520   | .2942  | .3742   | .4779  | .5842   | .6932   | .7622   | .8240  | .8982  |
| 8   | .2332   | .2732   | .3107   | .3574  | .4437   | .5508  | .6689   | .7936   | .8557   | .9202  | .9974  |
| 9   | .2875   | .3321   | .3875   | .4424  | .5122   | .6122  | .7171   | .8175   | .9023   | 1.1007 | 1.1907 |
| 10  | .3465   | .3956   | .4407   | .4961  | .5963   | .7186  | .8499   | .9764   | 1.0555  | 1.1259 | 1.2100 |
| 11  | .4105   | .4641   | .5132   | .5729  | .6801   | .8095  | .9488   | 1.0821  | 1.1651  | 1.2391 | 1.3273 |
| 12  | .4805   | .5487   | .5917   | .6560  | .7707   | .9083  | 1.0559  | 1.1968  | 1.2845  | 1.3627 | 1.4558 |
| 13  | .5575   | .6207   | .6779   | .7471  | .8720   | 1.0169 | 1.1741  | 1.3240  | 1.4175  | 1.5007 | 1.6000 |
| 14  | .6425   | .7121   | .7741   | .8487  | .9811   | 1.1490 | 1.3076  | 1.4669  | 1.5700  | 1.6598 | 1.7673 |
| 15  | .7417   | .8166   | .8633   | .9109  | .1.0991 | 1.2809 | 1.4651  | 1.6418  | 1.8515  | 1.9704 |        |
| 16  | .8575   | .9402   | 1.0147  | 1.0744 | 1.2636  | 1.4565 | 1.6607  | 1.8602  | 1.9861  | 2.0994 | 2.2550 |
| 17  | 1.00027 | 1.0663  | 1.1609  | 1.2831 | 1.4658  | 1.6675 | 1.8910  | 2.1708  | 2.3244  | 2.4637 | 2.6334 |
| 18  | 1.2114  | 1.2746  | 1.4279  | 1.5544 | 1.7858  | 2.0773 | 2.4172  | 2.7568  | 2.9840  | 3.1934 | 3.4112 |
| 19  | 1       | .0007   | .0017   | .0034  | .0069   | .0188  | .0449   | .0883   | .1435   | .1938  | .2230  |
| 2   | .0109   | .0163   | .0239   | .0355  | .0595   | .1099  | .1707   | .2401   | .2876   | .3322  | .3773  |
| 3   | .0300   | .0424   | .0648   | .0746  | .1151   | .1742  | .2483   | .3272   | .3797   | .4280  | .4674  |

## PERCENTILE POINTS OF THE CHI (1 D.F.) CRITERION STATISTICS

| N  | 1      | .01    | .025   | .05    | .10    | .25    | .50    | .75    | .90    | .95    | .975   | .99    |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 19 | 4      | .8578  | .8769  | .9046  | .9195  | .9702  | .9741  | .9741  | .9769  | .9869  | .9873  | .9876  |
| 5  | .8914  | .9149  | .9487  | .9749  | .9794  | .9794  | .9794  | .9794  | .9794  | .9794  | .9794  | .9794  |
| 6  | .8977  | .9582  | .9859  | .9959  | .9959  | .9959  | .9959  | .9959  | .9959  | .9959  | .9959  | .9959  |
| 7  | .9173  | .9723  | .9777  | .9777  | .9777  | .9777  | .9777  | .9777  | .9777  | .9777  | .9777  | .9777  |
| 8  | .9723  | .9862  | .9942  | .9942  | .9942  | .9942  | .9942  | .9942  | .9942  | .9942  | .9942  | .9942  |
| 9  | .9564  | .9714  | .9856  | .9856  | .9856  | .9856  | .9856  | .9856  | .9856  | .9856  | .9856  | .9856  |
| 10 | .9229  | .9770  | .9864  | .9864  | .9864  | .9864  | .9864  | .9864  | .9864  | .9864  | .9864  | .9864  |
| 11 | .9457  | .9790  | .9876  | .9876  | .9876  | .9876  | .9876  | .9876  | .9876  | .9876  | .9876  | .9876  |
| 12 | .9454  | .9790  | .9876  | .9876  | .9876  | .9876  | .9876  | .9876  | .9876  | .9876  | .9876  | .9876  |
| 13 | .9158  | .9747  | .9721  | .9721  | .9721  | .9721  | .9721  | .9721  | .9721  | .9721  | .9721  | .9721  |
| 14 | .9572  | .9557  | .9741  | .9741  | .9741  | .9741  | .9741  | .9741  | .9741  | .9741  | .9741  | .9741  |
| 15 | .9772  | .9760  | .9826  | .9826  | .9826  | .9826  | .9826  | .9826  | .9826  | .9826  | .9826  | .9826  |
| 16 | .9742  | .9742  | .9868  | .9868  | .9868  | .9868  | .9868  | .9868  | .9868  | .9868  | .9868  | .9868  |
| 17 | .9899  | .9899  | .9899  | .9899  | .9899  | .9899  | .9899  | .9899  | .9899  | .9899  | .9899  | .9899  |
| 18 | 1.0326 | 1.1277 | 1.2809 | 1.3113 | 1.4027 | 1.5237 | 1.6427 | 1.7649 | 1.8847 | 1.9877 | 2.0877 | 2.1914 |
| 19 | 1.2202 | 1.2217 | 1.2709 | 1.2809 | 1.2809 | 1.2809 | 1.2809 | 1.2809 | 1.2809 | 1.2809 | 1.2809 | 1.2809 |
| 20 | 1      | .8006  | .8016  | .8022  | .8022  | .8066  | .8172  | .8427  | .8860  | .9167  | .9575  | .9717  |
| 2  | .8005  | .8165  | .8226  | .8227  | .8227  | .8227  | .8227  | .8227  | .8227  | .8227  | .8227  | .8227  |
| 3  | .8285  | .8702  | .8708  | .8708  | .8708  | .8708  | .8708  | .8708  | .8708  | .8708  | .8708  | .8708  |
| 4  | .8667  | .8619  | .8695  | .8733  | .8733  | .8733  | .8733  | .8733  | .8733  | .8733  | .8733  | .8733  |
| 5  | .8864  | .8987  | .9108  | .9108  | .9108  | .9108  | .9108  | .9108  | .9108  | .9108  | .9108  | .9108  |
| 6  | .9274  | .9296  | .9296  | .9296  | .9296  | .9296  | .9296  | .9296  | .9296  | .9296  | .9296  | .9296  |
| 7  | .9296  | .9461  | .9741  | .9741  | .9741  | .9741  | .9741  | .9741  | .9741  | .9741  | .9741  | .9741  |
| 8  | .9263  | .9263  | .9263  | .9263  | .9263  | .9263  | .9263  | .9263  | .9263  | .9263  | .9263  | .9263  |
| 9  | .9262  | .9262  | .9262  | .9262  | .9262  | .9262  | .9262  | .9262  | .9262  | .9262  | .9262  | .9262  |
| 10 | .9261  | .9261  | .9261  | .9261  | .9261  | .9261  | .9261  | .9261  | .9261  | .9261  | .9261  | .9261  |
| 11 | .9260  | .9260  | .9260  | .9260  | .9260  | .9260  | .9260  | .9260  | .9260  | .9260  | .9260  | .9260  |
| 12 | .9259  | .9259  | .9259  | .9259  | .9259  | .9259  | .9259  | .9259  | .9259  | .9259  | .9259  | .9259  |
| 13 | .9258  | .9258  | .9258  | .9258  | .9258  | .9258  | .9258  | .9258  | .9258  | .9258  | .9258  | .9258  |
| 14 | .9257  | .9257  | .9257  | .9257  | .9257  | .9257  | .9257  | .9257  | .9257  | .9257  | .9257  | .9257  |
| 15 | .9256  | .9256  | .9256  | .9256  | .9256  | .9256  | .9256  | .9256  | .9256  | .9256  | .9256  | .9256  |
| 16 | .9255  | .9255  | .9255  | .9255  | .9255  | .9255  | .9255  | .9255  | .9255  | .9255  | .9255  | .9255  |
| 17 | .9254  | .9254  | .9254  | .9254  | .9254  | .9254  | .9254  | .9254  | .9254  | .9254  | .9254  | .9254  |
| 18 | .9253  | .9253  | .9253  | .9253  | .9253  | .9253  | .9253  | .9253  | .9253  | .9253  | .9253  | .9253  |
| 19 | .9252  | .9252  | .9252  | .9252  | .9252  | .9252  | .9252  | .9252  | .9252  | .9252  | .9252  | .9252  |
| 20 | .9251  | .9251  | .9251  | .9251  | .9251  | .9251  | .9251  | .9251  | .9251  | .9251  | .9251  | .9251  |

CONT. ON PAGE 2

## PERCENTILE POINTS OF THE CHI (1 D.F.) ORDER STATISTICS

| N  | I      | .01    | .025   | .05    | .10     | .25    | .50     | .75    | .90    | .95    | .975    | .99     |
|----|--------|--------|--------|--------|---------|--------|---------|--------|--------|--------|---------|---------|
| 21 | 11     | .2274  | .4274  | .6236  | .4739   | .5646  | .6745   | .7972  | .9070  | .9779  | .9911   | .9965   |
| 12 | 3917   | .4462  | .4844  | .5387  | .5344   | .7562  | .8746   | .9524  | .9743  | .9824  | .9842   | .9842   |
| 13 | 4539   | .5106  | .5192  | .5685  | .7085   | .8306  | .9610   | .9853  | .9926  | .9973  | .9980   | .9980   |
| 14 | 5129   | .5675  | .6190  | .6798  | .7878   | .8164  | .8637   | .9182  | .9263  | .9375  | .9421   | .9421   |
| 15 | 5819   | .6405  | .6945  | .7602  | .8737   | .9098  | .9448   | .9725  | .9821  | .9891  | .9943   | .9943   |
| 16 | 6558   | .7138  | .7773  | .8164  | .9182   | .9129  | .9669   | .9834  | .9913  | .9954  | .9987   | .9987   |
| 17 | 7202   | .8002  | .8608  | .9130  | .9874   | .9794  | .9947   | .9982  | .9995  | .9995  | .9995   | .9995   |
| 18 | 8143   | .9019  | .9757  | 1.0059 | 1.1073  | 1.2655 | 1.4456  | 1.7181 | 1.9263 | 1.9231 | 2.0393  | 2.0393  |
| 19 | 9056   | 1.0774 | 1.1118 | 1.1900 | 1.2661  | 1.5328 | 1.7345  | 1.9795 | 2.0327 | 2.1637 | 2.2976  | 2.2976  |
| 20 | 1.0874 | 1.1776 | 1.1625 | 1.3628 | 1.4617  | 1.7586 | 1.9770  | 2.0320 | 2.0826 | 2.5106 | 2.6386  | 2.6386  |
| 21 | 1.2974 | 1.6014 | 1.6076 | 1.6205 | 1.8285  | 2.1385 | 2.4675  | 2.8067 | 2.9107 | 3.2078 | 3.4925  | 3.4925  |
| 22 | 1      | 1.0076 | 1.0014 | 1.0029 | 1.0060  | 1.163  | 1.3889  | 1.7666 | 1.7469 | 1.7602 | 1.947   | 2.199   |
| 2  | 1.0085 | 1.1110 | 1.0205 | 1.0056 | 1.0048  | 1.0043 | 1.481   | 2.020  | 2.0709 | 2.0703 | 2.1196  | 2.4268  |
| 3  | 1.0258 | 1.0264 | 1.0472 | 1.0027 | 1.0027  | 1.0027 | 1.506   | 2.154  | 2.848  | 3.111  | 3.170   | 4.5283  |
| 4  | 1.0694 | 1.0651 | 1.0810 | 1.0126 | 1.0126  | 1.0126 | 1.486   | 2.075  | 2.069  | 2.1570 | 4.4535  | 4.5283  |
| 5  | 1.0780 | 1.0082 | 1.182  | 1.1445 | 1.1662  | 1.2552 | 1.4256  | 1.4276 | 1.4276 | 1.4276 | 1.5868  | 1.5868  |
| 6  | 1.1164 | 1.1460 | 1.186  | 1.1801 | 1.2177  | 1.3227 | 1.4975  | 1.5751 | 1.5751 | 1.5751 | 1.6640  | 1.6640  |
| 7  | 1.1662 | 1.1747 | 1.1818 | 1.2013 | 1.2814  | 1.3814 | 1.4761  | 1.5745 | 1.5745 | 1.5745 | 1.7458  | 1.7458  |
| 8  | 1.1851 | 1.2172 | 1.2476 | 1.2856 | 1.3517  | 1.4445 | 1.5426  | 1.6385 | 1.6390 | 1.6390 | 1.8184  | 1.8184  |
| 9  | 2.2677 | 2.2625 | 2.2955 | 2.3776 | 2.6134  | 2.8774 | 3.106   | 3.107  | 3.107  | 3.107  | 3.2099  | 3.2099  |
| 10 | 2.7113 | 3.1016 | 3.1669 | 3.3016 | 3.4716  | 3.6723 | 3.806   | 3.849  | 3.849  | 3.849  | 3.9782  | 3.9782  |
| 11 | 3.187  | 3.6124 | 3.6124 | 3.6066 | 4.4485  | 4.4297 | 4.6207  | 4.6118 | 4.6118 | 4.6118 | 4.9001  | 4.9001  |
| 12 | 3.693  | 4.1515 | 4.5751 | 5.0984 | 5.0993  | 5.7101 | 8.197   | 8.4210 | 1.0124 | 1.0754 | 1.1652  | 1.1652  |
| 13 | 4.223  | 4.772  | 5.1717 | 6.681  | 7.843   | 9.084  | 1.0266  | 1.1005 | 1.1005 | 1.1005 | 1.1654  | 1.1654  |
| 14 | 4.6812 | 5.3220 | 5.8116 | 6.391  | 7.613   | 9.445  | 10.931  | 11.665 | 11.665 | 11.665 | 13.4728 | 13.4728 |
| 15 | 5.624  | 5.5607 | 5.656  | 7.1116 | 8.103   | 9.476  | 10.561  | 11.06  | 11.06  | 11.06  | 13.6559 | 13.6559 |
| 16 | 6.110  | 6.6718 | 7.240  | 7.897  | 8.041   | 10.305 | 11.845  | 12.203 | 12.203 | 12.203 | 14.9099 | 14.9099 |
| 17 | 6.851  | 7.403  | 7.968  | 8.3757 | 9.912   | 11.411 | 12.2741 | 13.105 | 13.105 | 13.105 | 17.0766 | 17.0766 |
| 18 | 7.678  | 8.7665 | 9.082  | 9.720  | 1.01020 | 1.2560 | 1.6765  | 1.7741 | 1.7741 | 1.7741 | 18.8653 | 18.8653 |
| 19 | 8.610  | 9.753  | 1.0729 | 1.0827 | 1.2244  | 1.3065 | 1.6693  | 1.7606 | 1.7606 | 1.7606 | 20.0507 | 20.0507 |
| 20 | 9.731  | 1.0546 | 1.277  | 1.2152 | 1.3775  | 1.5560 | 1.7563  | 1.8370 | 1.8370 | 1.8370 | 21.158  | 21.158  |
| 21 | 1.117  | 1.2644 | 1.2869 | 1.3816 | 1.5642  | 1.7797 | 2.0166  | 2.2701 | 2.2701 | 2.2701 | 2.7022  | 2.7022  |
| 22 | 1.3139 | 1.4263 | 1.5248 | 1.6479 | 1.8679  | 1.8770 | 2.1569  | 2.4360 | 2.4360 | 2.4360 | 3.5050  | 3.5050  |
| 23 | 1      | 1.0005 | 1.0014 | 1.0028 | 1.0156  | 1.0372 | 1.0734  | 1.1127 | 1.1127 | 1.1127 | 1.1868  | 2.2294  |
| 2  | 1.0082 | 1.0134 | 1.0196 | 1.0293 | 1.0555  | 1.0902 | 1.1419  | 1.2004 | 1.2004 | 1.2004 | 2.2786  | 3.2761  |
| 3  | 1.0246 | 1.0348 | 1.0458 | 1.0613 | 1.0949  | 1.1441 | 1.273   | 1.3763 | 1.3763 | 1.3763 | 3.4590  | 4.8886  |
| 4  | 1.0621 | 1.0621 | 1.0774 | 1.0980 | 1.1401  | 1.1985 | 1.2600  | 1.422  | 1.422  | 1.422  | 4.342   | 4.8886  |
| 5  | 1.0743 | 1.0936 | 1.1128 | 1.1379 | 1.1874  | 1.2535 | 1.3109  | 1.4097 | 1.4097 | 1.4097 | 5.532   | 5.532   |
| 6  | 1.0952 | 1.1265 | 1.1512 | 1.1804 | 1.2465  | 1.3094 | 1.3929  | 1.4765 | 1.4765 | 1.4765 | 6.369   | 6.369   |
| 7  | 1.1391 | 1.1663 | 1.1923 | 1.2252 | 1.2872  | 1.3662 | 1.4553  | 1.5992 | 1.5992 | 1.5992 | 7.102   | 7.102   |
| 8  | 1.1749 | 1.2067 | 1.2457 | 1.2720 | 1.3496  | 1.4243 | 1.5184  | 1.6146 | 1.6146 | 1.6146 | 7.930   | 7.930   |
| 9  | 2.1514 | 2.2406 | 2.2815 | 2.3295 | 2.3720  | 2.4499 | 2.5451  | 2.6489 | 2.7491 | 2.7491 | 3.0455  | 3.0455  |
| 10 | 2.2574 | 2.2949 | 2.3427 | 2.3722 | 2.4499  | 2.5451 | 2.6489  | 2.7491 | 2.7491 | 2.7491 | 3.9349  | 3.9349  |
| 11 | 2.3271 | 2.3427 | 2.3801 | 2.4245 | 2.5033  | 2.6085 | 2.7171  | 2.8213 | 2.8213 | 2.8213 | 4.0126  | 4.0126  |
| 12 | 2.3695 | 2.3933 | 2.4322 | 2.4819 | 2.5697  | 2.6745 | 2.7879  | 2.8638 | 2.8638 | 2.8638 | 4.0955  | 4.0955  |
| 13 | 2.4468 | 2.4894 | 2.4894 | 2.5248 | 2.6331  | 2.7435 | 2.8619  | 2.9499 | 2.9499 | 2.9499 | 4.1815  | 4.1815  |

| PERCENTILE POINTS OF T.I.F CHI 11 D.F.1 GRNFP STATISTICS |       |        |        |        |       |       |        |       |        |        |        |       |
|--|-------|--------|--------|--------|-------|-------|--------|-------|--------|--------|--------|-------|
| N  | I     | .01    | .025   | .05    | .10   | .25   | .50    | .75   | .90    | .95    | .975   | .99   |
| 29   | 14    | 4546   | 5035   | 5488   | 6736  | 1005  | 8163   | 9400  | 10575  | 11306  | 11554  | 12726 |
| 15   | 5169  | 5641   | 6121   | 6599   | 777   | 8937  | 1021   | 11459 | 12222  | 1289   | 14755  |       |
| 16   | 5727  | 6297   | 6801   | 7412   | 8401  | 9760  | 1127   | 1215  | 12615  | 1325   | 14771  |       |
| 17   | 6306  | 6998   | 7538   | 8185   | 9325  | 10674 | 1206   | 13454 | 14308  | 15059  | 15952  |       |
| 18   | 7121  | 7772   | 8347   | 8945   | 10245 | 11676 | 1296   | 14640 | 15529  | 16319  | 17222  |       |
| 19   | 7949  | 8636   | 9241   | 9986   | 1180  | 1281  | 1442   | 15995 | 16954  | 17829  | 18861  |       |
| 20   | 8882  | 9623   | 10247  | 1081   | 12630 | 14161 | 15917  | 17619 | 18626  | 19642  | 20780  |       |
| 21   | 9883  | 10745  | 11572  | 12394  | 13036 | 15780 | 17740  | 19594 | 20911  | 21009  | 23232  |       |
| 22   | 10467 | 11270  | 12100  | 14070  | 15835 | 17997 | 19851  | 21674 | 24164  | 25520  | 27173  |       |
| 23   | 13363 | 14460  | 15450  | 16633  | 18927 | 21742 | 24797  | 28159 | 30581  | 32636  | 3568   |       |
| 24   | 1     | 10005  | 10112  | 10188  | 10187 | 10149 | 10157  | 10704 | 1149   | 1476   | 1795   | 22706 |
| 2  | 10079 | 10129  | 10248  | 10281  | 10503 | 10865 | 11362  | 11925 | 12313  | 12679  | 13137  |       |
| 3  | 10246 | 10393  | 10438  | 10587  | 10909 | 11381 | 1179   | 12622 | 13052  | 1451   | 1543   |       |
| 4  | 10451 | 10594  | 10740  | 10948  | 11342 | 11902 | 1280   | 13286 | 13769  | 14174  | 14693  |       |
| 5  | 10710 | 10895  | 11079  | 1119   | 11794 | 12629 | 13174  | 13933 | 14424  | 14871  | 15415  |       |
| 6  | 11004 | 11228  | 11445  | 11725  | 12263 | 1263  | 13766  | 14572 | 15088  | 15556  | 16121  |       |
| 7  | 11328 | 11584  | 11874  | 12151  | 12745 | 14162 | 15210  | 16236 | 16821  | 1755   | 1821   |       |
| 8  | 11677 | 11972  | 12249  | 12597  | 13245 | 14058 | 14964  | 15852 | 16414  | 16918  | 17523  |       |
| 9  | 12052 | 12178  | 12683  | 13062  | 13761 | 14624 | 15577  | 16503 | 17086  | 17608  | 18233  |       |
| 10   | 12450 | 12807  | 13149  | 13547  | 14297 | 15205 | 16202  | 17167 | 17771  | 18311  | 18755  |       |
| 11   | 12871 | 13259  | 13616  | 14053  | 14842 | 15804 | 16846  | 17848 | 18474  | 19132  | 19677  |       |
| 12   | 13118 | 13737  | 14117  | 14542  | 15417 | 16425 | 1752   | 18552 | 19270  | 19777  | 20465  |       |
| 13   | 13790 | 14237  | 14743  | 15136  | 16015 | 17072 | 1795   | 19285 | 19956  | 20554  | 21265  |       |
| 14   | 14291 | 14767  | 15198  | 15719  | 16634 | 17749 | 18370  | 19053 | 19753  | 20137  | 21217  |       |
| 15   | 14824 | 15310  | 15785  | 16315  | 17378 | 18465 | 19097  | 19866 | 20592  | 21236  | 23073  |       |
| 16   | 15393 | 15920  | 16412  | 16991  | 18014 | 19205 | 19705  | 20705 | 21735  | 22165  | 23165  |       |
| 17   | 16005 | 16574  | 17053  | 17695  | 18772 | 19665 | 20396  | 21396 | 22676  | 23471  | 24176  |       |
| 18   | 16669 | 17272  | 17812  | 18459  | 19636 | 20938 | 21862  | 22711 | 24542  | 25225  | 26122  |       |
| 19   | 17396 | 18038  | 18612  | 19298  | 20074 | 21927 | 23458  | 24373 | 25765  | 26560  | 27508  |       |
| 20   | 18207 | 18893  | 19506  | 19219  | 19727 | 20349 | 21369  | 22621 | 23715  | 24034  | 25062  |       |
| 21   | 19141 | 19877  | 20572  | 21172  | 21714 | 22464 | 23214  | 24271 | 25881  | 26831  | 28072  |       |
| 22   | 19223 | 19810  | 20263  | 20456  | 2156  | 21988 | 22965  | 23870 | 241085 | 242179 | 243496 |       |
| 23   | 19595 | 20503  | 20310  | 21420  | 21605 | 21817 | 220528 | 22838 | 24321  | 25671  | 27116  |       |
| 24   | 19576 | 194664 | 195650 | 198876 | 19911 | 21008 | 21417  | 2494  | 27078  | 2757   | 2780   |       |
| 25   | 1     | 10005  | 10013  | 10026  | 10053 | 10143 | 10343  | 10677 | 11105  | 11420  | 11728  | 12124 |
| 2  | 10076 | 10121  | 10181  | 10269  | 10483 | 10831 | 11209  | 11851 | 12225  | 12579  | 13022  |       |
| 3  | 10226 | 10310  | 10420  | 10553  | 10872 | 11327 | 11902  | 12522 | 12937  | 1323   | 13793  |       |
| 4  | 10569 | 10700  | 10890  | 11287  | 11827 | 12470 | 13150  | 13608 | 14013  | 14521  |        |       |
| 5  | 10857 | 11032  | 11264  | 11721  | 12321 | 13040 | 13781  | 14256 | 14689  | 15214  |        |       |
| 6  | 11384 | 11784  | 11652  | 12169  | 12843 | 13617 | 14394  | 14893 | 15345  | 15892  |        |       |
| 7  | 11757 | 12050  | 12631  | 13361  | 14187 | 15005 | 15527  | 15997 | 16553  |        |        |       |
| 8  | 12151 | 12485  | 13107  | 13890  | 14762 | 15619 | 16162  | 16640 |        |        |        |       |
| 9  | 12564 | 12928  | 13597  | 14629  | 15746 | 16240 | 17082  | 17306 |        |        |        |       |
| 10   | 12997 | 13489  | 14101  | 14981  | 15942 | 16871 | 17453  | 17974 |        |        |        |       |
| 11   | 13449 | 13868  | 14626  | 15550  | 16552 | 17516 | 18119  | 18657 |        |        |        |       |
| 12   | 14166 | 14368  | 15168  | 16136  | 17181 | 18084 | 18804  | 19360 |        |        |        |       |

وَالْمُؤْمِنُونَ هُمُ الْأَوَّلُونَ مَنْ يَعْمَلْ مِنْ حُسْنٍ يَرَهُ

## PERCENTILE POINTS OF THE CHI (11 D.F.) TEST STATISTICS

| N  | 1  | .001  | .025  | .05   | .10   | .25   | .50   | .75   | .90   | .95   | .975  | .99   |
|----|----|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 27 | 8  | .1412 | .1732 | .1978 | .2287 | .2564 | .2592 | .2606 | .2616 | .2614 | .2611 | .2609 |
|    | 9  | .1796 | .2085 | .2356 | .2632 | .2913 | .3086 | .3140 | .3175 | .3175 | .3171 | .3170 |
|    | 10 | .2140 | .2749 | .2749 | .2749 | .3113 | .3489 | .3489 | .3489 | .3489 | .3489 | .3489 |
|    | 11 | .2502 | .2844 | .3159 | .3456 | .3748 | .4166 | .4166 | .4166 | .4166 | .4166 | .4166 |
|    | 12 | .2882 | .3250 | .3586 | .3977 | .4342 | .4636 | .4636 | .4636 | .4636 | .4633 | .4633 |
|    | 13 | .3297 | .3674 | .4031 | .4466 | .4812 | .5180 | .5180 | .5180 | .5180 | .5179 | .5179 |
|    | 14 | .3761 | .4118 | .4496 | .4863 | .5219 | .5674 | .5674 | .5674 | .5674 | .5673 | .5673 |
|    | 15 | .4142 | .4582 | .4981 | .5367 | .5715 | .6132 | .6132 | .6132 | .6132 | .6131 | .6131 |
|    | 16 | .4507 | .4907 | .5301 | .5691 | .6091 | .6504 | .6504 | .6504 | .6504 | .6503 | .6503 |
|    | 17 | .4868 | .5248 | .5648 | .6047 | .6447 | .6856 | .6856 | .6856 | .6856 | .6855 | .6855 |
|    | 18 | .5118 | .5518 | .5918 | .6318 | .6718 | .7128 | .7128 | .7128 | .7128 | .7127 | .7127 |
|    | 19 | .5361 | .5761 | .6161 | .6561 | .6961 | .7371 | .7371 | .7371 | .7371 | .7370 | .7370 |
|    | 20 | .5598 | .5998 | .6398 | .6798 | .7198 | .7598 | .7598 | .7598 | .7598 | .7597 | .7597 |
|    | 21 | .5816 | .6216 | .6616 | .7016 | .7416 | .7826 | .7826 | .7826 | .7826 | .7825 | .7825 |
|    | 22 | .6126 | .6526 | .6926 | .7326 | .7726 | .8136 | .8136 | .8136 | .8136 | .8135 | .8135 |
|    | 23 | .6416 | .6816 | .7216 | .7616 | .8016 | .8426 | .8426 | .8426 | .8426 | .8425 | .8425 |
|    | 24 | .6716 | .7116 | .7516 | .7916 | .8316 | .8726 | .8726 | .8726 | .8726 | .8725 | .8725 |
|    | 25 | .7006 | .7406 | .7806 | .8206 | .8606 | .9016 | .9016 | .9016 | .9016 | .9015 | .9015 |
|    | 26 | .7272 | .7672 | .8072 | .8472 | .8872 | .9282 | .9282 | .9282 | .9282 | .9281 | .9281 |
|    | 27 | .7515 | .7915 | .8315 | .8715 | .9115 | .9525 | .9525 | .9525 | .9525 | .9524 | .9524 |
| 28 | 1  | .8064 | .8064 | .8064 | .8064 | .8064 | .8064 | .8064 | .8064 | .8064 | .8063 | .8063 |
|    | 2  | .8220 | .8219 | .8218 | .8217 | .8216 | .8215 | .8214 | .8213 | .8212 | .8211 | .8210 |
|    | 3  | .8286 | .8286 | .8285 | .8284 | .8283 | .8282 | .8281 | .8280 | .8279 | .8278 | .8277 |
|    | 4  | .8356 | .8356 | .8355 | .8354 | .8353 | .8352 | .8351 | .8350 | .8349 | .8348 | .8347 |
|    | 5  | .8403 | .8403 | .8402 | .8401 | .8400 | .8399 | .8398 | .8397 | .8396 | .8395 | .8394 |
|    | 6  | .8451 | .8451 | .8450 | .8449 | .8448 | .8447 | .8446 | .8445 | .8444 | .8443 | .8442 |
|    | 7  | .8491 | .8491 | .8490 | .8489 | .8488 | .8487 | .8486 | .8485 | .8484 | .8483 | .8482 |
|    | 8  | .8531 | .8531 | .8530 | .8529 | .8528 | .8527 | .8526 | .8525 | .8524 | .8523 | .8522 |
|    | 9  | .8565 | .8565 | .8564 | .8563 | .8562 | .8561 | .8560 | .8559 | .8558 | .8557 | .8556 |
|    | 10 | .8598 | .8598 | .8597 | .8596 | .8595 | .8594 | .8593 | .8592 | .8591 | .8590 | .8589 |
|    | 11 | .8629 | .8629 | .8628 | .8627 | .8626 | .8625 | .8624 | .8623 | .8622 | .8621 | .8620 |
|    | 12 | .8652 | .8652 | .8651 | .8650 | .8649 | .8648 | .8647 | .8646 | .8645 | .8644 | .8643 |
|    | 13 | .8676 | .8676 | .8675 | .8674 | .8673 | .8672 | .8671 | .8670 | .8669 | .8668 | .8667 |
|    | 14 | .8702 | .8702 | .8701 | .8700 | .8699 | .8698 | .8697 | .8696 | .8695 | .8694 | .8693 |
|    | 15 | .8725 | .8725 | .8724 | .8723 | .8722 | .8721 | .8720 | .8719 | .8718 | .8717 | .8716 |
|    | 16 | .8744 | .8744 | .8743 | .8742 | .8741 | .8740 | .8739 | .8738 | .8737 | .8736 | .8735 |
|    | 17 | .8764 | .8764 | .8763 | .8762 | .8761 | .8760 | .8759 | .8758 | .8757 | .8756 | .8755 |
|    | 18 | .8785 | .8785 | .8784 | .8783 | .8782 | .8781 | .8780 | .8779 | .8778 | .8777 | .8776 |
|    | 19 | .8805 | .8805 | .8804 | .8803 | .8802 | .8801 | .8800 | .8799 | .8798 | .8797 | .8796 |
|    | 20 | .8821 | .8821 | .8820 | .8819 | .8818 | .8817 | .8816 | .8815 | .8814 | .8813 | .8812 |
|    | 21 | .8839 | .8839 | .8838 | .8837 | .8836 | .8835 | .8834 | .8833 | .8832 | .8831 | .8830 |
|    | 22 | .8857 | .8857 | .8856 | .8855 | .8854 | .8853 | .8852 | .8851 | .8850 | .8849 | .8848 |
|    | 23 | .8875 | .8875 | .8874 | .8873 | .8872 | .8871 | .8870 | .8869 | .8868 | .8867 | .8866 |
|    | 24 | .8891 | .8891 | .8890 | .8889 | .8888 | .8887 | .8886 | .8885 | .8884 | .8883 | .8882 |
|    | 25 | .8902 | .8902 | .8901 | .8900 | .8900 | .8899 | .8898 | .8897 | .8896 | .8895 | .8894 |
|    | 26 | .8910 | .8910 | .8909 | .8908 | .8907 | .8906 | .8905 | .8904 | .8903 | .8902 | .8901 |
|    | 27 | .8911 | .8911 | .8910 | .8909 | .8908 | .8907 | .8906 | .8905 | .8904 | .8903 | .8902 |

| PERCENTILE POINTS OF THE CHI ( $\chi^2$ ) N.F.1 GMRFR STATISTICS |        |        |        |        |        |         |         |         |         |         |
|--|--------|--------|--------|--------|--------|---------|---------|---------|---------|---------|
| N  | i      | .01    | .05    | .10    | .25    | .50     | .75     | .90     | .95     | .99     |
| 28   | .78    | 1.4297 | 1.5465 | 1.6278 | 1.7562 | 1.9767  | 2.2560  | 2.5689  | 2.8984  | 3.3140  |
| 29   | 1      | 1.0004 | .9011  | .8022  | .6945  | .5124   | .3296   | .0986   | .0958   | .1233   |
| 2  | .0105  | .0106  | .0155  | .0132  | .0416  | .0718   | .1133   | .1606   | .1634   | .1503   |
| 3  | .0194  | .0274  | .0611  | .0844  | .1145  | .1145   | .1444   | .2189   | .2554   | .2245   |
| 4  | .0376  | .0488  | .0608  | .0777  | .1107  | .1575   | .2165   | .2742   | .3136   | .2636   |
| 5  | .0581  | .0734  | .0885  | .1084  | .1414  | .1861   | .2447   | .3123   | .3876   | .3314   |
| 6  | .0820  | .1004  | .1183  | .1382  | .1760  | .2254   | .2980   | .3611   | .4320   | .4283   |
| 7  | .1085  | .1294  | .1409  | .1599  | .1832  | .2119   | .2657   | .3123   | .3879   | .4294   |
| 8  | .1361  | .1603  | .1603  | .1832  | .2129  | .2492   | .3070   | .3793   | .4852   | .5264   |
| 9  | .1659  | .1928  | .1928  | .2179  | .2492  | .2797   | .3456   | .4556   | .5760   | .6278   |
| 10   | .1974  | .2268  | .2540  | .2877  | .3096  | .4256   | .5053   | .5377   | .5872   | .6314   |
| 11   | .2205  | .2622  | .2715  | .3275  | .4079  | .4728   | .5610   | .6443   | .6974   | .7454   |
| 12   | .2652  | .2992  | .3205  | .3686  | .4324  | .4712   | .5113   | .5689   | .6246   | .6846   |
| 13   | .3115  | .3378  | .3709  | .4112  | .4895  | .5708   | .6648   | .7147   | .7879   | .8270   |
| 14   | .3704  | .4179  | .4553  | .5129  | .5811  | .6218   | .7102   | .7810   | .8608   | .9203   |
| 15   | .4774  | .5197  | .4665  | .5110  | .5745  | .6745   | .7743   | .8712   | .9212   | .9824   |
| 16   | .5979  | .6436  | .4206  | .5021  | .5487  | .6311   | .7291   | .8125   | .8816   | .9465   |
| 17   | .6441  | .6902  | .4647  | .5982  | .6462  | .7061   | .7961   | .8738   | .9381   | .9931   |
| 18   | .5972  | .6596  | .5996  | .6505  | .7439  | .8456   | .9576   | .1.0634 | .6974   | .8548   |
| 19   | .6597  | .7222  | .6522  | .7053  | .7055  | .7984   | .9266   | .1.1267 | .8019   | .8608   |
| 20   | .6795  | .7615  | .7079  | .7624  | .8253  | .8615   | .9747   | .1.2945 | .8698   | .9212   |
| 21   | .7186  | .7962  | .7472  | .8253  | .8726  | .9161   | .1.1727 | .9207   | .9816   | .9931   |
| 22   | .7227  | .7870  | .8310  | .8918  | .9027  | .1.1230 | .1.2528 | .1.3792 | .1.5683 | .1.6131 |
| 23   | .7462  | .8072  | .8072  | .8442  | .8462  | .9062   | .9576   | .1.0634 | .1.1559 | .1.1877 |
| 24   | .8556  | .9197  | .8964  | .9646  | .9646  | .9856   | .9856   | .9856   | .1.0634 | .1.2559 |
| 25   | .9336  | 1.0014 | 1.0117 | 1.0336 | 1.0792 | 1.1367  | 1.2694  | 1.3266  | 1.4267  | 1.4337  |
| 26   | 1.0950 | 1.1223 | 1.1598 | 1.2721 | 1.3728 | 1.5234  | 1.7054  | 1.8722  | 1.9722  | 1.9923  |
| 27   | 1.271  | 1.2064 | 1.2064 | 1.3618 | 1.5111 | 1.5804  | 1.9818  | 2.1863  | 2.3068  | 2.4160  |
| 28   | 1.2594 | 1.3480 | 1.3480 | 1.4577 | 1.5236 | 1.6495  | 1.9018  | 2.1209  | 2.3557  | 2.4214  |
| 29   | 1.4598 | 1.5571 | 1.5571 | 1.7724 | 1.9872 | 2.2633  | 2.5804  | 2.8090  | 3.1263  | 3.2956  |
| 30   | 1      | 1.0004 | .9111  | .9021  | .8644  | .8120   | .7286   | .6566   | .6927   | .793    |
| 2  | .0163  | .0163  | .0150  | .0124  | .0642  | .0642   | .0642   | .0642   | .1555   | .2175   |
| 3  | .0287  | .0265  | .0249  | .0249  | .0726  | .1107   | .1503   | .2110   | .2474   | .2803   |
| 4  | .0357  | .0471  | .0588  | .0746  | .1070  | .1523   | .2075   | .2654   | .3036   | .3189   |
| 5  | .0561  | .0790  | .0968  | .1141  | .1365  | .1797   | .2164   | .2549   | .3173   | .3951   |
| 6  | .0790  | .0968  | .1446  | .1698  | .2176  | .2791   | .3491   | .4189   | .4635   | .4904   |
| 7  | .1042  | .1248  | .1446  | .2044  | .2565  | .3223   | .3963   | .4693   | .5157   | .5527   |
| 8  | .1312  | .1545  | .1766  | .2390  | .2962  | .3662   | .4438   | .5159   | .5680   | .6079   |
| 9  | .1498  | .1857  | .2171  | .3618  | .5111  | .6488   | .7463   | .8390   | .8966   | .9478   |
| 10   | .1501  | .1784  | .2447  | .2773  | .3349  | .4107   | .4919   | .5708   | .6205   | .6630   |
| 11   | .2218  | .2524  | .2867  | .3155  | .4155  | .4561   | .5406   | .6223   | .6794   | .7442   |
| 12   | .2550  | .2879  | .3189  | .3454  | .4215  | .5024   | .5902   | .6747   | .7442   | .8109   |
| 13   | .2897  | .3247  | .3567  | .3956  | .4655  | .5499   | .6409   | .7281   | .8025   | .8886   |
| 14   | .3259  | .3630  | .4166  | .4708  | .5986  | .6928   | .7827   | .8747   | .9478   | .9978   |
| 15   | .4637  | .4029  | .4384  | .4813  | .5516  | .6488   | .7463   | .8390   | .8966   | .9478   |
| 16   | .4731  | .4644  | .4817  | .5265  | .5662  | .7077   | .8164   | .8970   | .9564   | .9931   |

| PERCENTILE POINTS OF THE CHI ( $\chi^2$ , D.F.) ORDER STATISTICS |    |        |        |        |        |        |        |        |        |        |        |        |
|--|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| N  | I  | .01    | .025   | .05    | .10    | .25    | .50    | .75    | .90    | .95    | .975   | .99    |
| 30   | 17 | .46444 | .4878  | .5267  | .5736  | .6564  | .7545  | .8587  | .9573  | 1.0185 | 1.0727 | 1.1371 |
|  | 16 | .4877  | .5331  | .5739  | .6228  | .7089  | .8106  | .9184  | .0203  | 1.0333 | 1.1392 | 1.2056 |
|  | 19 | .5331  | .5807  | .6233  | .6743  | .7638  | .8604  | .9810  | 1.0863 | 1.1515 | 1.2093 | 1.2779 |
|  | 20 | .5811  | .6209  | .6754  | .7285  | .8217  | .9113  | .0471  | 1.1562 | 1.2237 | 1.2846 | 1.3544 |
|  | 21 | .6319  | .6840  | .7305  | .7860  | .8831  | .9971  | 1.1173 | 1.2307 | 1.3009 | 1.3630 | 1.4369 |
|  | 22 | .6861  | .7407  | .7897  | .8473  | .9486  | 1.0675 | 1.1928 | 1.3110 | 1.3841 | 1.4490 | 1.5261 |
|  | 23 | .7442  | .8015  | .8525  | .9142  | 1.0102 | 1.1436 | 1.2747 | 1.3985 | 1.4751 | 1.5431 | 1.6241 |
|  | 24 | .8073  | .8675  | .9211  | .9849  | 1.0952 | 1.2269 | 1.3649 | 1.4953 | 1.5762 | 1.6481 | 1.7317 |
|  | 25 | .8764  | .9400  | .9966  | 1.0632 | 1.1816 | 1.3139 | 1.4650 | 1.6046 | 1.6908 | 1.7676 | 1.8592 |
|  | 26 | .9515  | 1.0211 | 1.0812 | 1.1528 | 1.2781 | 1.4577 | 1.5824 | 1.7315 | 1.8246 | 1.9078 | 2.0073 |
|  | 27 | 1.0415 | 1.1140 | 1.1785 | 1.2555 | 1.3906 | 1.5504 | 1.7212 | 1.8840 | 1.9876 | 2.0797 | 2.1904 |
|  | 28 | 1.1437 | 1.2246 | 1.2950 | 1.3793 | 1.5279 | 1.7053 | 1.8968 | 2.0824 | 2.1999 | 2.3059 | 2.4341 |
|  | 29 | 1.2470 | 1.3653 | 1.4445 | 1.5400 | 1.7100 | 1.9164 | 2.1435 | 2.3683 | 2.5129 | 2.6446 | 2.8055 |
|  | 30 | 1.4673 | 1.5731 | 1.6594 | 1.7873 | 2.0032 | 2.2761 | 2.5919 | 2.9195 | 3.1368 | 3.3782 | 3.5868 |

TABLE 3. Contd.

(Page 38)

## PERCENTILE POINTS OF THE UNTABLE ORDER STATISTICS

 $\sigma = 2.0$ 

| N  | r  | .01    | .025    | .05     | .10     | .25     | .50     | .75     | .90     | .95     | .975    | .99      |
|----|----|--------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----------|
| 2  | 1  | .07089 | .11251  | .16015  | .22052  | .33926  | .5887   | .83255  | 1.07298 | 1.22387 | 1.45810 | 1.61743  |
|    | 2  | .32459 | .41486  | .50379  | .61655  | .83255  | 1.10813 | 1.41778 | 1.72329 | 1.91713 | 2.09182 | 2.30126  |
| 3  | 1  | .05788 | .09187  | .13076  | .18740  | .30067  | .48068  | .67978  | .87400  | .99929  | 1.10180 | 1.23897  |
|    | 2  | .26619 | .31472  | .38135  | .46181  | .62852  | .83255  | 1.05820 | 1.27697 | 1.41417 | 1.53665 | 1.68281  |
|    | 3  | .49258 | .58811  | .67787  | .76988  | .97107  | 1.25626 | 1.54662 | 1.82686 | 2.01026 | 2.19611 | 2.39757  |
| 4  | 1  | .05013 | .07956  | .11324  | .16230  | .27818  | .41628  | .58871  | .75871  | .86541  | .96032  | 1.07298  |
|    | 2  | .20714 | .26451  | .32048  | .39218  | .52744  | .72088  | .88575  | 1.06677 | 1.17978 | 1.28014 | 1.39998  |
|    | 3  | .38966 | .46457  | .53667  | .61156  | .78054  | .97602  | 1.18937 | 1.39571 | 1.52537 | 1.64165 | 1.78218  |
|    | 4  | .61655 | .71196  | .80019  | .89202  | 1.10813 | 1.40580 | 1.63328 | 1.91045 | 2.09874 | 2.25071 | 2.44698  |
| 5  | 1  | .04183 | .07116  | .10128  | .16516  | .22487  | .37223  | .52656  | .67861  | .77406  | .85894  | .95970   |
|    | 2  | .18229 | .23228  | .28199  | .35010  | .46409  | .61368  | .77812  | .92638  | 1.03500 | 1.12261 | 1.22668  |
|    | 3  | .33416 | .39820  | .45864  | .51217  | .66729  | .80266  | 1.01154 | 1.18315 | 1.29022 | 1.38558 | 1.49924  |
|    | 4  | .50112 | .57749  | .64645  | .72351  | .80840  | 1.07165 | 1.28106 | 1.47891 | 1.60351 | 1.71531 | 1.84957  |
|    | 5  | .71252 | .80649  | .89226  | .98482  | 1.19000 | 1.42085 | 1.69027 | 1.96731 | 2.14120 | 2.29061 | 2.49211  |
| 6  | 1  | .04093 | .06646  | .09246  | .13221  | .21097  | .33989  | .48068  | .61940  | .70660  | .78410  | .87609   |
|    | 2  | .14471 | .21032  | .25428  | .31172  | .41221  | .55620  | .70266  | .84698  | .93370  | 1.01267 | 1.10594  |
|    | 3  | .20755 | .25456  | .30723  | .37358  | .50252  | .72070  | .89757  | 1.04834 | 1.14210 | 1.22539 | 1.32441  |
|    | 4  | .45593 | .50201  | .56242  | .63560  | .76047  | .92900  | 1.10195 | 1.24685 | 1.37977 | 1.46113 | 1.57108  |
|    | 5  | .59061 | .66660  | .73595  | .80220  | .92102  | 1.15220 | 1.34105 | 1.54252 | 1.66334 | 1.77208 | 1.90282  |
|    | 6  | .76988 | .88212  | .96636  | 1.07974 | 1.25634 | 1.48845 | 1.74972 | 2.01268 | 2.18317 | 2.33883 | 2.52839  |
| 7  | 1  | .03789 | .06016  | .08560  | .12268  | .20222  | .31460  | .44562  | .57353  | .65519  | .72594  | .81110   |
|    | 2  | .19141 | .23335  | .29421  | .35654  | .48532  | .60032  | .74544  | .87722  | .95757  | .92977  | 1.01540  |
|    | 3  | .27099 | .32286  | .37126  | .43115  | .54018  | .67286  | .81592  | .95226  | 1.03682 | 1.11195 | 1.20106  |
|    | 4  | .39175 | .45100  | .50528  | .57144  | .69007  | .83265  | .95520  | 1.13047 | 1.22075 | 1.30098 | 1.39643  |
|    | 5  | .51924 | .58773  | .64609  | .71919  | .84932  | 1.00513 | 1.17221 | 1.33195 | 1.43172 | 1.52077 | 1.62722  |
|    | 6  | .66411 | .73955  | .80782  | .89041  | 1.03715 | 1.21202 | 1.40427 | 1.59391 | 1.71184 | 1.81802 | 1.96600  |
|    | 7  | .84623 | .94676  | 1.02217 | 1.12776 | 1.31021 | 1.53673 | 1.79229 | 2.05042 | 2.21886 | 2.37149 | 2.55867  |
| 8  | 1  | .03544 | .05626  | .08007  | .11475  | .18953  | .29435  | .41628  | .51649  | .61194  | .67905  | .75871   |
|    | 2  | .14090 | .17622  | .21794  | .27446  | .36856  | .47288  | .59045  | .72200  | .79760  | .86645  | .94417   |
|    | 3  | .25054 | .29847  | .34320  | .39853  | .49220  | .62163  | .75350  | .87901  | .95683  | 1.02580 | 1.10761  |
|    | 4  | .36995 | .41328  | .46204  | .52346  | .63176  | .76146  | .89043  | 1.02214 | 1.12778 | 1.18619 | 1.27219  |
|    | 5  | .47002 | .52996  | .58631  | .65013  | .76626  | .89569  | 1.05625 | 1.19521 | 1.28280 | 1.36067 | 1.45346  |
|    | 6  | .58911 | .65536  | .71568  | .78709  | .91472  | 1.06458 | 1.22243 | 1.36503 | 1.48230 | 1.56319 | 1.67317  |
|    | 7  | .72645 | .80093  | .86809  | .96910  | 1.09317 | 1.26741 | 1.45632 | 1.63679 | 1.75246 | 1.85560 | 1.98224  |
|    | 8  | .90902 | .99791  | 1.07373 | 1.17723 | 1.35580 | 1.57764 | 1.82846 | 2.08240 | 2.24785 | 2.39943 | 2.58461  |
| 9  | 1  | .03342 | .05306  | .07549  | .10820  | .17879  | .27752  | .39247  | .50581  | .57694  | .64022  | .71532   |
|    | 2  | .13232 | .16206  | .20467  | .25039  | .33668  | .44496  | .56376  | .67782  | .74873  | .81163  | .88619   |
|    | 3  | .24741 | .29902  | .32072  | .37240  | .46642  | .58069  | .70369  | .82067  | .89315  | .95735  | 1.03345  |
|    | 4  | .33150 | .38384  | .42091  | .48603  | .58541  | .70466  | .83495  | .95647  | 1.03162 | 1.09332 | 1.17737  |
|    | 5  | .43300 | .48813  | .53806  | .59838  | .70535  | .83255  | .96777  | 1.09579 | 1.17509 | 1.24644 | 1.32902  |
|    | 6  | .53630 | .59638  | .65161  | .71810  | .83016  | .96320  | 1.11107 | 1.26850 | 1.33392 | 1.40990 | 1.50043  |
|    | 7  | .64894 | .71461  | .77362  | .84650  | .96765  | 1.11865 | 1.27756 | 1.42972 | 1.54242 | 1.61003 | 1.71199  |
|    | 8  | .78022 | .85369  | .91977  | .99034  | 1.14060 | 1.31031 | 1.49464 | 1.67352 | 1.78707 | 1.88956 | 2.01340  |
|    | 9  | .95656 | 1.04396 | 1.12332 | 1.21999 | 1.39521 | 1.61307 | 1.85986 | 2.11032 | 2.27382 | 2.42381 | 2.60728  |
| 10 | 1  | .03170 | .05032  | .07162  | .10265  | .16961  | .26328  | .37233  | .47985  | .54733  | .60736  | .67861   |
|    | 2  | .12514 | .15979  | .19356  | .23679  | .31839  | .42077  | .53209  | .64090  | .70792  | .76734  | .83779   |
|    | 3  | .22062 | .26281  | .30217  | .35086  | .46249  | .56497  | .66272  | .77273  | .84086  | .89110  | .97267   |
|    | 4  | .31281 | .36000  | .40318  | .45576  | .54978  | .66231  | .78226  | .89576  | .96591  | 1.02803 | 1.10165  |
|    | 5  | .40178 | .45512  | .50150  | .55771  | .65716  | .77519  | .89044  | 1.01075 | 1.09100 | 1.15671 | 1.23358  |
|    | 6  | .49632 | .55114  | .60145  | .66128  | .76674  | .89149  | 1.02246 | 1.14861 | 1.22601 | 1.29468 | 1.37629  |
|    | 7  | .59277 | .65246  | .70700  | .77316  | .89406  | 1.01762 | 1.16923 | 1.29362 | 1.3777  | 1.47100 | 1.56041  |
|    | 8  | .70101 | .76604  | .82428  | .89659  | 1.01760 | 1.16300 | 1.31899 | 1.46822 | 1.54167 | 1.64528 | 1.74553  |
|    | 9  | .82733 | .89690  | .94888  | 1.06313 | 1.18149 | 1.34853 | 1.52945 | 1.70559 | 1.81761 | 1.91836 | 2.004070 |
|    | 10 | .99842 | 1.08464 | 1.16262 | 1.25757 | 1.42095 | 1.64725 | 1.88766 | 2.11500 | 2.22681 | 2.44542 | 2.62740  |

## PERCENTILE POINTS OF THE VETRINE ORDER STATISTICS

 $\gamma = 1.6$ 

| $n$ | $k$ | .01     | .025     | .05      | .10      | .25      | .50      | .75      | .90     | .95      | .975     | .99      |         |
|-----|-----|---------|----------|----------|----------|----------|----------|----------|---------|----------|----------|----------|---------|
| ^   | 1   | 1.12135 | 1.17436  | 1.23100  | 1.29808  | 1.46042  | 1.65651  | 1.86362  | 1.95797 | 1.17541  | 1.27764  | 1.39600  |         |
|     | 2   | 1.40651 | 1.49468  | 1.57718  | 1.67916  | 1.86332  | 1.99561  | 1.32217  | 1.94557 | 1.68328  | 1.80474  | 1.94792  |         |
| ^   | 3   | 1.10223 | 1.16000  | 1.19647  | 1.21195  | 1.23442  | 1.254    | 1.24444  | 1.29958 | 1.32944  | 1.38520  | 1.418700 |         |
|     | 2   | 1.32606 | 1.32558  | 1.34321  | 1.34374  | 1.38970  | 1.36163  | 1.04532  | 1.31603 | 1.31968  | 1.41013  | 1.41665  |         |
|     | 3   | 1.56792 | 1.65299  | 1.73268  | 1.82804  | 1.95765  | 1.20022  | 1.41766  | 1.62607 | 1.75440  | 1.86955  | 2.00615  |         |
| ^   | 4   | 1.09123 | 1.13199  | 1.17507  | 1.22348  | 1.36893  | 1.49603  | 1.65451  | 1.80179 | 1.89079  | 1.96813  | 1.95797  |         |
|     | 2   | 1.28380 | 1.36513  | 1.40259  | 1.47292  | 1.59913  | 1.75071  | 1.90791  | 1.05937 | 1.14141  | 1.21860  | 1.30887  |         |
|     | 3   | 1.47145 | 1.54155  | 1.60595  | 1.62548  | 1.62721  | 1.98072  | 1.14482  | 1.30569 | 1.40185  | 1.48656  | 1.58666  |         |
|     | 4   | 1.6     | 1.7      | 1.76202  | 1.81767  | 1.92657  | 1.92117  | 1.22412  | 1.48002 | 1.6784   | 1.80264  | 1.91362  | 2.04509 |
| ^   | 5   | 1.08342 | 1.12072  | 1.16012  | 1.21156  | 1.21914  | 1.45367  | 1.59862  | 1.73313 | 1.81472  | 1.88564  | 1.97763  |         |
|     | 2   | 1.25621 | 1.31157  | 1.36324  | 1.42686  | 1.56110  | 1.67663  | 1.81816  | 1.94877 | 1.92790  | 1.99604  | 1.17757  |         |
|     | 3   | 1.41604 | 1.47872  | 1.53566  | 1.59173  | 1.72341  | 1.86363  | 1.00922  | 1.14601 | 1.22611  | 1.29809  | 1.38260  |         |
|     | 4   | 1.57638 | 1.64452  | 1.70664  | 1.7842   | 1.90022  | 1.96617  | 1.11115  | 1.26758 | 1.65901  | 1.53983  | 1.63553  |         |
|     | 5   | 1.76240 | 1.81194  | 1.91220  | 1.99874  | 1.15000  | 1.33117  | 1.52756  | 1.71030 | 1.83877  | 1.94681  | 2.07612  |         |
| ^   | 6   | 1       | 1.07765  | 1.11223  | 1.14885  | 1.19852  | 1.29669  | 1.42176  | 1.55652 | 1.68175  | 1.75743  | 1.82318  | 1.89958 |
|     | 2   | 1.21625 | 1.28728  | 1.33491  | 1.39456  | 1.49882  | 1.62364  | 1.75347  | 1.87493 | 1.94660  | 1.00906  | 1.08389  |         |
|     | 3   | 1.37918 | 1.43624  | 1.48786  | 1.49994  | 1.58568  | 1.78568  | 1.91718  | 1.03849 | 1.11215  | 1.17657  | 1.25206  |         |
|     | 4   | 1.51458 | 1.57621  | 1.63121  | 1.69577  | 1.81095  | 1.94327  | 1.08076  | 1.20831 | 1.28262  | 1.35471  | 1.43535  |         |
|     | 5   | 1.66403 | 1.72723  | 1.78269  | 1.85327  | 1.97477  | 1.12002  | 1.272215 | 1.41448 | 1.59266  | 1.68067  | 1.67309  |         |
|     | 6   | 1.82804 | 1.90453  | 1.97300  | 1.105609 | 1.200230 | 1.37463  | 1.56450  | 1.74993 | 1.86756  | 1.97333  | 2.10027  |         |
| ^   | 7   | 1       | 1.07292  | 1.10552  | 1.13995  | 1.18665  | 1.22895  | 1.39456  | 1.52324 | 1.64098  | 1.71213  | 1.77396  | 1.84578 |
|     | 2   | 1.22087 | 1.26868  | 1.31310  | 1.37191  | 1.46520  | 1.58200  | 1.70451  | 1.81654 | 1.88434  | 1.94341  | 1.01220  |         |
|     | 3   | 1.35185 | 1.40477  | 1.45262  | 1.51016  | 1.61008  | 1.72835  | 1.84080  | 1.91612 | 1.92039  | 1.08860  | 1.15785  |         |
|     | 4   | 1.47250 | 1.52886  | 1.57920  | 1.63913  | 1.73220  | 1.86343  | 1.98814  | 1.10308 | 1.17301  | 1.23429  | 1.30622  |         |
|     | 5   | 1.52126 | 1.58187  | 1.70507  | 1.76819  | 1.87672  | 1.00410  | 1.14444  | 1.25774 | 1.32256  | 1.39847  | 1.47624  |         |
|     | 6   | 1.70765 | 1.78556  | 1.84346  | 1.91332  | 1.03021  | 1.16860  | 1.31160  | 1.45201 | 1.53734  | 1.61316  | 1.70339  |         |
|     | 7   | 1.88157 | 1.95564  | 1.92119  | 1.10006  | 1.25122  | 1.41012  | 1.59457  | 1.77606 | 1.89138  | 1.99534  | 2.12037  |         |
| ^   | 8   | 1       | 1.06913  | 1.10003  | 1.13267  | 1.17694  | 1.26444  | 1.37592  | 1.49603 | 1.60765  | 1.67510  | 1.73371  | 1.80179 |
|     | 2   | 1.20851 | 1.25388  | 1.29568  | 1.34732  | 1.46018  | 1.55021  | 1.66494  | 1.7060  | 1.83450  | 1.89017  | 1.95508  |         |
|     | 3   | 1.33046 | 1.38011  | 1.42195  | 1.47004  | 1.57461  | 1.68366  | 1.79738  | 1.90198 | 1.96531  | 1.102059 | 1.16820  |         |
|     | 4   | 1.44669 | 1.49221  | 1.54002  | 1.59570  | 1.65262  | 1.71952  | 1.81952  | 1.02563 | 1.09003  | 1.14637  | 1.21232  |         |
|     | 5   | 1.56681 | 1.61722  | 1.67400  | 1.70862  | 1.80858  | 1.92397  | 1.06317  | 1.15339 | 1.22047  | 1.27739  | 1.34868  |         |
|     | 6   | 1.65488 | 1.71314  | 1.76419  | 1.82569  | 1.93115  | 1.15320  | 1.17968  | 1.20768 | 1.27009  | 1.33397  | 1.50505  |         |
|     | 7   | 1.77440 | 1.83722  | 1.89300  | 1.95907  | 1.02386  | 1.20798  | 1.34936  | 1.43118 | 1.56637  | 1.64042  | 1.72872  |         |
|     | 8   | 1.92653 | 1.99833  | 1.101260 | 1.14263  | 1.22673  | 1.34404  | 1.62057  | 1.79825 | 1.91168  | 2.01413  | 2.13765  |         |
| ^   | 9   | 1       | 1.06594  | 1.09543  | 1.12657  | 1.16880  | 1.24227  | 1.38462  | 1.47320 | 1.57968  | 1.64405  | 1.70924  | 1.76492 |
|     | 2   | 1.19829 | 1.24112  | 1.28308  | 1.33029  | 1.41857  | 1.52324  | 1.63224  | 1.73264 | 1.79335  | 1.84622  | 1.90787  |         |
|     | 3   | 1.31203 | 1.36008  | 1.40262  | 1.45276  | 1.53232  | 1.64221  | 1.75422  | 1.85376 | 1.96573  | 1.02667  | 1.08667  |         |
|     | 4   | 1.41543 | 1.46484  | 1.50894  | 1.56142  | 1.64241  | 1.72747  | 1.84562  | 1.96503 | 1.02527  | 1.07792  | 1.13954  |         |
|     | 5   | 1.51191 | 1.56341  | 1.60907  | 1.6610   | 1.76535  | 1.86363  | 1.97613  | 1.07592 | 1.13778  | 1.19195  | 1.25552  |         |
|     | 6   | 1.60756 | 1.66133  | 1.70884  | 1.76696  | 1.86165  | 1.97295  | 1.08791  | 1.16130 | 1.25922  | 1.31268  | 1.39258  |         |
|     | 7   | 1.70756 | 1.76420  | 1.81417  | 1.87454  | 1.97565  | 1.109369 | 1.21668  | 1.23107 | 1.340151 | 1.44375  | 1.54745  |         |
|     | 8   | 1.81992 | 1.88113  | 1.93529  | 1.99048  | 1.11008  | 1.24136  | 1.37997  | 1.50079 | 1.62114  | 1.66374  | 1.75043  |         |
|     | 9   | 1.96500 | 1.99372  | 1.10978  | 1.17243  | 1.20521  | 1.44556  | 1.64200  | 1.81752 | 1.92932  | 2.01268  | 2.15264  |         |
| ^   | 10  | 1       | 1.06322  | 1.09140  | 1.12134  | 1.16183  | 1.26184  | 1.36392  | 1.45367 | 1.55576  | 1.61746  | 1.67165  | 1.73333 |
|     | 2   | 1.19953 | 1.23059  | 1.26881  | 1.31586  | 1.40022  | 1.50031  | 1.60456  | 1.70654 | 1.75855  | 1.80908  | 1.86798  |         |
|     | 3   | 1.20848 | 1.24336  | 1.28382  | 1.4221   | 1.51724  | 1.61713  | 1.71955  | 1.81362 | 1.87052  | 1.92016  | 1.97808  |         |
|     | 4   | 1.30466 | 1.34161  | 1.40250  | 1.53332  | 1.61975  | 1.71910  | 1.8164   | 1.91569 | 1.97264  | 1.02237  | 1.08051  |         |
|     | 5   | 1.48608 | 1.52272  | 1.57581  | 1.6280   | 1.71470  | 1.81582  | 1.7195   | 1.01497 | 1.07282  | 1.12351  | 1.18286  |         |
|     | 6   | 1.57046 | 1.62136  | 1.66582  | 1.71840  | 1.80856  | 1.8710   | 1.01988  | 1.11772 | 1.17705  | 1.22290  | 1.29115  |         |
|     | 7   | 1.65903 | 1.71150  | 1.75777  | 1.81220  | 1.90611  | 1.91140  | 1.12547  | 1.22875 | 1.29188  | 1.37741  | 1.43249  |         |
|     | 8   | 1.75264 | 1.80794  | 1.85476  | 1.91233  | 1.91332  | 1.91332  | 1.12860  | 1.24703 | 1.35067  | 1.42847  | 1.48934  |         |
|     | 9   | 1.85937 | 1.91200  | 1.97130  | 1.02636  | 1.31320  | 1.32020  | 1.60538  | 1.53285 | 1.61274  | 1.68008  | 1.76939  |         |
|     | 10  | 1.99874 | 1.106101 | 1.12220  | 1.22122  | 1.24411  | 1.24411  | 1.66232  | 1.62450 | 1.69469  | 2.01408  | 2.16581  |         |

## PERCENTILE POINTS OF THE WEIBULL ORDER STATISTICS

 $C = 5.0$ 

| $n$ | $k$ | .01    | .025    | .05     | .10     | .25     | .50     | .75     | .90      | .95     | .975     | .99     |
|-----|-----|--------|---------|---------|---------|---------|---------|---------|----------|---------|----------|---------|
| 2   | 1   | .34722 | .41733  | .48062  | .55505  | .62854  | .80902  | .92932  | 1.02858  | 1.08416 | 1.13025  | 1.18152 |
|     | 2   | .61758 | .70333  | .75971  | .82411  | .89232  | 1.04192 | 1.14986 | 1.24321  | 1.29741 | 1.34341  | 1.39566 |
| 3   | 1   | .31990 | .39489  | .46110  | .51181  | .58252  | .74601  | .85643  | .94846   | .99972  | 1.04221  | 1.08949 |
|     | 2   | .57102 | .62975  | .68004  | .73732  | .83048  | .92922  | 1.02288 | 1.10274  | 1.14869 | 1.18749  | 1.23144 |
|     | 3   | .75334 | .80870  | .85507  | .90997  | .99893  | 1.09558 | 1.19067 | 1.27478  | 1.32457 | 1.36732  | 1.41639 |
| 4   | 1   | .30201 | .36331  | .41811  | .48320  | .59070  | .70429  | .80902  | .89543   | .94182  | .98394   | 1.02858 |
|     | 2   | .53272 | .58748  | .63634  | .68769  | .77494  | .86609  | .95263  | 1.02010  | 1.06837 | 1.10390  | 1.14406 |
|     | 3   | .65592 | .72590  | .77943  | .82470  | .89549  | .99034  | 1.07183 | 1.14266  | 1.18400 | 1.21924  | 1.25955 |
|     | 4   | .80411 | .87294  | .91470  | .96256  | 1.04192 | 1.12058 | 1.21684 | 1.29555  | 1.34263 | 1.38334  | 1.43038 |
| 5   | 1   | .28883 | .34746  | .40015  | .46211  | .56492  | .67355  | .77371  | .85635   | .90262  | .94099   | .98368  |
|     | 2   | .50618 | .55310  | .60269  | .65325  | .71560  | .82258  | .90459  | 1.07405  | 1.01385 | 1.04735  | 1.08515 |
|     | 3   | .65501 | .69160  | .73176  | .77700  | .85065  | .92922  | 1.00440 | .1.06759 | 1.13931 | 1.17584  |         |
|     | 4   | .78584 | .80882  | .84060  | .88341  | .95177  | 1.02095 | 1.10415 | 1.16944  | 1.20789 | 1.24090  | 1.27888 |
|     | 5   | .87321 | .91757  | .95641  | .99237  | 1.07234 | 1.15176 | 1.23594 | 1.31034  | 1.35501 | 1.39528  | 1.44088 |
| 6   | 1   | .22849 | .23501  | .28582  | .34556  | .45469  | .54943  | .64600  | .82568   | .87030  | .90730   | .94846  |
|     | 2   | .48675 | .52500  | .57871  | .62734  | .70627  | .78971  | .86826  | .93484   | .97293  | 1.00497  | 1.04110 |
|     | 3   | .61675 | .66460  | .69297  | .74158  | .81167  | .88728  | .95770  | 1.01006  | 1.05458 | 1.08470  | 1.11895 |
|     | 4   | .71741 | .75008  | .79449  | .83473  | .90047  | .97122  | 1.03960 | 1.09923  | 1.13612 | 1.16392  | 1.19806 |
|     | 5   | .80096 | .85026  | .88458  | .92378  | .98442  | 1.05871 | 1.12790 | 1.18932  | 1.22575 | 1.25717  | 1.29340 |
|     | 6   | .90097 | .95107  | .98641  | 1.02718 | 1.09558 | 1.17245 | 1.26080 | 1.32285  | 1.36558 | 1.40475  | 1.44923 |
| 7   | 1   | .22703 | .22464  | .27410  | .34203  | .45216  | .52922  | .6233   | .80061   | .84388  | .87975   | .91966  |
|     | 2   | .46096 | .51524  | .55112  | .60556  | .68285  | .76348  | .83935  | .90364   | .94039  | .97124   | 1.00613 |
|     | 3   | .59917 | .63622  | .67278  | .71625  | .78145  | .85343  | .92185  | .98062   | 1.01459 | 1.04336  | 1.07603 |
|     | 4   | .68719 | .72724  | .76105  | .79945  | .86209  | .92922  | .97405  | 1.05028  | 1.08305 | 1.11098  | 1.14290 |
|     | 5   | .76919 | .80738  | .83969  | .87446  | .93676  | 1.00205 | 1.06562 | 1.12149  | 1.15437 | 1.18257  | 1.21501 |
|     | 6   | .84898 | .88631  | .91818  | .95467  | 1.01486 | 1.08102 | 1.14647 | 1.20500  | 1.23990 | 1.27010  | 1.30514 |
|     | 7   | .93892 | .97759  | 1.01071 | 1.04927 | 1.11413 | 1.18751 | 1.26288 | 1.33269  | 1.37527 | 1.41257  | 1.45615 |
| 8   | 1   | .26292 | .21420  | .26424  | .32065  | .45424  | .51312  | .59429  | .77952   | .82164  | .85657   | .89541  |
|     | 2   | .45663 | .51524  | .56367  | .60794  | .65346  | .71176  | .81544  | .87786   | .91351  | .94349   | .97728  |
|     | 3   | .57634 | .61454  | .65194  | .69212  | .75737  | .82682  | .89296  | .94972   | .98250  | 1.01024  | 1.04173 |
|     | 4   | .66382 | .70226  | .73487  | .77188  | .81218  | .86981  | .95891  | 1.01273  | 1.04404 | 1.07069  | 1.10108 |
|     | 5   | .73933 | .77571  | .80660  | .84173  | .89291  | .96123  | 1.02173 | 1.07393  | 1.10475 | 1.13110  | 1.16133 |
|     | 6   | .80094 | .84447  | .87447  | .90867  | .96493  | 1.02616 | 1.08613 | 1.13916  | 1.17051 | 1.19749  | 1.22862 |
|     | 7   | .88000 | .91502  | .94472  | .97932  | 1.03427 | 1.09908 | 1.16162 | 1.21786  | 1.25155 | 1.28079  | 1.31481 |
|     | 8   | .96256 | .99916  | 1.03078 | 1.06744 | 1.12948 | 1.20006 | 1.27302 | 1.34029  | 1.38263 | 1.41920  | 1.46204 |
| 9   | 1   | .25672 | .20891  | .25576  | .31085  | .45227  | .50885  | .58790  | .76137   | .80251  | .83662   | .87458  |
|     | 2   | .44539 | .49104  | .53017  | .57471  | .64697  | .72231  | .79513  | .85564   | .89070  | .91990   | .95282  |
|     | 3   | .55049 | .60007  | .63453  | .67361  | .73707  | .80460  | .86887  | .92399   | .95580  | .98272   | 1.01325 |
|     | 4   | .64453 | .68181  | .71343  | .74932  | .80776  | .87023  | .93039  | .98236   | 1.01255 | .1.02821 | 1.06749 |
|     | 5   | .71548 | .75061  | .78043  | .81431  | .86969  | .92932  | .98698  | 1.03727  | 1.06667 | 1.09177  | 1.12050 |
|     | 6   | .77946 | .81322  | .84193  | .87462  | .92925  | .98638  | 1.04303 | 1.09284  | 1.12215 | 1.16729  | 1.17621 |
|     | 7   | .84116 | .87423  | .90243  | .93463  | .98725  | 1.04580 | 1.10294 | 1.15372  | 1.18386 | 1.20986  | 1.23994 |
|     | 8   | .90550 | .93868  | .96710  | .99974  | 1.05573 | 1.11417 | 1.17436 | 1.22872  | 1.26141 | 1.28986  | 1.32304 |
|     | 9   | .98220 | 1.01726 | 1.04762 | 1.08779 | 1.14210 | 1.21077 | 1.28172 | 1.34815  | 1.38900 | 1.42495  | 1.46715 |
| 10  | 1   | .25194 | .20247  | .24824  | .30229  | .45179  | .50436  | .57395  | .74549   | .78578  | .81918   | .85635  |
|     | 2   | .43547 | .48020  | .51847  | .56202  | .63268  | .70733  | .77751  | .83698   | .87095  | .89949   | .93165  |
|     | 3   | .54633 | .58595  | .61952  | .65774  | .71968  | .78557  | .84826  | .90201   | .93302  | .95924   | .98898  |
|     | 4   | .59222 | .64454  | .69534  | .73229  | .78718  | .84806  | .90644  | .95692   | .98622  | 1.01112  | 1.04748 |
|     | 5   | .66676 | .70248  | .75882  | .79171  | .84540  | .90316  | .95892  | 1.00746  | 1.03579 | 1.05996  | 1.08752 |
|     | 6   | .75562 | .78826  | .81498  | .84753  | .89021  | .94500  | 1.00940 | 1.05692  | 1.08492 | 1.10883  | 1.13628 |
|     | 7   | .81180 | .84351  | .87256  | .90128  | .95190  | 1.00497 | 1.06088 | 1.10869  | 1.13661 | 1.16078  | 1.18865 |
|     | 8   | .86705 | .89888  | .92161  | .95421  | 1.00578 | 1.05226 | 1.11711 | 1.16405  | 1.19519 | 1.22038  | 1.24960 |
|     | 9   | .92698 | .95844  | .98440  | 1.01703 | 1.06013 | 1.12705 | 1.18526 | 1.23008  | 1.26994 | 1.29772  | 1.33018 |
|     | 10  | .99937 | 1.03204 | 1.06420 | 1.09400 | 1.15376 | 1.22008 | 1.28932 | 1.35444  | 1.39460 | 1.43002  | 1.47167 |